

Observation and astrophysics of gravitational waves: Current status and future prospects

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Based on LVK's population paper, [arXiv:2111.03634](https://arxiv.org/abs/2111.03634)

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on Gravitation and Cosmology



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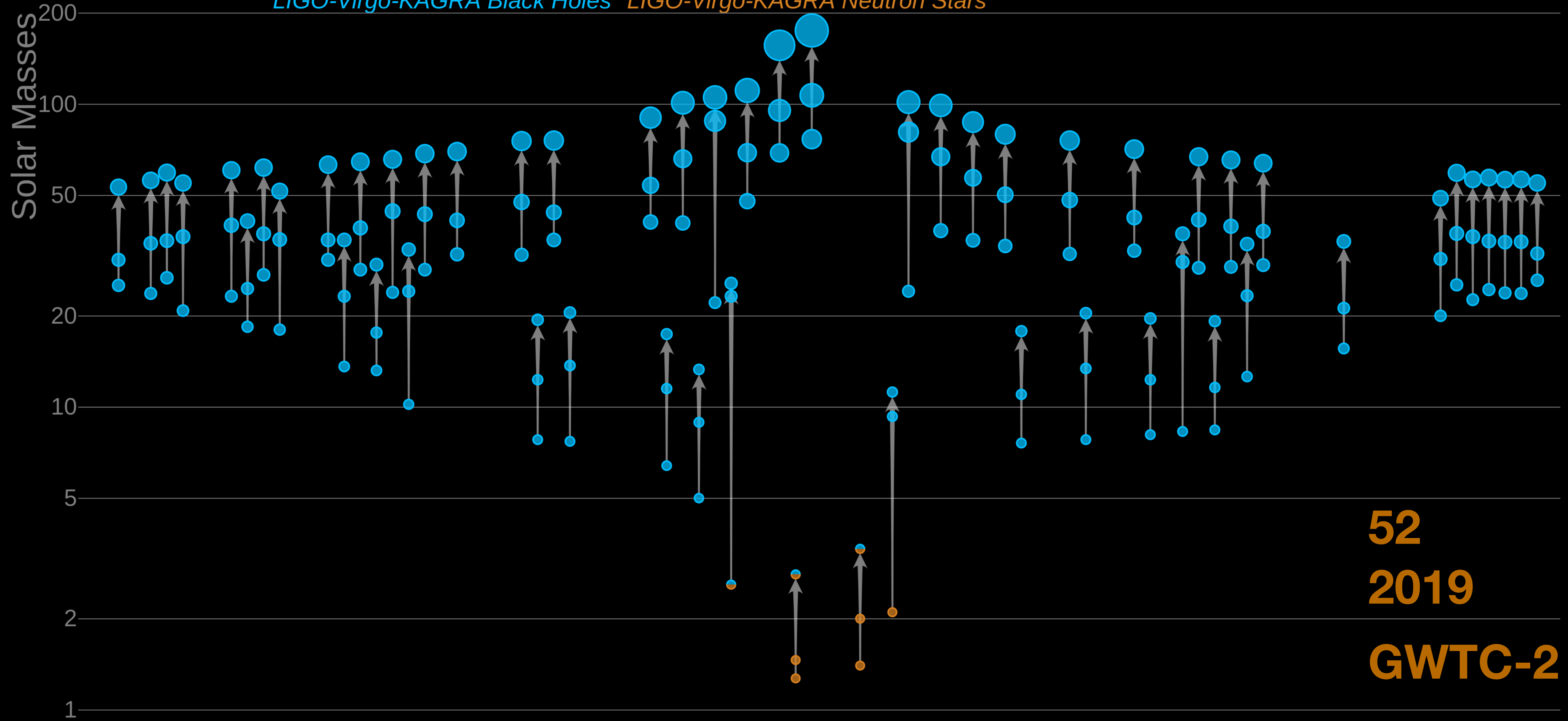
Masses in the Stellar Graveyard

