

The present and future of Hubble tension

Supratik Pal

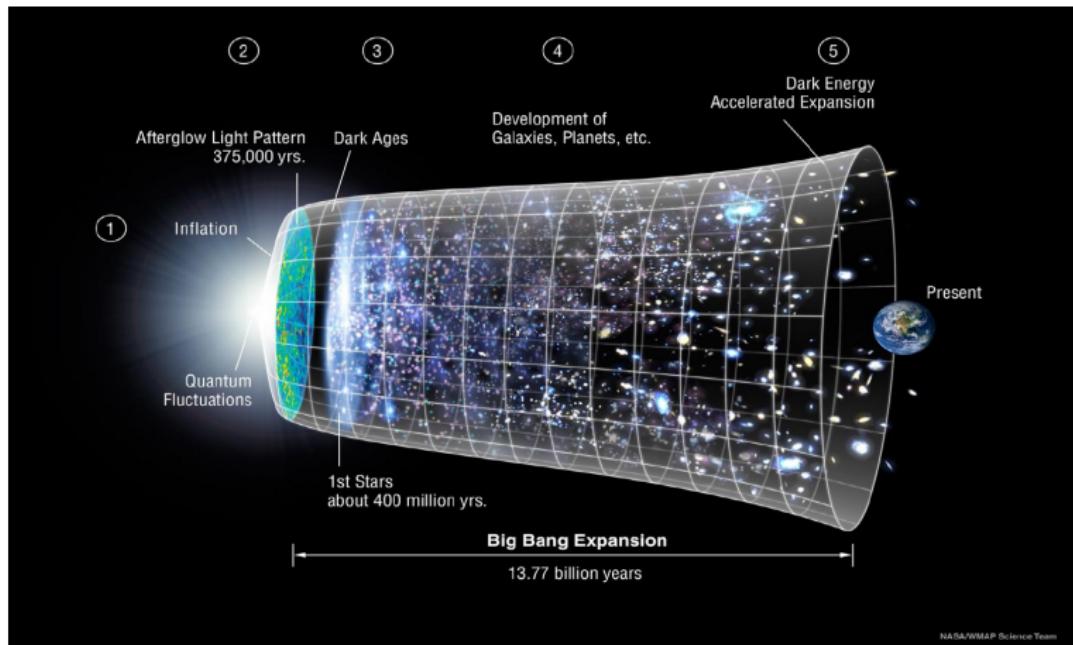
Indian Statistical Institute Kolkata

April 4, 2024

Conclusion



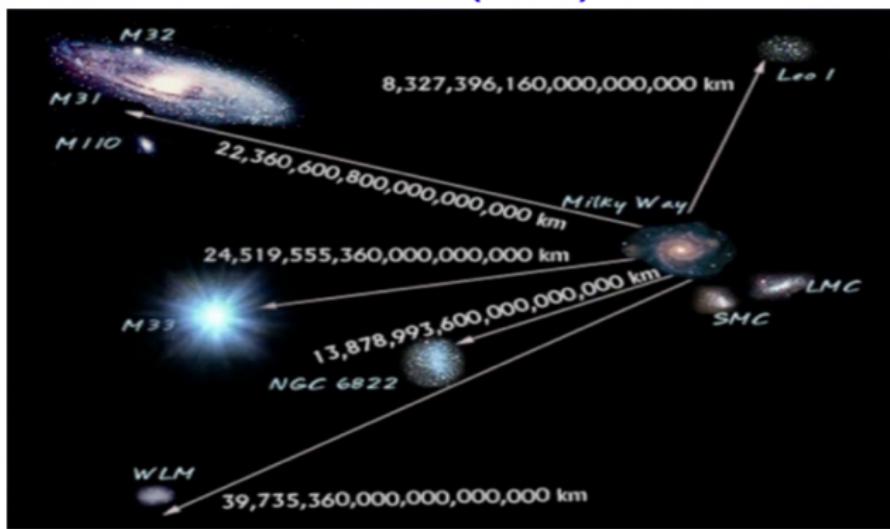
A Cosmologist's wishlist...



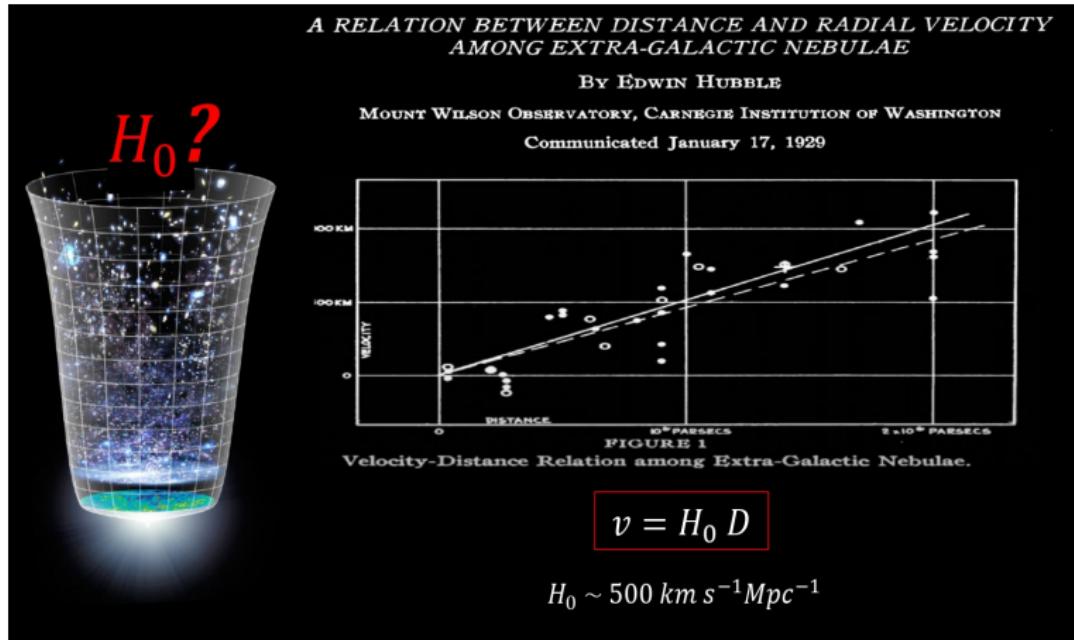
....to explain uniquely!!

The "coolest" parameter: "The constant" a la Hubble

**The grand old man of Observational Cosmology:
Hubble (1929)**

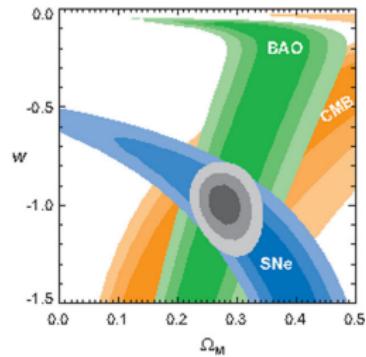
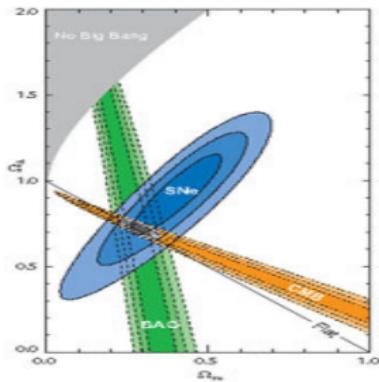


The "coolest" parameter: "The constant" a la Hubble



"The constant" from other observations

CMB, BAO, SNIa...



Universe is accelerating at present \Rightarrow
Measure Hubble parameter indirectly (using a cosmological model)
from these observations

"The constant" a la Planck and SH0ES

Dataset	Value: km/s/Mpc
WMAP9	69.7 ± 2.1
Riess 2011	72.8 ± 2.4
Planck 2013	67.3 ± 1.2
Efstathiou 2014	70.6 ± 3.3
Planck 2015	67.3 ± 1.0
Riess 2016	73.24 ± 1.74
Plank 2018	67.4 ± 0.5
Riess 2018	74.03 ± 1.42
Riess 2020	73.2 ± 1.3
Riess 2022 (SH0ES)	73.04 ± 1.04

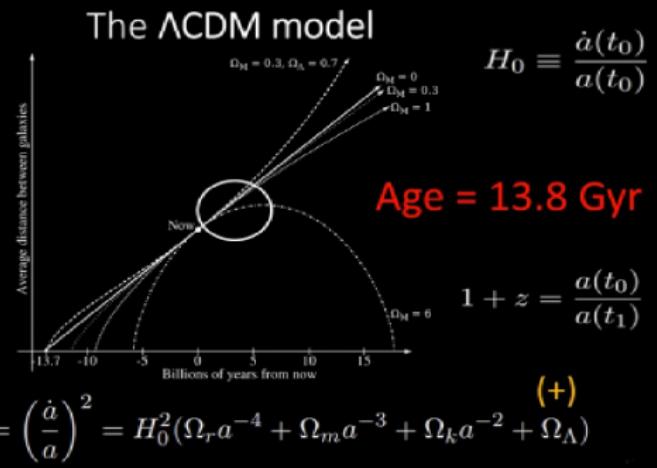
Source of "constant" headache!

Why does the Hubble constant matter?

$H_0 = H(z=0)$ sets all scales in the Universe and $H(z)$ is related to its expansion history (hence the energy-density content)

It allows us to infer:

- Age of the Universe
- Energy budget of luminous sources
- Masses of galaxies and clusters
- Physical scales of cosmic objects
- Dark matter constraints
- Neutrino mass constraints
- Λ CDM extension parameter(s) constraints
- Et cetera!

