Leptogenesis and dark matter in the presence of primordial black holes

based on JCAP 11 (2021) 019 (arXiv 2104.14496), with D. Borah, D. Mahanta, and arXiv 2111.08034, with B. Barman, D. Borah, R. Roshan. Weekly meeting on Cosmology, IIT Madras.

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- Introduction and Motivation.
- Primordial Black Holes.
- The Scotogenic model.
- Leptogenesis and DM from PBH.
- Asymmetric DM from PBH.
- Conclusion.

Matter - Antimatter Asymmetry.



Baryon Asymmetry (from BBN and CMB) : $\eta_B = \frac{n_B - n_{\bar{B}}}{n_{\gamma}} \approx 6.1 \times 10^{-10}$.

¹ Credit : Alan Stonebraker	<□> < □ > < □ > <	ヨト ・ヨト	ą.	900
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Conditions for Baryogenesis (Sakharov 1967) :
a) Baryon No. Violation (X → Y + B).
b) C and CP violation : Γ(X → Y + B) ≠ Γ(X̄ → Ȳ + B̄) and Γ(X → q_Lq_L) + Γ(X → q_Rq_R) ≠ Γ(X̄ → q̄_Lq̄_L) + Γ(X̄ → q̄_Rq̄_R).
c) Departure from thermal equilibrium : Γ(X → Y + B) ≠ Γ(Y + B → X).

The SM of Particle Physics fails to provide these.

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Baryogenesis through Leptogenesis : $Y_{ii}\overline{L}_i\overline{H}N_i + M_{ii}N_iN_i$ Asymmetry ($n_{\Delta L}$) created in lepton sector (around $T \sim M_N$). B + L violating sphaleron processes (Khlebnikov & Shaposhnikov'88) Baryon Asymmetry ($\frac{n_{\Delta B}}{\epsilon} \approx -\frac{28}{79} \frac{n_{\Delta L}}{\epsilon}$). ^aCredit : 1301.3062[hep-ph]

Bonus : Closely connected to neutrino mass through seesaw mechanisms [R.N. Mohapatra et al. 1980].

Dark Matter.

A plethora of evidences...



 $\Omega_{DM}h^2 = 0.12 \pm 0.01$ (Planck 2018)

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The SM of Particle Physics fails to explain... Some BSM particle ?

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Cosmic History prior to BBN ?

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A Universe dominated by Primordial Black Holes (PBH)....(Hawking 1975)

(from a few grams to some solar masses).

Formation (B. Carr et al. 2002.12778) :

- Collapse of large inhomogeneities.
- Bubble collisions.
- Collapse of cosmic string loops.

Primordial Black Holes .

• PBH formed in the very early universe,

$$M_{
m BH}(T_{
m in})pprox rac{4\pi}{3}rac{
ho_{
m Rad}(T_{
m in})}{H^3(T_{
m in})}.$$

Lower bound : $H_I \leq 2.5 imes 10^{-5} M_{
m Pl} \implies M_{
m in} \gtrsim 0.1 \ g$

• Black hole temperature :

$$T_{\rm BH} = rac{1}{8\pi\,GM_{
m BH}} pprox 1.06 \; \left(rac{10^{13}~{
m g}}{M_{
m BH}}
ight) \; {
m GeV}.$$

Initial PBH fraction :

$$eta = rac{
ho_{
m BH}(T_{
m in})}{
ho_{
m Rad}(T_{
m in})}.$$

• Hawking evaporation :

$$\frac{dM_{BH}}{dt} = -\sum_{a} \frac{g_{a}}{2\pi^{2}} \int_{0}^{\infty} \frac{\sigma_{abs}^{s_{a}}(M_{BH}, p) p^{3} dp}{\exp[E_{a}(p)/T_{BH}] - (-1)^{2s_{a}}}$$
$$\approx -5.34 \times 10^{25} \varepsilon(M_{BH}) \left(\frac{1 \text{ g}}{M_{BH}}\right)^{2} gs^{-1}. \quad J.MacGibbon, 1991.$$

$$T_{\rm ev} \approx \left(\frac{9g_*(T_{\rm BH})}{10240} \right)^{rac{1}{4}} \left(\frac{M_{\rm Pl}^5}{M_{
m in}^3} \right)^{rac{1}{2}}.$$

- $M_{in}\gtrsim 10^{15}g$ can be a DM candidate.
- $M_{in} \lesssim 10^{15} g$ can lead to DM-genesis, matter-antimatter asymmetry.