LIGO-Virgo-KAGRA Black Holes LIGO-Virgo-KAGRA Neutron Stars



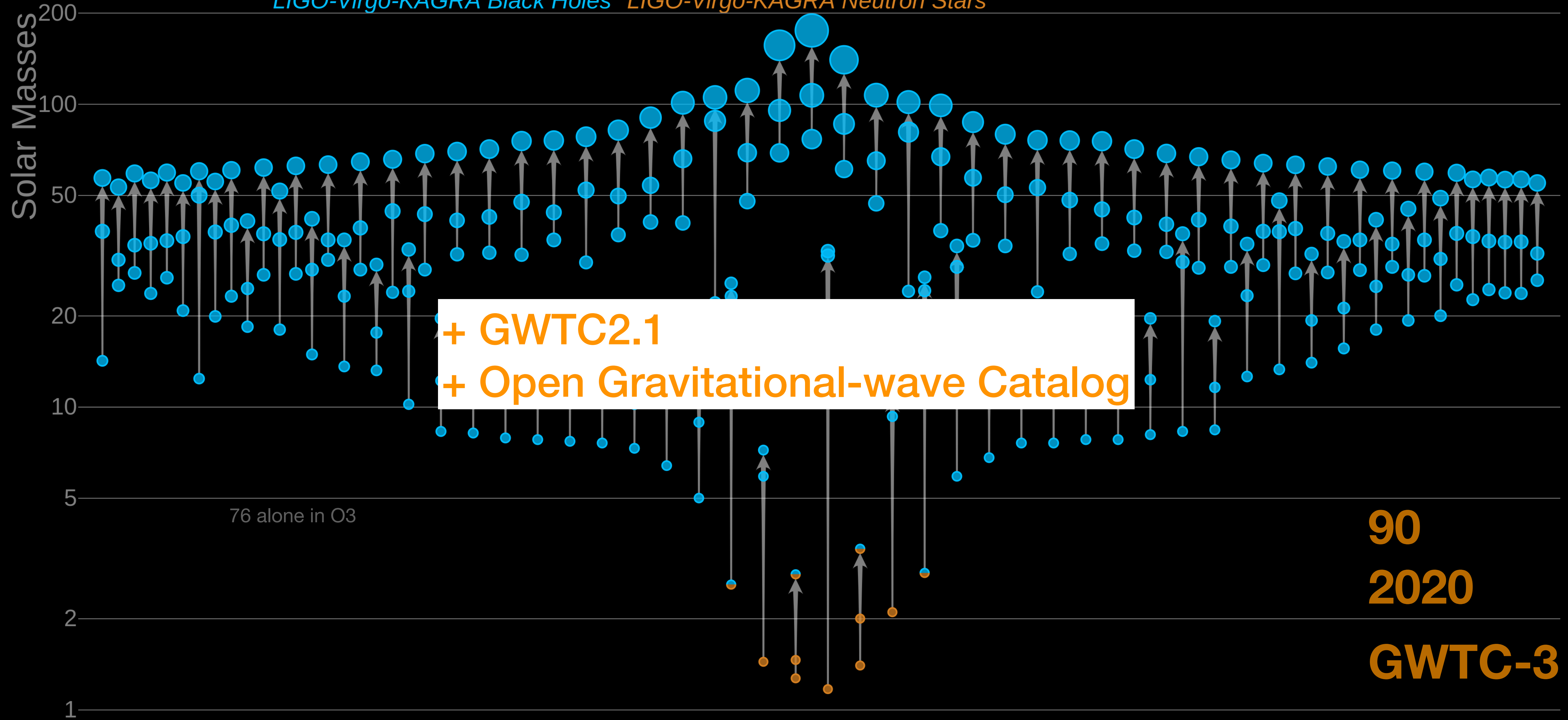
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