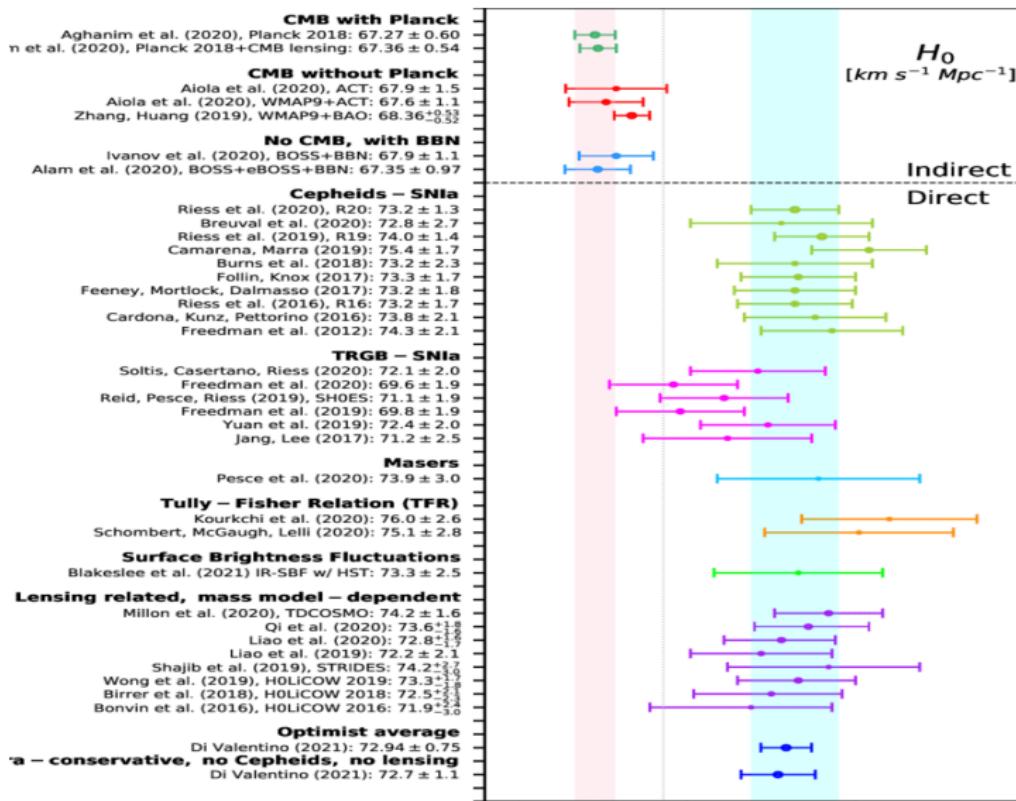


$$H^2(a) = \left(\frac{\dot{a}}{a}\right)^2 = H_0^2(\Omega_r a^{-4} + \Omega_m a^{-3} + \Omega_k a^{-2} + \Omega_\Lambda)$$

Some other datasets in tension with Λ CDM

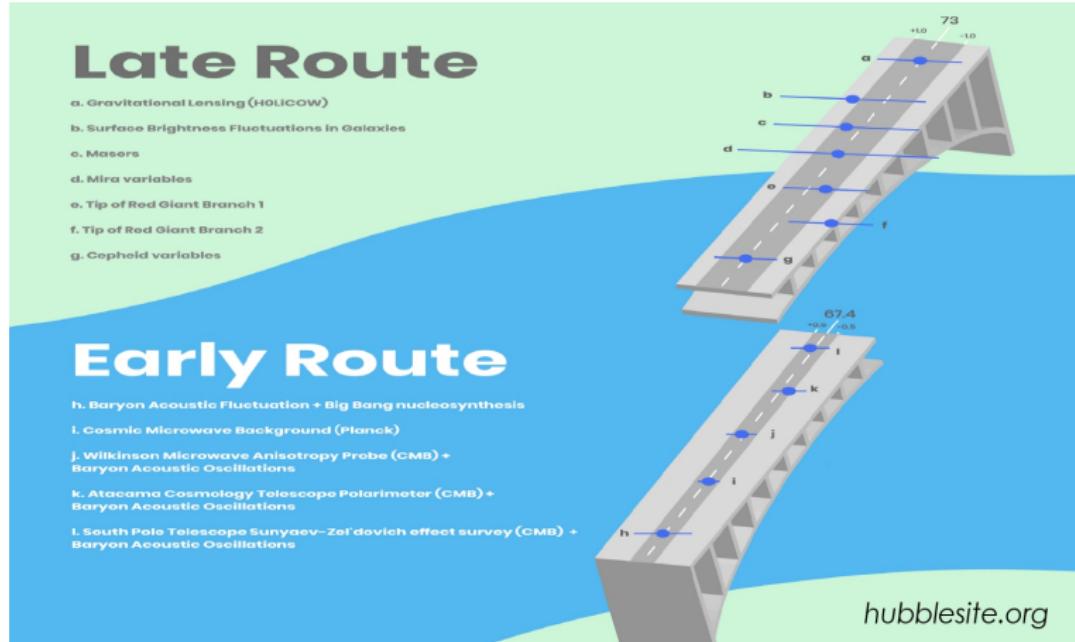
- PAN-STARRS1 data $\rightarrow 2.4\sigma$ Rest et.al., ApJ:2013
- Ly α BAO data ($z = 2.34$) $\rightarrow 2.5\sigma$
- Lensing amplitude $\rightarrow A_L = 1.22 \pm 0.10$ (Planck TT + low P)
- H0LiCOW(lensed quasars) $\rightarrow 4.2\sigma$ Suyu et.al., MNRAS:2016
- H0LiCOW XIII +R18 $\rightarrow 5.3\sigma$ Wong et.al., MNRAS:2020
-

Summary of observations so far: Whisker plot



De Valentino et. al., In the realm of Hubble tension, CQG(2021)

Late time vs early time measurements?



Inverse distance ladder vs low redshift measurements

THE HUBBLE TENSION AS IT STANDS

Not just Planck vs SH0ES...

...but...

"inverse distance ladder" vs "several low-z"
 H_0 measurements!

Very far from a solution ☺

Claimed "solutions" often overstated...
...or just wrong!

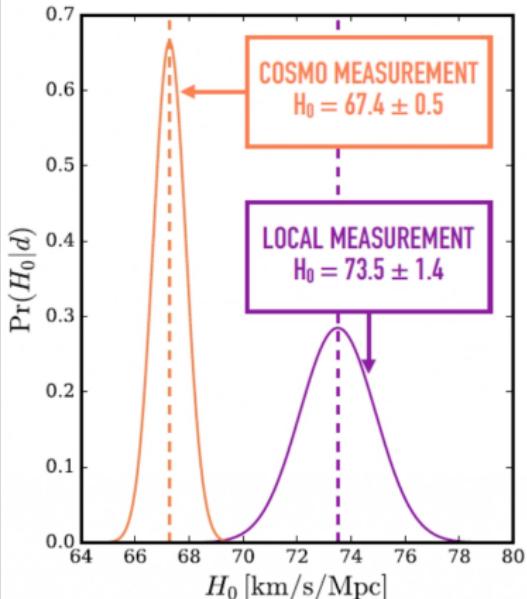
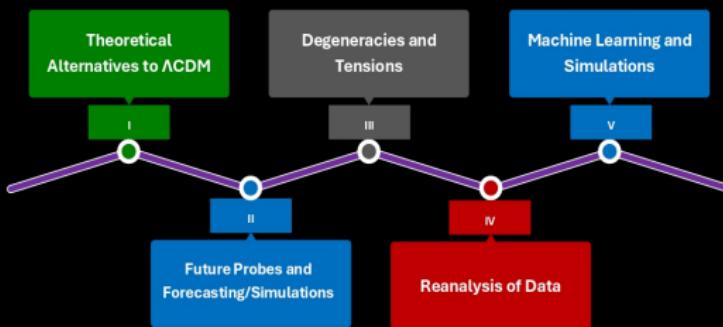


Image credit: Stephen Feeney

Research proposals (and aspirations)

“Tensions and Anomalies in the Age of Precision Cosmology”

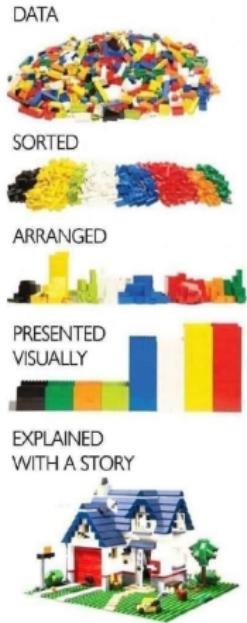


borrowed from Rahul Shah's thesis proposal

Some beyond- Λ CDM Parametrizations

Models	Additional parameters	Motivation
Chevallier-Polarski-Linder (CPL)	w_0, w_a	Simplest dynamical DE parametrization with redshift-varying EoS to resolve the coincidence problem: $w(z) = w_0 + w_a \frac{z}{1+z}$.
Jassal-Bagla-Padmanabhan (JBP)	w_0, w_a	Phenomenologically chosen redshift-dependent DE EoS: $w(z) = w_0 + w_a \frac{z}{(1+z)^2}$.
Phenomenologically Emergent Dark Energy (PEDE)	—	Redshift-dependent DE density parameter to resolve the H_0 tension: $\Omega(z) = (1 - \Omega_{m0})[1 - \tanh(\log_{10}(1 + z))]$.
Vacuum Metamorphosis (VM)	M related to Ω_{m0}	Motivated by non-perturbative effects of quantum gravity where a gravitational phase transition occurs at some critical redshift $z_c = -1 + \frac{3\Omega_{m0}}{4(1-M)}$.
Elaborated Vacuum Metamorphosis (VM-VEV)	M independent of Ω_{m0}	Extension of original VM model allowing a non-vanishing DE component at $z > z_c$, i.e., before the gravitational phase transition.

and there are many more...



A laundry-list/bingo table of mistakes in the literature

Disclaimer: we are (almost?) all sinners

- Leaving out one or more key datasets: BAO, Hubble flow SNels, CMB polarization, (galaxy clustering?)
- Local H_0 prior misuse See warnings in Benevento et al. 2020; Camarena & Marra 2021; Efstathiou 2021
- "Solving" the tension just by inflating error bars but not moving the central value of H_0
- Getting a high H_0 at the expense of a) worsening other tensions (e.g. σ_8), or b) a poor $\Delta\chi^2$ (Bayesian evidence prefers Λ CDM)
- (Uncompelling underlying fundamental physics models)

Take-away message: we don't yet have a solution, claimed solutions are in the best case overstated, in the worst case wrong

Possible reason in current observations?