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Upper bound : $M_{\rm in} \lesssim 2 \times 10^8 {\rm ~g}$ (BBN) $M_{\rm in} \lesssim 2 \times 10^5 {\rm ~g}$ (Sphaleron).

Baryon Asymmetry from PBH (Hawking 1974, Carr 1976).

• PBH evaporate to RHNs which are heavy enough (Fujita et al. 1401.1909) :

$$(\mathsf{PBH}) \xrightarrow[\times N_{\nu}]{\text{evaporation}} \begin{pmatrix} \mathsf{right handed} \\ \mathsf{neutrino} \end{pmatrix} \xrightarrow[\times \epsilon]{\frac{\mathsf{decay}}{\times \epsilon}} \begin{pmatrix} \mathsf{lepton} \\ \mathsf{number} \end{pmatrix} \xrightarrow[\times \kappa]{\frac{\mathsf{sphaleron}}{\times \kappa}} \begin{pmatrix} \mathsf{baryon} \\ \mathsf{number} \end{pmatrix}.$$

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- We consider a low scale leptogenesis setup.
- Both thermal and non-thermal contribution important.
- PBH may evaporate before, during or after the scale of leptogenesis (Y.F. Perez et al. 2010.03565).
- Initial PBH abundance (β) high enough, giving maximal contribution to leptogenesis and DM.

The Particle Physics Setup [Scotogenic Model, E.Ma 2006].

BSM Particles	$SU(2)_L$	Z_2
$N_i(i = 1, 2, 3)$	0	—
$\eta = (\eta^{\pm} H^0 + i A^0 / \sqrt{2})$	1	_

$$\begin{split} \mathcal{L} &\supset \; \frac{1}{2} (M_N)_{ij} N_i N_j + \left(Y_{ij} \, \bar{L}_i \tilde{\eta} N_j + \text{h.c.} \right) \\ \mathcal{V}(\Phi_1, \eta) \; = \; \mu_1^2 |\Phi_1|^2 + \mu_2^2 |\eta|^2 + \frac{\lambda_1}{2} |\Phi_1|^4 + \frac{\lambda_2}{2} |\eta|^4 + \lambda_3 |\Phi_1|^2 |\eta|^2 \\ &+ \lambda_4 |\Phi_1^{\dagger} \eta|^2 + \left[\frac{\lambda_5}{2} (\Phi_1^{\dagger} \eta)^2 + \text{h.c.} \right]. \end{split}$$

• Light neutrino mass at loop-level :

$$(m_{\nu})_{ij} = \sum_{k} \frac{Y_{ik} Y_{jk} M_{k}}{32\pi^{2}} \left[L_{k}(m_{H^{0}}^{2}) - L_{k}(m_{A^{0}}^{2}) \right]$$

$$L_k(m^2) = \frac{m^2}{m^2 - M_k^2} \ln \frac{m^2}{M_k^2}.$$

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The Scotogenic model

• CP asymmetry :





Boltzmann equations :