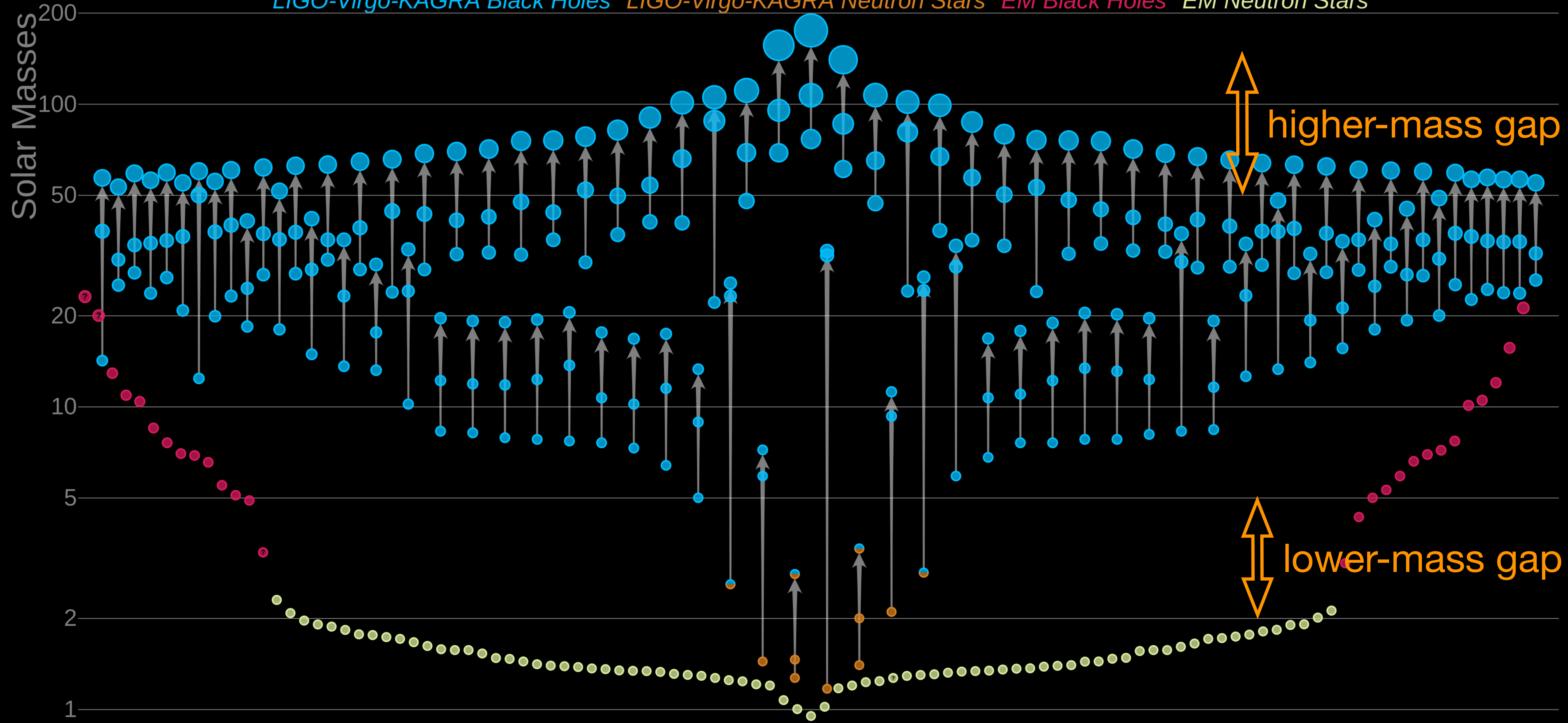
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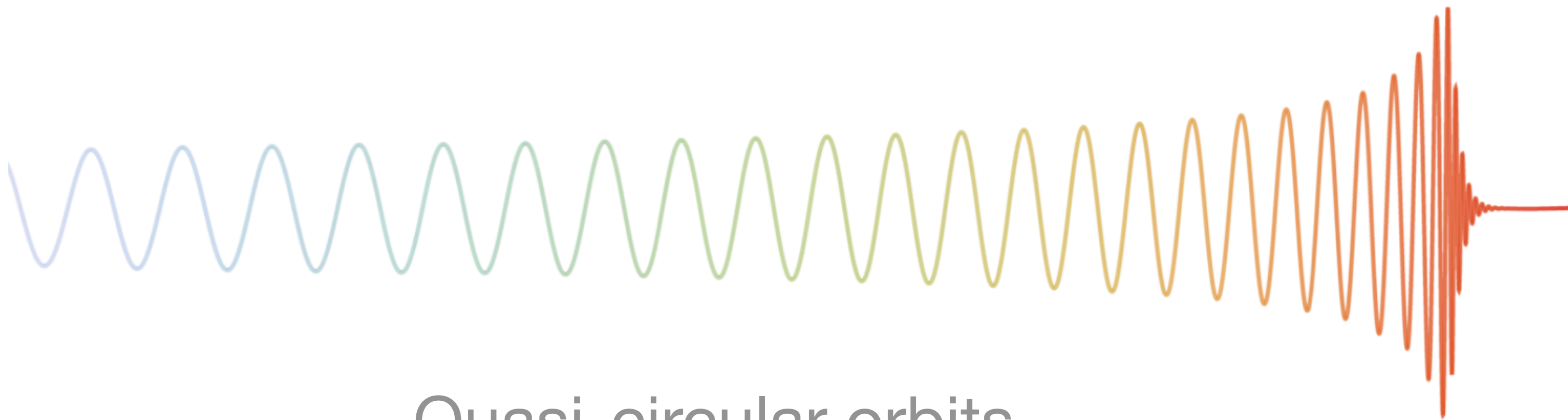
Masses in the Stellar Graveyard