- H_0 tension

Bhattacharyya, Alam, Pandey, Das, SP: ApJ:2019

Dataset	Value: km/s/Mpc
WMAP9	69.7 ± 2.1
Riess 2011	72.8 ± 2.4
Planck 2013	67.3 ± 1.2
Efstathiou 2014	70.6 ± 3.3
Planck 2015	67.3 ± 1.0
Riess 2016	73.24 ± 1.74
Riess 2018	74.03 ± 1.42
Riess 2020	73.2 ± 1.3
Riess 2022 (SH0ES)	73.04 ± 1.04

Possible reason in current observations?

- H_0 tension

Bhattacharyya, Alam, Pandey, Das, SP: ApJ:2019

Dataset	Value: km/s/Mpc
WMAP9	69.7 ± 2.1
Riess 2011	72.8 ± 2.4
Planck 2013	67.3 ± 1.2
Efstathiou 2014	70.6 ± 3.3
Planck 2015	67.3 ± 1.0
Riess 2016	73.24 ± 1.74
Riess 2018	74.03 ± 1.42
Riess 2020	73.2 ± 1.3
Riess 2022 (SH0ES)	73.04 ± 1.04

- $\sigma_8 (8h^{-1}\text{Mpc})$ tension

Dataset	Value: $S_8 = \sigma_8 \sqrt{\Omega_{0m}/0.3}$
Planck 2015	0.851 ± 0.013
Clusters (X-ray)	0.745 ± 0.039
Weak lensing	0.75 ± 0.04
DES Y3 (2021)	0.784 ± 0.012

Generic Parametrization Scheme

- Consider most generic situation: two fluids (DM-DE), interacting, both perturbed
- Write down background and perturbation equations
- Parametrization: $\{w_{DM,eff}, w_{DE,eff}, C_{sDM,eff}^2, C_{sDE,eff}^2\}$
- Boils down to different models for specific choice
 - * $w_{DM,eff} = 0, w_{DE,eff} = -1, C_{sDM,eff}^2 = 0, C_{sDE,eff}^2 = 0$
⇒ Λ CDM
 - * $w_{DM,eff} = 0, w_{DE,eff} > -1, C_{sDM,eff}^2 = 0, C_{sDE,eff}^2 = 1$
⇒ non-phantom, w_z CDM
 - * $w_{DM,eff} = 0, w_{DE,eff} < -1, C_{sDM,eff}^2 = 0, C_{sDE,eff}^2 = 1$
⇒ phantom, w_z CDM
 - * $w_{DM,eff} = 0, w_{DE,eff} < -1, C_{sDM,eff}^2 = 0, C_{sDE,eff}^2 \neq 1$
⇒ modified gravity
 - * $w_{DM,eff} \neq 0, w_{DE,eff} = -1, C_{sDM,eff}^2 = 0, C_{sDE,eff}^2 = 1$
⇒ warm dark matter
 - * $w_{DM,eff} \neq 0, w_{DE,eff} < -1 \text{ or } > -1, C_{sDM,eff}^2 \neq 0, C_{sDE,eff}^2 \neq 1$
⇒ interacting DM-DE
- Constrain these parameters from data

Parameters (Planck15/ Planck+R16/ Planck+BSH)

Phantom

Data	Model	Ω_{dm}	H_0	σ_8	w_0	w_a	$w_{\text{DM,eff}}$	$c_{\text{sDE,eff}}^2$	χ_{bf}^2	$\chi_{\Lambda\text{CDM}}^2 - \chi_{\text{bf}}^2$
<i>Planck</i>	ΛCDM	$0.30^{+0.02}_{-0.02}$	$68.1^{+1.2}_{-1.2}$	$0.85^{+0.03}_{-0.02}$	-1	0	0	1	781.07	0
	CPLCDM	$0.19^{+0.02}_{-0.04}$	$88.4^{+11.6}_{-3.7}$	$1.02^{+0.08}_{-0.06}$	$-1.5^{+0.3}_{-0.3}$	$-0.13^{+0.27}_{-0.03}$	0	1	779.83	-1.24
	$+w_{\text{DM,eff}}$	$0.62^{+0.32}_{-0.59}$	$66.7^{+32.0}_{-11.1}$	$0.80^{+0.27}_{-0.13}$	$-2.0^{+1.0}_{-1.0}$	$-0.45^{+0.48}_{-1.50}$	$-0.0075^{+0.005}_{-0.004}$	1	778.26	-2.81
	$+c_{\text{sDE,eff}}^2$	$0.68^{+0.32}_{-0.66}$	$64.9^{+11.7}_{-13.5}$	$0.79^{+0.28}_{-0.14}$	$-2.0^{+1.0}_{-1.0}$	$-0.42^{+0.49}_{-1.58}$	$-0.0078^{+0.005}_{-0.004}$	$1.03^{+0.84}_{-0.45}$	778.88	-2.19
<i>Planck</i>	ΛCDM	$0.29^{+0.01}_{-0.01}$	$69.7^{+1.0}_{-1.0}$	$0.86^{+0.02}_{-0.02}$	-1	0	0	1	786.66	0
	CPLCDM	$0.26^{+0.01}_{-0.01}$	$74.0^{+1.7}_{-1.7}$	$0.90^{+0.02}_{-0.03}$	$-1.1^{+0.1}_{-0.1}$	$-0.27^{+0.46}_{-0.26}$	0	1	782.02	-4.64
	$+w_{\text{DM,eff}}$	$0.29^{+0.02}_{-0.02}$	$74.5^{+2.1}_{-2.1}$	$0.88^{+0.03}_{-0.03}$	$-2.0^{+1.0}_{-1.0}$	$-0.96^{+1.10}_{-1.50}$	$-0.005^{+0.001}_{-0.003}$	1	777.65	-9.01
	$+c_{\text{sDE,eff}}^2$	$0.29^{+0.02}_{-0.02}$	$74.5^{+2.1}_{-2.2}$	$0.89^{+0.02}_{-0.02}$	$-2.0^{+1.0}_{-1.0}$	$-0.94^{+1.05}_{-1.65}$	$-0.005^{+0.001}_{-0.002}$	$1.03^{+0.96}_{-0.34}$	780.19	-6.47
<i>Planck</i>	ΛCDM	$0.30^{+0.01}_{-0.01}$	$68.5^{+0.6}_{-0.6}$	$0.86^{+0.02}_{-0.02}$	-1	0	0	1	1490.66	0
	CPLCDM	$0.29^{+0.01}_{-0.01}$	$69.8^{+1.0}_{-1.0}$	$0.87^{+0.02}_{-0.02}$	$-1.05^{+0.05}_{-0.01}$	$-0.15^{+0.21}_{-1.10}$	0	1	1490.29	-0.37
	$+w_{\text{DM,eff}}$	$0.30^{+0.01}_{-0.01}$	$69.7^{+1.0}_{-1.0}$	$0.86^{+0.02}_{-0.02}$	$-1.06^{+0.06}_{-0.01}$	$-0.33^{+0.39}_{-0.19}$	$-0.0012^{+0.001}_{-0.001}$	1	1488.14	-2.52
	$+c_{\text{sDE,eff}}^2$	$0.30^{+0.01}_{-0.01}$	$69.7^{+1.0}_{-1.0}$	$0.86^{+0.02}_{-0.02}$	$-1.06^{+0.06}_{-0.01}$	$-0.34^{+0.40}_{-0.18}$	$-0.0012^{+0.001}_{-0.001}$	$1.02^{+0.98}_{-1.02}$	1488.83	-1.83