$$\begin{split} \frac{d\varrho_{\rm BH}}{da} &= \frac{1}{M_{\rm BH}} \frac{dM_{\rm BH}}{da} \varrho_{\rm BH}, \\ \frac{d\varrho_{\rm Rad}}{da} &= -\frac{\epsilon_{\rm SM}(M_{\rm BH})}{\epsilon(M_{\rm BH})} \frac{1}{M_{\rm BH}} \frac{dM_{\rm BH}}{da} a_{\varrho_{\rm BH}}, \\ aH \frac{dn_{N_1}^T}{da} &= -\left(n_{N_1}^T - n_{N_1}^{\rm eq}\right) \Gamma_1^T, \\ aH \frac{dn_{N_1}^{\rm BH}}{da} &= -\left(n_{N_1}^{\rm BH} - n_{N_1}^{\rm eq}\right) \Gamma_1^T + n_{\rm BH} \Gamma_{\rm BH \to N_1}, \\ aH \frac{dn_{B-L}}{da} &= \epsilon_1 \left[\left(n_{N_1}^T - n_{N_1}^{\rm eq}\right) \Gamma_1^T + n_{N_1}^{\rm BH} \Gamma_1^{\rm BH} \right] - (W_{ID} + \Delta W_{scattering}) n_{B-L}, \\ \frac{dT}{da} &= -T \left(\frac{1}{a} + \frac{\epsilon_{SM}(M_{\rm BH})}{\epsilon(M_{\rm BH})} \frac{1}{M} \frac{dM_{BH}}{da} \frac{a\varrho_{\rm BH}}{4\varrho_{\rm Rad}} \right). \end{split}$$



PBH evaporate before leptogenesis scale :



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PBH mass vs BAU :

PBH mass vs Leptogenesis Scale :



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Dark Matter in the presence of PBH

• Case I : DM candidate \rightarrow Lightest scalar of inert doublet.

In the presence of PBH (N. Bernal et al. 2011.12306) :

- **1** $T_{fo} > T_{eq}$: Usual WIMP DM in a RD universe, with PBH dilution.
- 2 $T_c < T_{fo} < T_{eq}$: PBH dominate (for $\beta > \beta_c$), $\rho_{Rad} \propto a^{-4}$.

$$I_{ev} < T_{fo} < T_c : \rho_{Rad} \propto a^{-3/2}$$

 $T_{fo} < T_{ev} : \text{RD universe again, no PBH dilution.}$



 $\Omega_{\text{DM}}^{\text{total}} h^2 = \Omega_{\text{DM}}^{\text{BH}} h^2 + \Omega_{\text{DM}}^{\text{fo}} h^2$ (P. Gondolo et al. 2009.02424).

 $T_{fo} > T_{ev} \implies M_{DM} > 3 MeV (trivially satisfied).$

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Dark Matter in the presence of PBH

DM from PBH (P. Gondolo et al. 2009.02424) :

$$\begin{split} N_{\rm DM} &= \frac{15\zeta(3)}{\pi^4} \frac{1}{g_*(T_{\rm BH})} \times \begin{cases} (\frac{M_{\rm in}}{M_{\rm Pl}})^2 & \text{for } M_{\rm DM} \leq T_{\rm BH}^{\rm in}, \\ (\frac{M_{\rm Pl}}{M_{\rm DM}})^2 & \text{for } M_{\rm DM} \geq T_{\rm BH}^{\rm in}. \end{cases} \\ Y_{\rm DM} &= \frac{n_{\rm DM}(T_0)}{s(T_0)} \simeq \frac{3}{4} N_{\rm DM} \times \begin{cases} \beta \frac{T_{\rm in}}{M_{\rm in}} & \text{for RD}, \ \beta \leq \beta_c, \\ \frac{\bar{T}_{\rm ev}}{M_{\rm in}} & \text{for MD}, \ \beta \geq \beta_c. \end{cases} \end{split}$$

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Case $I : N_1$ Leptogenesis and scalar DM.



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- $M_{DM} \gtrsim 4 \ GeV$ gets overproduced from PBH with large β .
- Light scalar DM ruled out from direct search constraints.

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Case II : N_2 Leptogenesis and fermion DM.

- N₁ : Light, singlet DM candidate.
- Thermal DM difficult to realize (Lee and Weinberg 1977), FIMP : $IW^{\pm}(Z) \longrightarrow N_1\eta, \ I\eta \longrightarrow W^{\pm}(Z)N_1, \ \eta \rightarrow N_1I.$
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Contours for observed BAU and DM abundance :



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Contours for observed BAU and DM abundance :



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Parameter space with and without PBH :



PBH evaporate before DM freezeout :



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- Coincidence Problem : $\Omega_{DM} \approx 5\Omega_{Baryon}$.
- A common origin of dark and visible sector ?

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Baryonic matter Abundance.