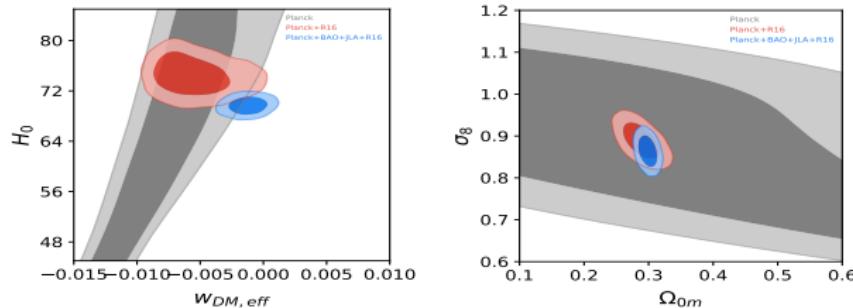
Non-phantom

Data	Model	Ω_{dm}	H_0	σ_8	$w_{0,\text{eff}}$	$w_{a,\text{eff}}$	$w_{\text{DM,eff}}$	$c_{\text{sDE,eff}}^2$	χ_{bf}^2	$\chi_{\Lambda\text{CDM}}^2 - \chi_{\text{bf}}^2$
<i>Planck</i>	ΛCDM	$0.30^{+0.02}_{-0.02}$	$68.1^{+1.2}_{-1.2}$	$0.85^{+0.03}_{-0.02}$	-1	0	0	1	781.07	0
	CPLCDM	$0.37^{+0.03}_{-0.05}$	$62.5^{+4.0}_{-2.7}$	$0.80^{+0.04}_{-0.03}$	$-0.82^{+0.14}_{-0.18}$	$0.03^{+0.22}_{-0.22}$	0	1	782.75	1.68
	$+w_{\text{DM,eff}}$	$1.06^{+0.31}_{-0.47}$	$44.0^{+4.3}_{-2.5}$	$0.60^{+0.05}_{-0.08}$	$-0.68^{+0.35}_{-0.32}$	$0.16^{+0.36}_{-0.40}$	$-0.012^{+0.004}_{-0.006}$	1	782.63	1.56
	$+c_{\text{sDE,eff}}^2$	$1.03^{+0.33}_{-0.43}$	$44.5^{+3.7}_{-8.0}$	$0.60^{+0.04}_{-0.09}$	$-0.68^{+0.05}_{-0.35}$	$0.16^{+0.36}_{-0.40}$	$-0.012^{+0.003}_{-0.006}$	$0.98^{+1.02}_{-0.98}$	780.58	-0.49
<i>Planck</i>	ΛCDM	$0.29^{+0.01}_{-0.01}$	$69.7^{+1.0}_{-1.0}$	$0.86^{+0.02}_{-0.02}$	-1	0	0	1	786.66	0
	CPLCDM	$0.29^{+0.01}_{-0.01}$	$68.6^{+1.3}_{-1.1}$	$0.85^{+0.02}_{-0.02}$	$-0.97^{+0.01}_{-0.03}$	$0.03^{+0.04}_{-0.06}$	0	1	788.97	2.31
	$+w_{\text{DM,eff}}$	$0.25^{+0.02}_{-0.02}$	$72.2^{+1.8}_{-1.8}$	$0.89^{+0.03}_{-0.03}$	$-0.92^{+0.01}_{-0.08}$	$0.05^{+0.48}_{-0.13}$	$0.004^{+0.001}_{-0.001}$	1	785.81	-0.85
	$+c_{\text{sDE,eff}}^2$	$0.25^{+0.02}_{-0.02}$	$72.2^{+1.8}_{-1.8}$	$0.89^{+0.03}_{-0.03}$	$-0.92^{+0.01}_{-0.08}$	$0.05^{+0.10}_{-0.59}$	$0.004^{+0.001}_{-0.002}$	$1.94^{+0.06}_{-1.94}$	785.73	-0.93
<i>Planck</i>	ΛCDM	$0.30^{+0.01}_{-0.01}$	$68.5^{+0.6}_{-0.6}$	$0.86^{+0.02}_{-0.02}$	-1	0	0	1	1490.66	0
	CPLCDM	$0.30^{+0.01}_{-0.01}$	$67.8^{+0.7}_{-0.7}$	$0.85^{+0.02}_{-0.02}$	$-0.97^{+0.01}_{-0.03}$	$0.04^{+0.04}_{-0.08}$	0	1	1493.36	2.70
	$+w_{\text{DM,eff}}$	$0.30^{+0.01}_{-0.01}$	$68.2^{+0.8}_{-0.8}$	$0.85^{+0.02}_{-0.02}$	$-0.96^{+0.01}_{-0.04}$	$0.10^{+0.07}_{-0.14}$	$0.0012^{+0.001}_{-0.001}$	1	1491.01	0.35
	$+c_{\text{sDE,eff}}^2$	$0.30^{+0.01}_{-0.01}$	$68.2^{+0.8}_{-0.8}$	$0.86^{+0.02}_{-0.02}$	$-0.96^{+0.01}_{-0.04}$	$0.09^{+0.06}_{-0.14}$	$0.0012^{+0.001}_{-0.001}$	$0.98^{+1.02}_{-0.98}$	1491.59	0.93

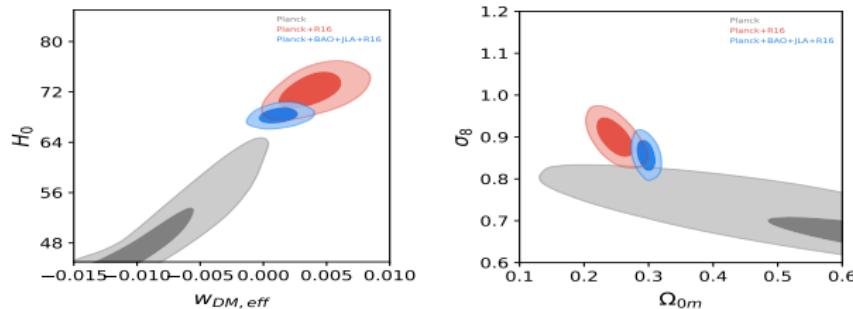


Major results (Planck+BSH)

Phantom

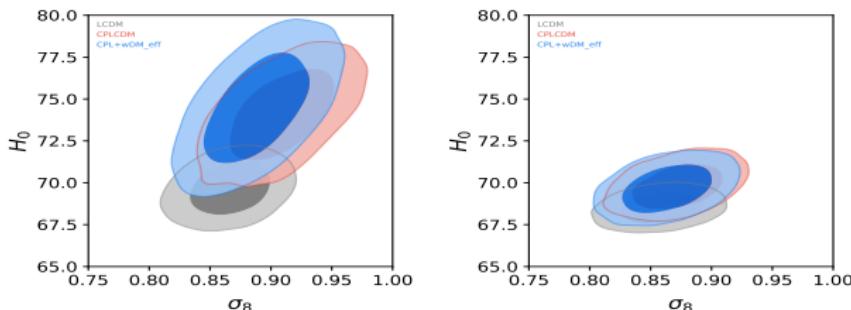


Non-phantom

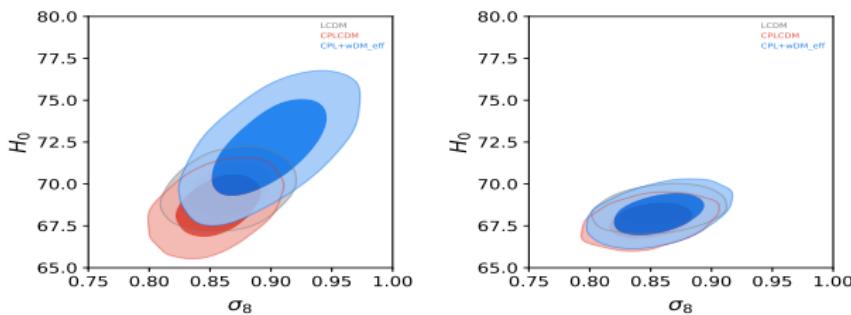


Correlation between H_0 and σ_8 tensions

Phantom



Non-phantom



Strong positive correlation between H_0 and σ_8 is generic to present cosmological data

SO IS IT NEW PHYSICS?

SEE EPIC REVIEW BY VALENTINO+ [2103.01183]

NO THEORETICAL MODIFICATION EXPLAINS TENSION (YET...)

Tension persists

Coupled quint-
essence (Poutsisou+
1604.04222)

$M_\phi = N_{\text{eff}} + w +$
running + $r + A_{\text{tors}}$ (Di
Valentino+1606.0063)

Early dark energy
(Kawala+1608.01309)

Dynamical vacuum
model dark energy
(Sola+1705.06723)

Phantom dark energy
(El-Zant+1809.09390)

however, that it still exhibits tension with local measurements of the Hubble constant. A full model selection

$w < -1$ now present at just ~ 1.1 sigma. The inclusion of the R16 prior in the Planck+BAO dataset produces a worse fit of $\Delta\chi^2 \sim 4.5$. This is due to the tension at the

In order for the best-fit value of H_0 for a Λ CDM + EE universe to coincide with the local measurement, a value of τ greater than its 5 σ Planck-16 value is required. (Such

definitely favors the Planck range for H_0

The model however faces serious problems when baryon acoustic oscillation data are included. This is true for both

σ_8 tension issues

Holographic DE +
sterile v
(Zhao+1703.08456)

DM-v interactions (Di
Valentino+1710.02559)

mic shear; thus we compare our result with the KiDS-450 result. We find a tension at the 1.9 σ level between the two. As discussed in the Planck 2015 paper [2], for

Here we show that it is impossible to solve both tensions simultaneously.

Preliminary

DM-dark rad interactions (Ko+1608.01083)

Twin Higgs (Prilepsina+1611.05879)

Two curvatures (Santos+1611.01885)

Evidence prefers LCDM

N_{eff} (dark rad) (Di Bari+1303.6267)
Sterile v (Wyman+1307.7715)

Non-parametric, time-dependent DE equation of state (Huang+1606.05965)

DM-DE interactions + sterile v
(Kumar+1608.02454)

Vacuum metamorphosis + $N_{\text{eff}} + \text{running} + M_V + A_{\text{tors}}$ (Di Valentino+1710.02153)

Interacting time-varying DE (Yang+1809.06883)
K-mouflage (Benevento+1809.09598)

(see also Verde+SF+1307.2904,
Leistedt+1404.5950, Heavens+1704.03467)

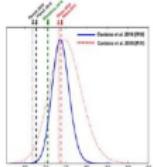
THEN IT MUST BE SYSTEMATICS, RIGHT? NO?

NO PROPOSED SYSTEMATICS EXPLAIN TENSION (YET)...

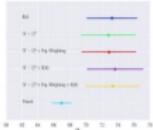
Not obviously systematics...

C
D
L

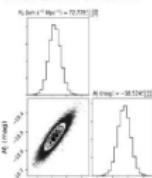
Outlier treatment:
Efstathiou:1311.3461
Cardona+:1611.06088
Feeney+:1707.0007



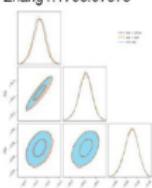
Cepheid color & extinction:
Follin+:1707.01175



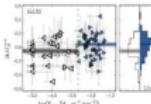
Near-infrared SNe:
Dhawan+:1707.00515



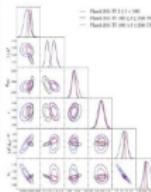
Blind analysis:
Zhang+:1706.07573



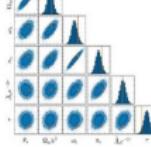
SN environment:
Rigault+:1412.6501 vs
Jones+:1506.02637



Low-high ℓ tension:
Addison+:1511.00055
vs Planck:1608.02487



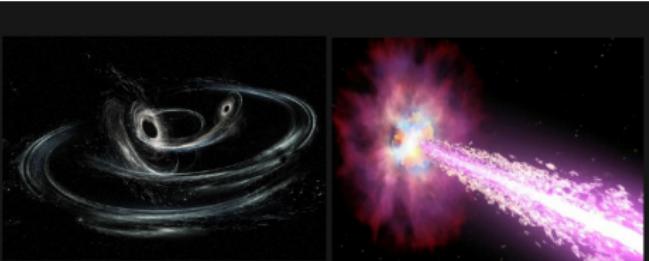
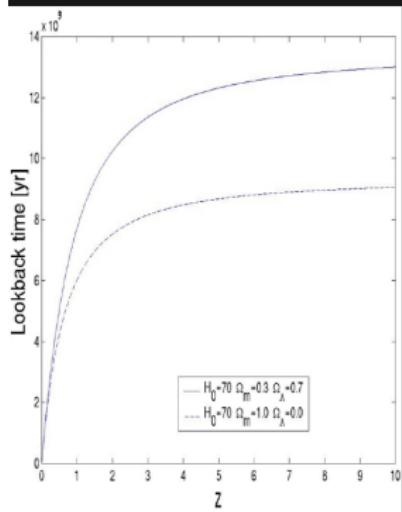
217x217 GHz spectra:
Spergel+:1312.3313



C
M
B

Looking towards future

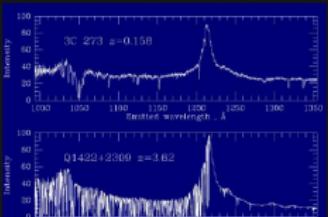
Intermediate Redshifts & Some Perspective



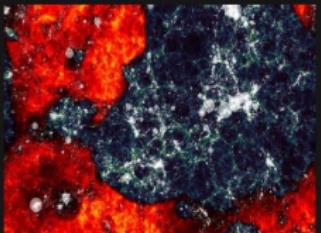
Gravitational Waves



Gamma Ray Bursts



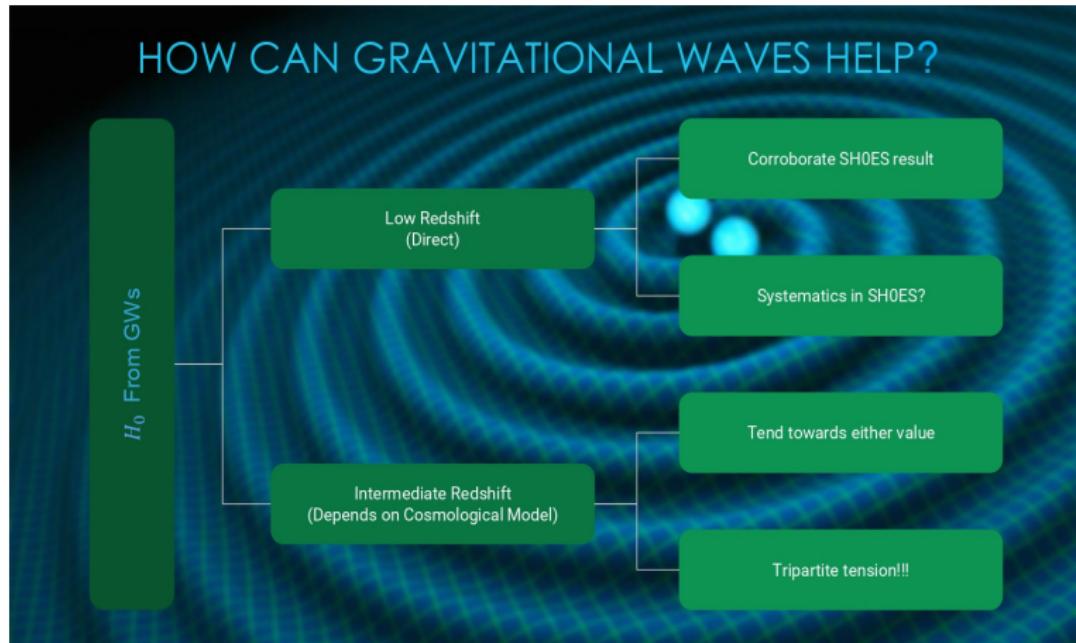
Lyman- α Forest



21-cm Signal from EoR



Future prospects: GW missions



How to get H_0 from Standard Sirens at intermediate redshifts?



Not

$$v = H_0 D$$

But

$$d_L = \frac{c(1+z)}{H_0} \int_0^z \frac{dz'}{E(z')}$$



$$E(z) = \sqrt{\Omega_{0m}(1+z)^3 + (1-\Omega_{0m})e^{3\int_0^{\ln(1+z)} d\ln(1+z')(1+w_{DE}(z'))}}$$

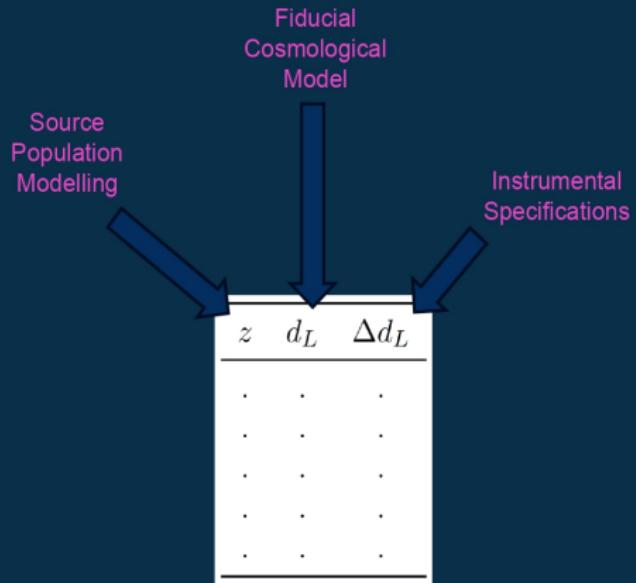
*Schutz, 1986

How to "see" GWs at intermediate redshifts?

Future GW missions!

Wait for / travel to the future? ☽

We can simulate!



Future prospects: GW missions

Baral, Roy, SP, MNRAS:2020

Shah, Bhaumik, Mukherjee, SP, JCAP:2023

Mukherjee, Shah, Bhaumik, SP, ApJ:2024

GW missions under consideration:

- eLISA
- Einstein Telescope

Different approaches used:

A three-pronged approach to forecasting
For a particular model

Fisher Matrix Forecasting	Parameter Estimation using Markov chain Monte Carlo (MCMC)	Non-parametric reconstruction using Gaussian processes (GPs)
Estimate on errors	Estimate on errors	Full reconstruction with errors and mean
No mean shifts	Can shift mean values	Cannot constrain all parameters
Depends on instrumental specifications	Sensitive to assumed cosmological model	Instrument independent and non-parametric

Models under investigation

Choose a fiducial model!

But how?!

"True" Universe unknown.
Choose some motivated by
 H_0 tension?

These may be
good
representative
choices!

Our choices

Baseline Model (6 parameters):
 Λ Cold Dark Matter (Λ CDM) [$\sim 5.0\sigma$]

Alternative models with 6 parameters:
Phenomenologically Emergent Dark Energy (PEDE) [$\sim 1.8\sigma$]
Vacuum Metamorphosis (VM) [$\sim 0.8\sigma$]

1-parameter extension:
Elaborated Vacuum Metamorphosis (VM-VEV) [$\sim 0.04\sigma$]

2-parameter extensions:
Chevallier-Polarski-Linder (CPL) [$\sim 3.7\sigma$]
Jassal-Bagla-Padmanabhan (JBP) [$\sim 3.8\sigma$]

RS, A. Bhaumik, P. Mukherjee, S. Pal, JCAP 06 (2023): 038

Current status of H_0 tension with the models

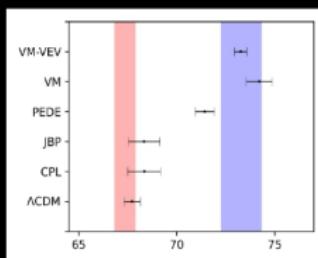
Reinvestigation done by

Shah, Bhaumik, Mukherjee, SP, JCAP:2023

Each model constrained* with current data without late-time measurement prior

Planck2018TTTEEE+lensing + Pantheon + BAO

[*PEDE & JBP not as successful for H_0 tension as previously claimed with a different dataset*]



With these constraints we simulate different possible future datasets
some

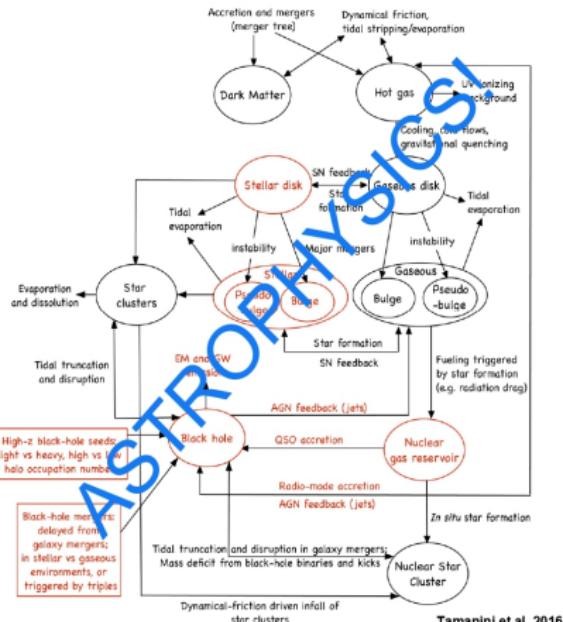
and move on to **forecasting**

* VM, VM-VEV constraints from Valentino et al. 2020

GW source population modelling

Source Population Modelling for MBHBs

- Pop III:** A light seed scenario where it is assumed that the first massive black holes grow from stellar remnants of early population III stars, which formed around $z \sim 15 - 20$ within massive dark matter halos. [~70 events/year]
- No Delay:** A heavy seed scenario in which protogalactic disk collapse (e.g., due to bar instabilities) leads to the formation of massive black holes. The MBHB coalescence events are assumed to take place simultaneously with the mergers of their host galaxies, which is a simplistic premise of this model. [~100 events/year]
- Delay:** A more realistic heavy seed scenario, in which there is a finite time delay between the merger of a given pair of host galaxies and that of the black holes. The intermediate period leading up to the MBHB merger is governed by a variety of complicated astrophysical processes which non-trivially affect the observable redshift distribution of the MBHB population. [~10 events/year]