- Matter-antimatter pair annihilates, asymmetric part $(n_B - n_{\overline{B}})$ remains.
- Not thermal (freezeout) production.

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Same out-of-equilibrium decay of a heavier particle generates $n_B - n_{\overline{B}} \sim n_{DM} - n_{\overline{DM}}$.

Asymmetric Dark Matter from PBH



$$-\mathcal{L} \supset \frac{1}{2} M_N \,\overline{N^c} N + y_N \,\overline{N} \, \widetilde{H}^{\dagger} \, \ell \, + \, m_\chi \,\overline{\chi} \, \chi + y_\chi \,\overline{N} \, \mathcal{S} \, \chi \, + \, \mathrm{h.c.} \, .$$



$$\begin{split} \epsilon_{\Delta L} &= \frac{\sum_{\alpha} [\Gamma(N_1 \rightarrow I_{\alpha} + H) - \Gamma(N_1 \rightarrow \overline{I_{\alpha}} + H^*)]}{\Gamma_1} \\ &\simeq \frac{M_1}{8 \pi} \frac{\mathrm{Im}[(3 \, y_N^* \, y_N^T + y_\chi^* \, y_\chi^T) \, M^{-1} y_N \, y_N^\dagger]_{11}}{[2 \, y_N \, y_N^\dagger + y_\chi \, y_\chi^\dagger]_{11}} \,, \end{split}$$

$$\epsilon_{\Delta\chi} = \frac{\Gamma(N_1 \to \chi + S) - \Gamma(N_1 \to \bar{\chi} + S^*)}{\Gamma_1}$$
$$\simeq \frac{M_1}{8\pi} \frac{\operatorname{Im}[(y_N^* y_N^T + y_\chi^* y_\chi^T) M^{-1} y_\chi y_\chi^\dagger]_{11}}{[2 y_N y_N^\dagger + y_\chi y_\chi^\dagger]_{11}}$$

$$\epsilon_{\Delta L} \lesssim rac{3}{16 \, \pi} \, rac{M_1 \, m_{
u, ext{max}}}{v^2}$$
 (Davidson – Ibbara bound).

• Baryon Number Yield : $\frac{n_B}{s}(T_0) = \mathcal{N} \epsilon_{\Delta L} a_{\text{sph}} \frac{n_{\text{PBH}}}{s} \Big|_{T_{\text{evap}}}.$

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Baryon Asymmetry from PBH



Dark Matter from PBH.

• Asymmetric DM Yield : $Y_{\text{DM}}(T_0) = \epsilon_{\Delta\chi} \mathcal{N} \frac{n_{\text{PBH}}}{s}(T_{\text{evap}})$.

$$\Omega_{\rm DM} h^2 = \frac{g_{\rm DM}}{g_{\star} \left(T_{\rm evap}\right)} \frac{m_{\rm DM} s_0}{\rho_c} \epsilon_{\Delta \chi} \frac{n_{\rm PBH}}{s} \Big|_{T_{\rm evap}} \begin{cases} \frac{4 \pi}{3} \left(m_{\rm in}/M_{\rm pl}\right)^2 & \text{for } T_{\rm BH}^{\rm in} > M_1 ; \\ \\ \frac{1}{48 \pi} \left(M_{\rm pl}/M_1\right)^2 & \text{for } T_{\rm BH}^{\rm in} < M_1 . \end{cases}$$



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Boltzmann equations for asymmetry : $a\mathcal{H}\frac{d\widetilde{N}_{B-L}}{d\xi} = \epsilon_{\Delta L} \left[\left(\widetilde{n}_{N_{1}}^{T} - \widetilde{n}_{N_{1}}^{eq} \right) \Gamma_{N_{1}}^{T} + \widetilde{n}_{N_{1}}^{BH} \Gamma_{N_{1}}^{BH} \right] - Br_{SM} \mathcal{W} \widetilde{N}_{B-L},$ $a\mathcal{H}\frac{dX}{d\xi} = \epsilon_{\Delta \chi} \left[\left(\widetilde{n}_{N_{1}}^{T} - \widetilde{n}_{N_{1}}^{eq} \right) \Gamma_{N_{1}}^{T} + \widetilde{n}_{N_{1}}^{BH} \Gamma_{N_{1}}^{BH} \right] - Br_{DM} \mathcal{W} X.$



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$$m_{\chi}: \{1-10^5\}$$
 GeV; $m_{\text{BH}}: \{1-12\}$ g; $y_{\chi}: \{10^{-4}-10^{-1}\}$.



- We have studied leptogenesis and DM in a common setup (Scotogenic Model), in the presence of PBH.
- PBH lead to non-thermal source of leptogenesis as well as dilution of asymmetry.
- For *N*₁ leptogenesis and scalar DM, no region of PBH parameters can simultaneously affect both.
- N₂ leptogenesis and fermion DM : cogenesis possible with PBH dependency.
- Light DM constrained from mixed DM astrophysical bounds.
- Observational consequences like gravitational waves in future experiments.

- Studied Asymmetric Dark matter, motivated from baryon-DM coincidence problem.
- Considered a non-thermal origin of these asymmetries from PBH.
- We stick to ultralight PBH (\sim 1 g 10 g) and high M_1 mass.
- Non-thermal RHNs dominate over thermal in generating the asymmetry.
- Asymmetry generated simultaneously in visible and dark sector with different DM masses.
- Origin, mass distribution, spin of PBH.... ?

Thanks for Listening

Questions/ Comments ?

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• CP asymmetry functions :

$$\begin{split} F(r_{ji},\eta_i) &= \sqrt{r_{ji}} \left[f(r_{ji},\eta_i) - \frac{\sqrt{r_{ji}}}{r_{ji}-1} (1-\eta_i)^2 \right], \\ f(r_{ji},\eta_i) &= \sqrt{r_{ji}} \left[1 + \frac{(1-2\eta_i+r_{ji})}{(1-\eta_i^2)^2} \ln(\frac{r_{ji}-\eta_i^2}{1-2\eta_i+r_{ji}}) \right]. \end{split}$$

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• Washout parameters :

$$W_{\rm ID} = rac{1}{4} \Gamma_{N_1}^T K_2(z) z^2,$$

 $\Delta W = rac{36\sqrt{5} M_P M_1 m_{\xi}^2 H}{2\sqrt{\pi} \sqrt{g_*} v^4 z \lambda_5^2}.$

• Boltzmann equations (WIMP) :

$$k\frac{d Y_{\rm DM}}{dz} = -\frac{\langle \sigma v \rangle s}{Hz} \left(Y_{\rm DM}^2 - Y_{\rm eq}^2\right).$$

• Boltzmann equations (FIMP) :

$$\begin{split} \frac{dY_{\eta}}{dz} &= -\frac{4\pi^2}{45} \frac{M_{\rm Pl} m_{\eta}}{1.66} \frac{\sqrt{g_*(z)}}{z^2} \bigg[\sum_{p \equiv \rm SM \ particles} \langle \sigma v \rangle_{\eta\eta \to \rho\rho} \bigg(Y_{\eta}^2 - (Y_{\eta}^{\rm eq})^2 \bigg) \bigg] \\ &- \frac{M_{\rm Pl}}{1.66} \frac{z}{m_{\eta}^2} \frac{\sqrt{g_*(z)}}{g_s(z)} \Gamma_{\eta \to N_1 l} Y_{\eta} \\ \frac{dY_{N_1}}{dz} &= \frac{M_{\rm Pl}}{1.66} \frac{z}{m_{\eta}^2} \frac{\sqrt{g_*(z)}}{g_s(z)} \Gamma_{\eta \to N_1 l} Y_{\eta} \\ &+ \frac{4\pi^2}{45} \frac{M_{\rm Pl} M_{\eta}}{1.66} \frac{\sqrt{g_*(z)}}{z^2} \times \bigg(\sum_{x = W^{\pm}, Z, \eta} \langle \sigma v_{lx \to N_1 x} \rangle \left(Y_x^{eq} Y_l^{eq} - Y_{N_1} Y_x \right) \bigg) \end{split}$$





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