Tamanini et al. 2016

Generate realistic mock catalogs

Instrumental Specifications

eLISA

$0.1 < z < 9.0$

$$\sigma_{\text{LISA}}^2 = \sigma_{\text{delens}}^2 + \sigma_v^2 + \sigma_{\text{inst}}^2 + \left(\frac{d}{dz}(d_L) \sigma_{\text{photo}} \right)^2$$

*for eLISA configuration L6A2M5N2

ET

$0.07 < z < 2.0$

$$\sigma_{\text{ET}}^2 = \sigma_{\text{inst}}^2 + \sigma_{\text{lens}}^2$$

Delensing error

Peculiar velocity error

Instrumental error

Photometric error

Ferreira et al. 2022

Fisher Matrix forecast analysis: eLISA

Λ CDM vs 5 (recent) parametrizations dedicated to H_0 tension

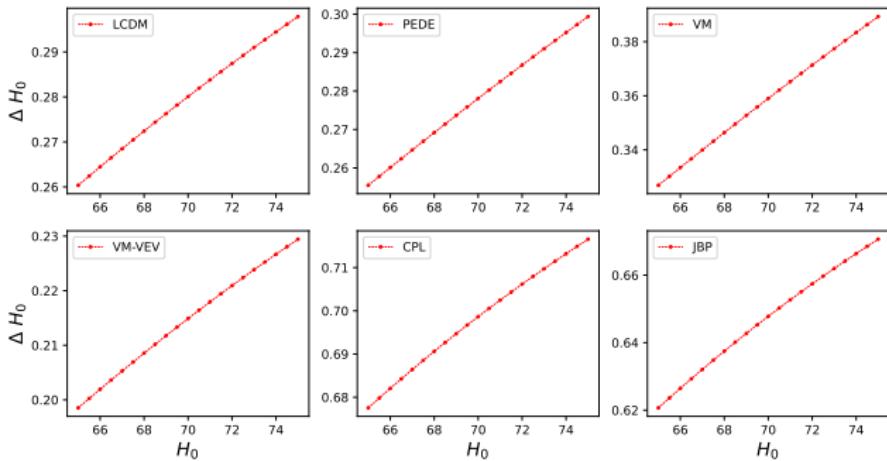


Figure: Dependence of errors estimated by Fisher analysis on the mean value of H_0 (km s⁻¹ Mpc⁻¹) for source type No Delay and eLISA mission duration of 10 years.

Parameter estimation using MCMC: eLISA

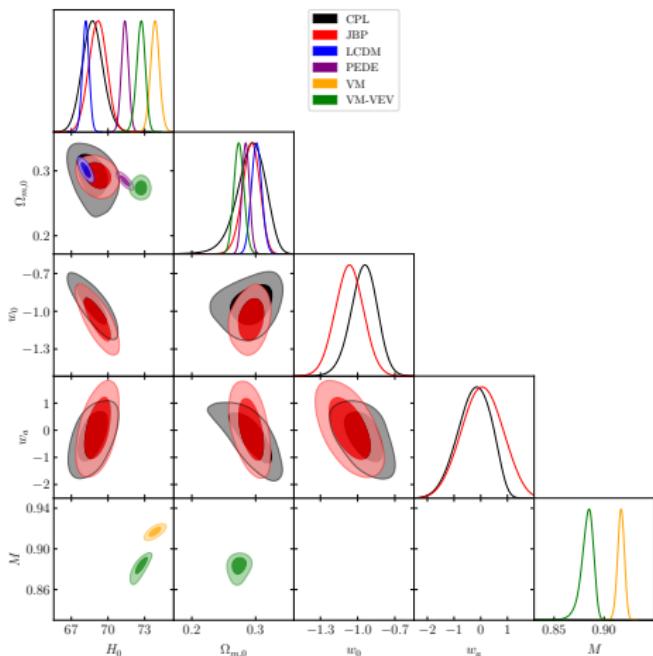
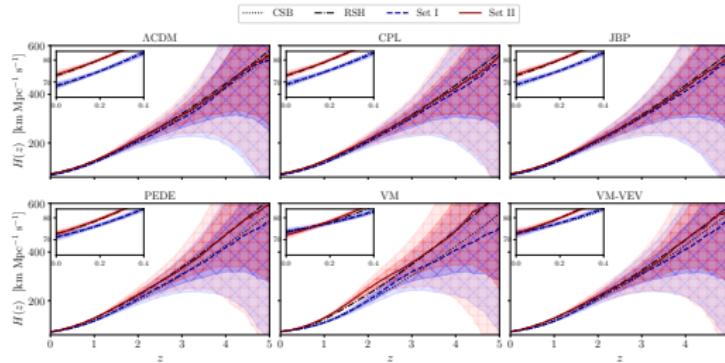


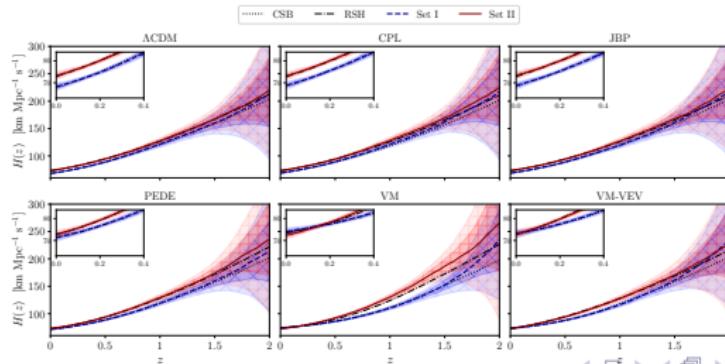
Figure: MCMC contours with No Delay source type for 10 years eLISA mission duration.

$H(z)$ reconstruction using Machine Learning (GP)

eLISA: \sim 10-year run for $0 < z < 5$



ET: \sim 3-year run for $0 < z < 2$



Performance summary: eLISA

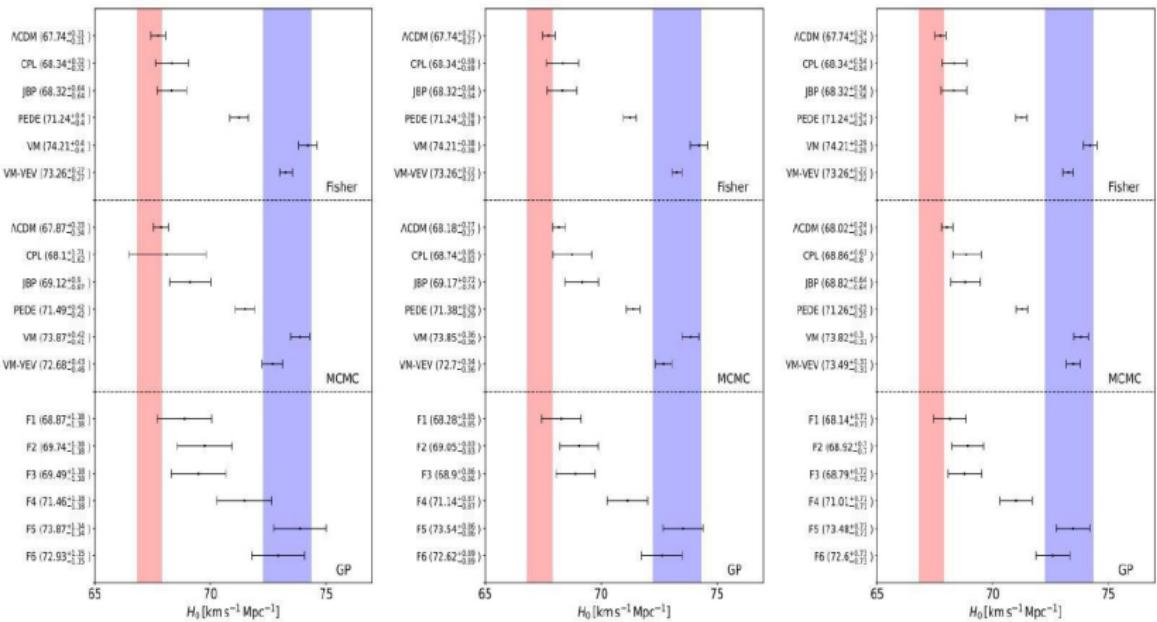
Shah, Bhaumik, Mukherjee, SP, JCAP:2023

Method	Λ CDM	CPL	JBP	PEDE	VM	VM-VEV
Current Datasets	4.98σ	3.69σ	3.78σ	1.79σ	0.74σ	0.04σ
Fisher Forecasting	5.20σ	4.15σ	4.11σ	1.91σ	0.84σ	0.04σ
GW MCMC	4.76σ	3.40σ	3.27σ	1.78σ	0.50σ	0.55σ
Gaussian Processes	3.74σ	3.19σ	3.27σ	1.59σ	0.18σ	0.49σ

GW missions have some prospects of relaxing the tension for a few parametrizations, do not worsen others...
...but the tension is far from being resolved

Performance summary: eLISA

So, what gives?



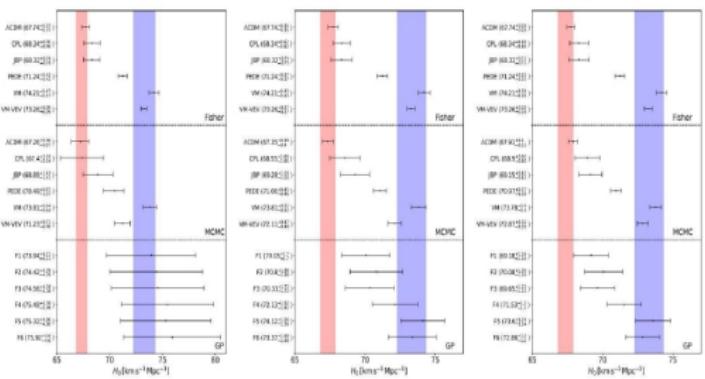
5 Years No Delay

10 Years No Delay

15 Years No Delay

Performance summary: eLISA

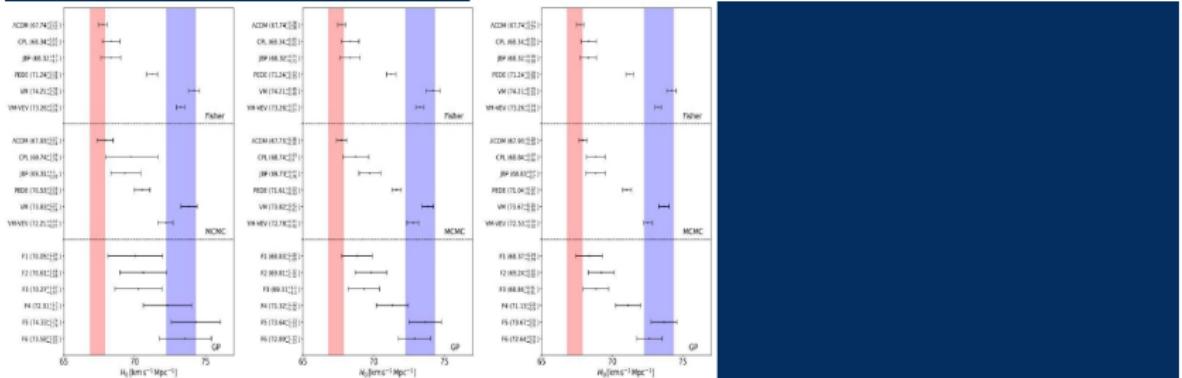
So, what gives?



5 Years Delay

10 Years Delay

15 Years Delay



5 Years Pop III

10 Years Pop III

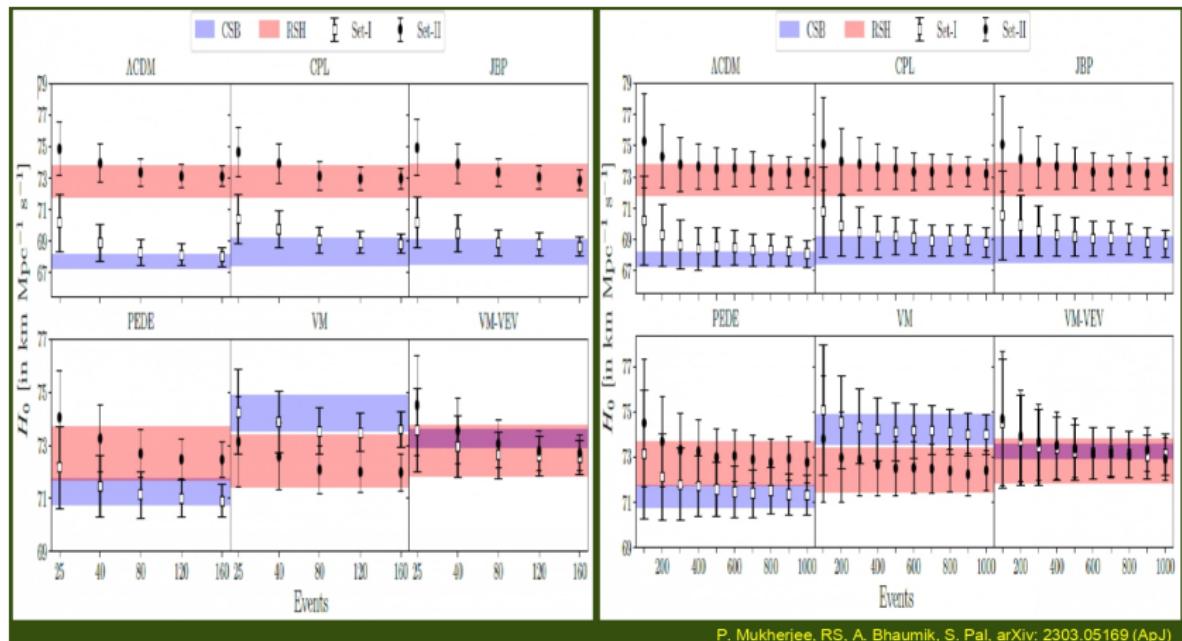
15 Years Pop III

RS, A. Bhaumik, P. Mukherjee, S. Pal, JCAP 06 (2023): 038

Performance summary: ET (GP only)

Mukherjee, Shah, Bhaumik, SP, ApJ:2024

Mock catalogs generated from CSB and RSH fiducials separately



P. Mukherjee, RS, A. Bhaumik, S. Pal, arXiv: 2303.05169 (ApJ)

Take-home message: GW

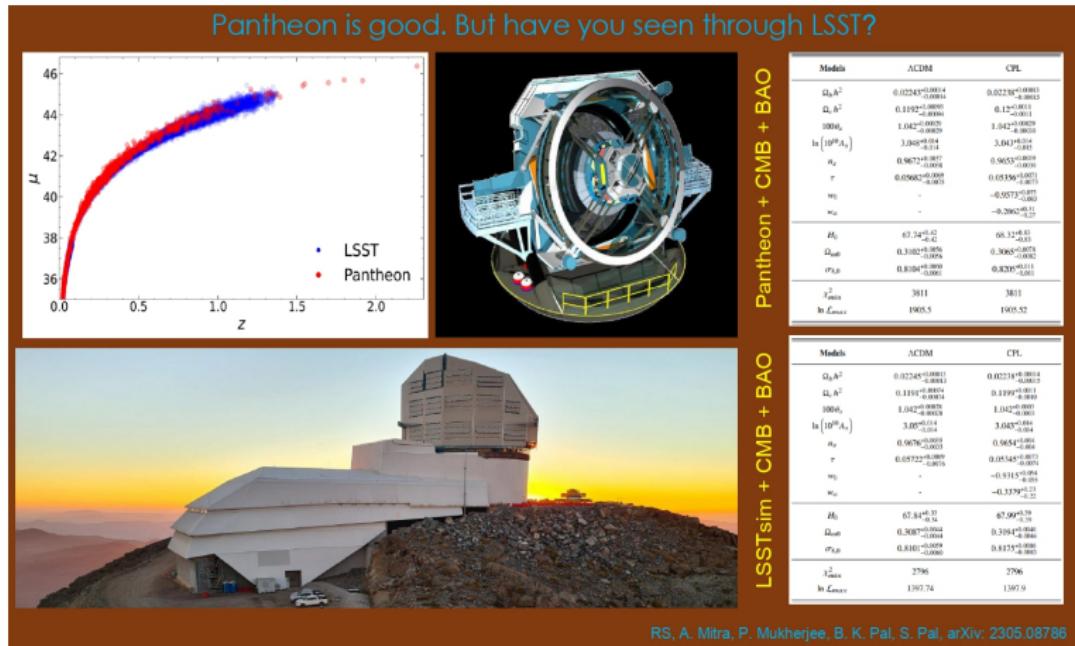
- GW missions have some prospects of relaxing the tension for a few parametrizations, do not worsen others
- Fisher shows eLISA to be more constraining than current data.
- MCMC shows marginally reduced tensions.
- GPs show H_0 value tending towards late-time value, without any such prior.
- But the tension is far from being resolved.

We urge the community to carry out forecasts using different methods so as to comparatively weigh and outweigh the pros and cons of each.

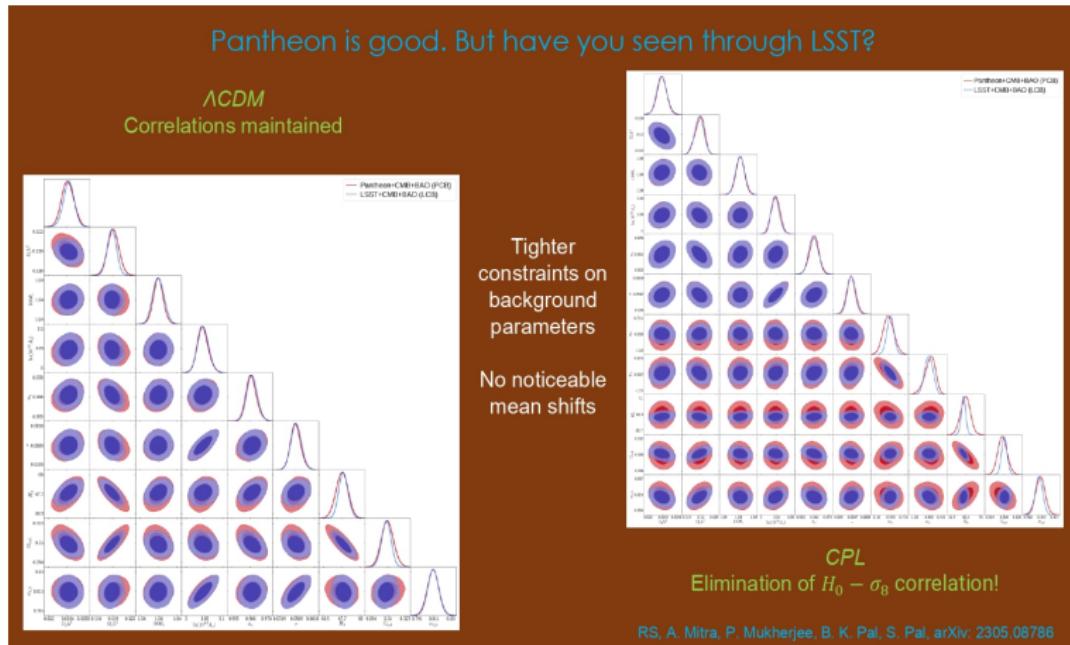
Future prospects: SNIa missions

Prospects of LSST Rubin Observatory

Shah, Mitra, Mukherjee, Pal, SP, arXiv:2305.08786

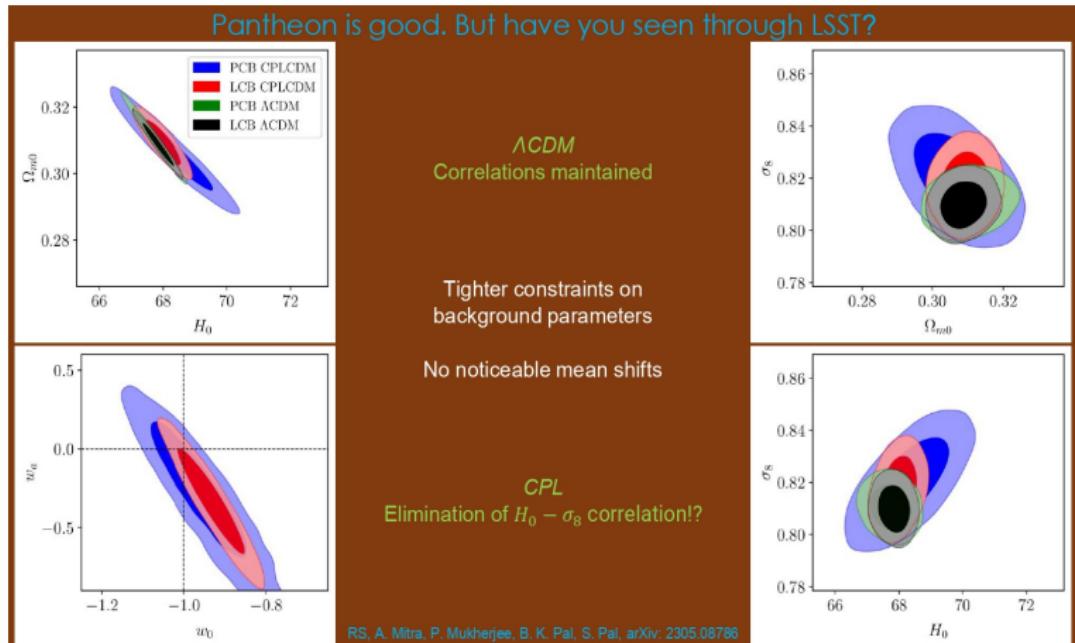


Pantheon vs LSST (+CMB+BAO)



Results with realistically generated mock catalog for LSST.
Other datasets real.

Pantheon vs LSST: any improvements?



Take-home message: SNIa

- Tighter constraints on background parameters, both for Λ CDM and CPL.
- No noticeable mean shift for H_0 .
- Tension is expected to persist with new SNIa data.
- For CPL: $H_0 - \sigma_8$ correlations is almost gone!
- Need to test with other models.

Can Cosmic Distance Ladder be reconstructed?

LADDER: a deep learning algorithm

Shah, Saha, Mukherjee, Garain, SP, arXiv:2401.17029

- Training ANN algorithm: Long-Short Term Memory (LSTM)
- Training dataset used: Pantheon
- Application of trained dataset so far: Pantheon+, BAO, GRB

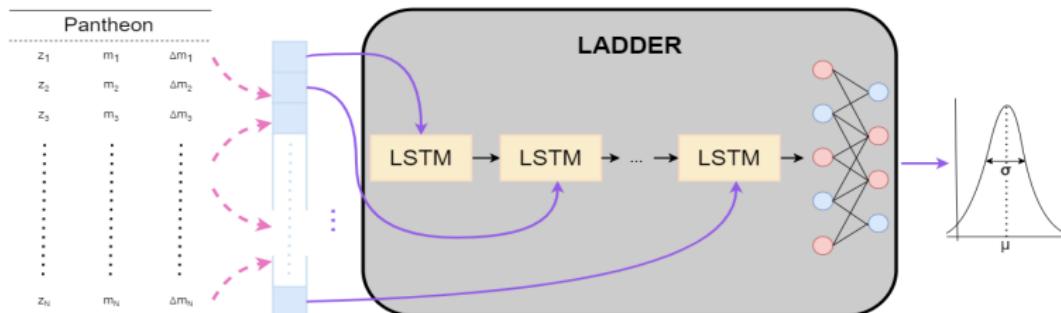
Can Cosmic Distance Ladder be reconstructed?

LADDER: a deep learning algorithm

Shah, Saha, Mukherjee, Garain, SP, arXiv:2401.17029

- Training ANN algorithm: Long-Short Term Memory (LSTM)
- Training dataset used: Pantheon
- Application of trained dataset so far: Pantheon+, BAO, GRB

Schematic diagram of LADDER algorithm



LADDER reconstruction of Pantheon+

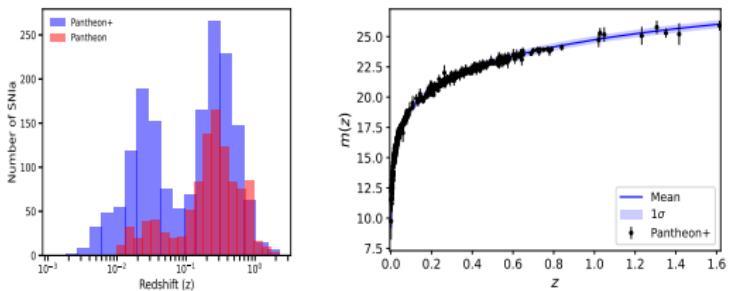


Figure: Redshift distribution (left); Pantheon+ vs reconstructed (right)

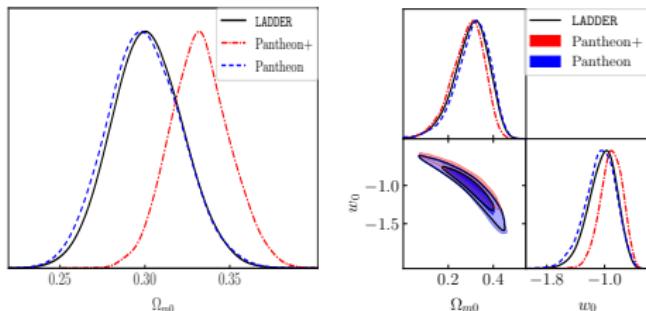


Figure: Cosmological parameters: Λ CDM (left); w CDM (right)

LADDER calibration of BAO (vs CMB Λ CDM-calibration)

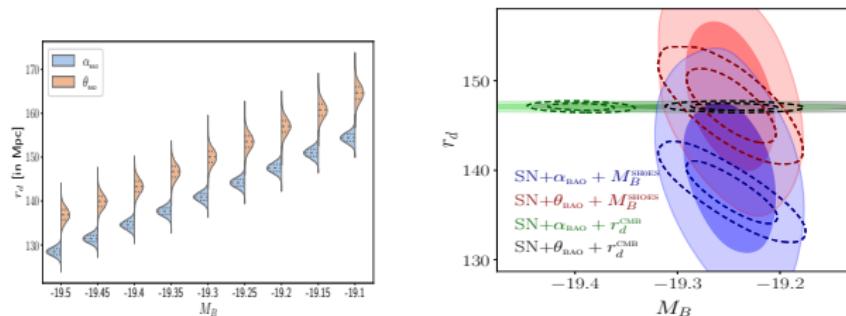


Figure: Angular vs Anisotropic BAO (left); LADDER mean + 1σ uncertainty predictions (right). Colored contours : LADDER predictions, dashed ones : CMB- Λ CDM calibration

Discrepancy between Angular vs Anisotropic BAO gone?

LADDER calibration of high-z (GRB) data

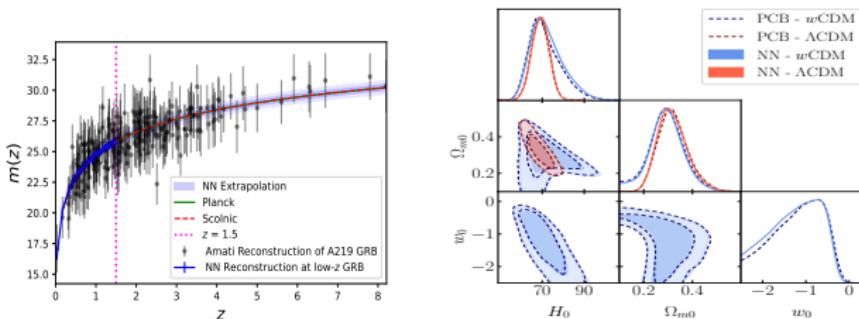


Figure: LADDER calibrated GRB vs other methods (left); Constraints on parameters (CC Hubble + calibrated high-z GRB)

LADDER calibration of high-z (GRB) data

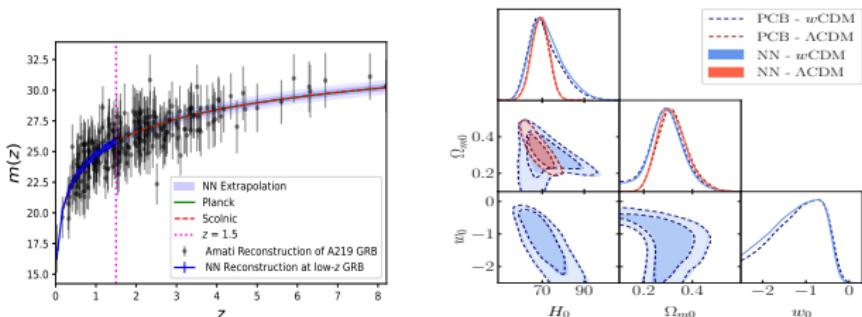


Figure: LADDER calibrated GRB vs other methods (left); Constraints on parameters (CC Hubble + calibrated high-z GRB)

Model	Λ CDM		wCDM		
	Calibrator	LADDER	PCB	LADDER	PCB
H_0		$69.203^{+4.050}_{-4.150}$	$68.996^{+4.187}_{-4.095}$	$71.224^{+9.058}_{-6.365}$	$70.265^{+8.989}_{-5.915}$
Ω_{m0}		$0.313^{+0.066}_{-0.055}$	$0.317^{+0.067}_{-0.057}$	$0.289^{+0.068}_{-0.074}$	$0.287^{+0.072}_{-0.085}$
w_0		$-1.257^{+0.627}_{-0.867}$	$-1.172^{+0.599}_{-0.866}$

Show improvements in mean of H_0 . How seriously one should take GRB?



Take-home message: Distance Ladder reconstruction

- Some interesting results but need to be verified with other datasets/ combinations.
- Whether it really helps in addressing Hubble tension is yet to be confirmed.
- Can act as a mock data generator (say for GW).
- Major challenge: derivative estimation in d_L' .

Conclusions

COSMOLOGY MARCHES ON



The point is not to pocket the truth but to chase it