LIGO-Virgo-KAGRA Black Holes *LIGO-Virgo-KAGRA Neutron Stars* *EM Black Holes* *EM Neutron Stars*

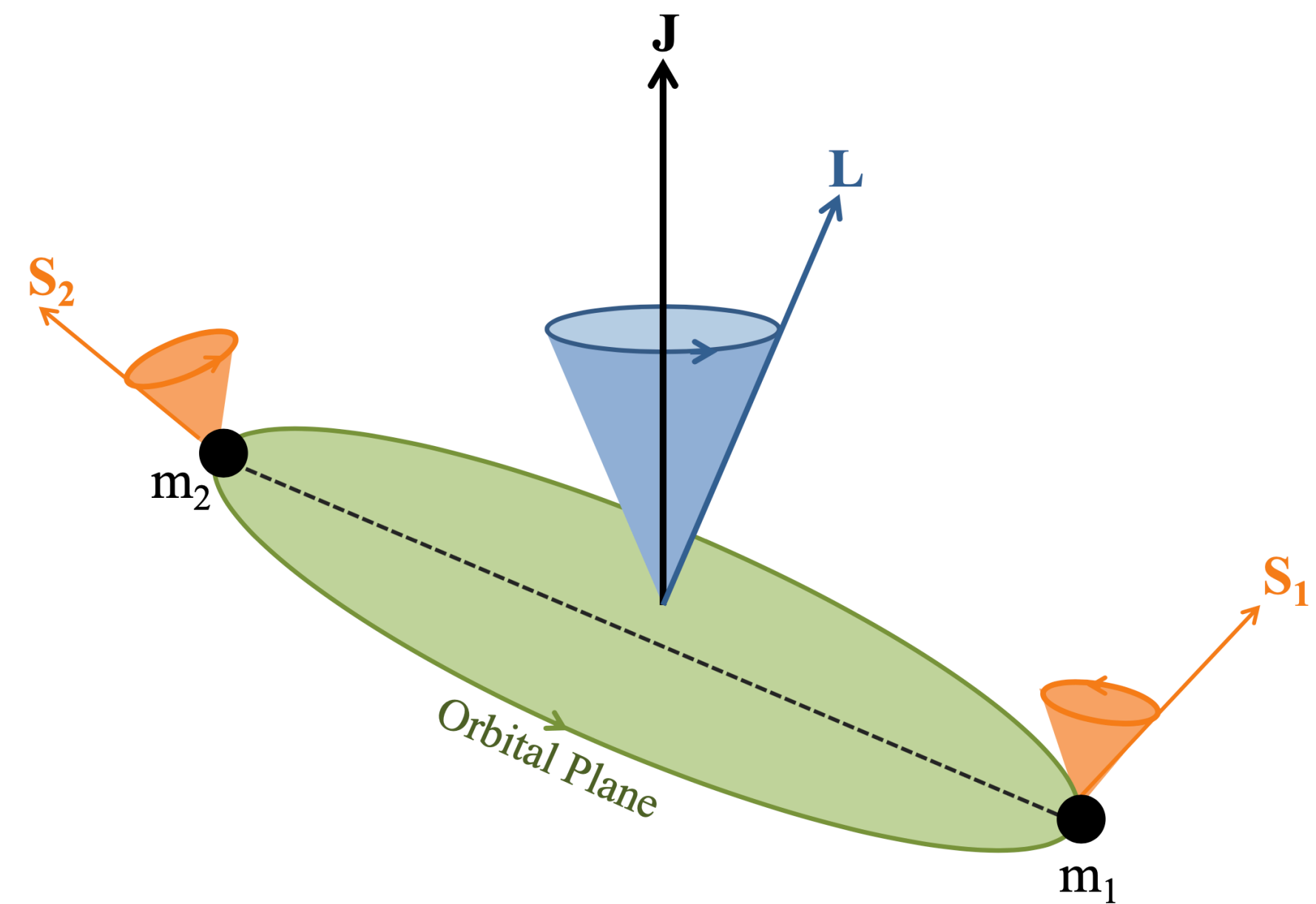


Questions:

- How these binary mergers form?
- What are the astrophysical environments in which these mergers take place?
- Is there a lower mass gap?
- Is there a higher mass gap?
- What is the rate of star formation throughout the Universe?
- New observations, new questions!

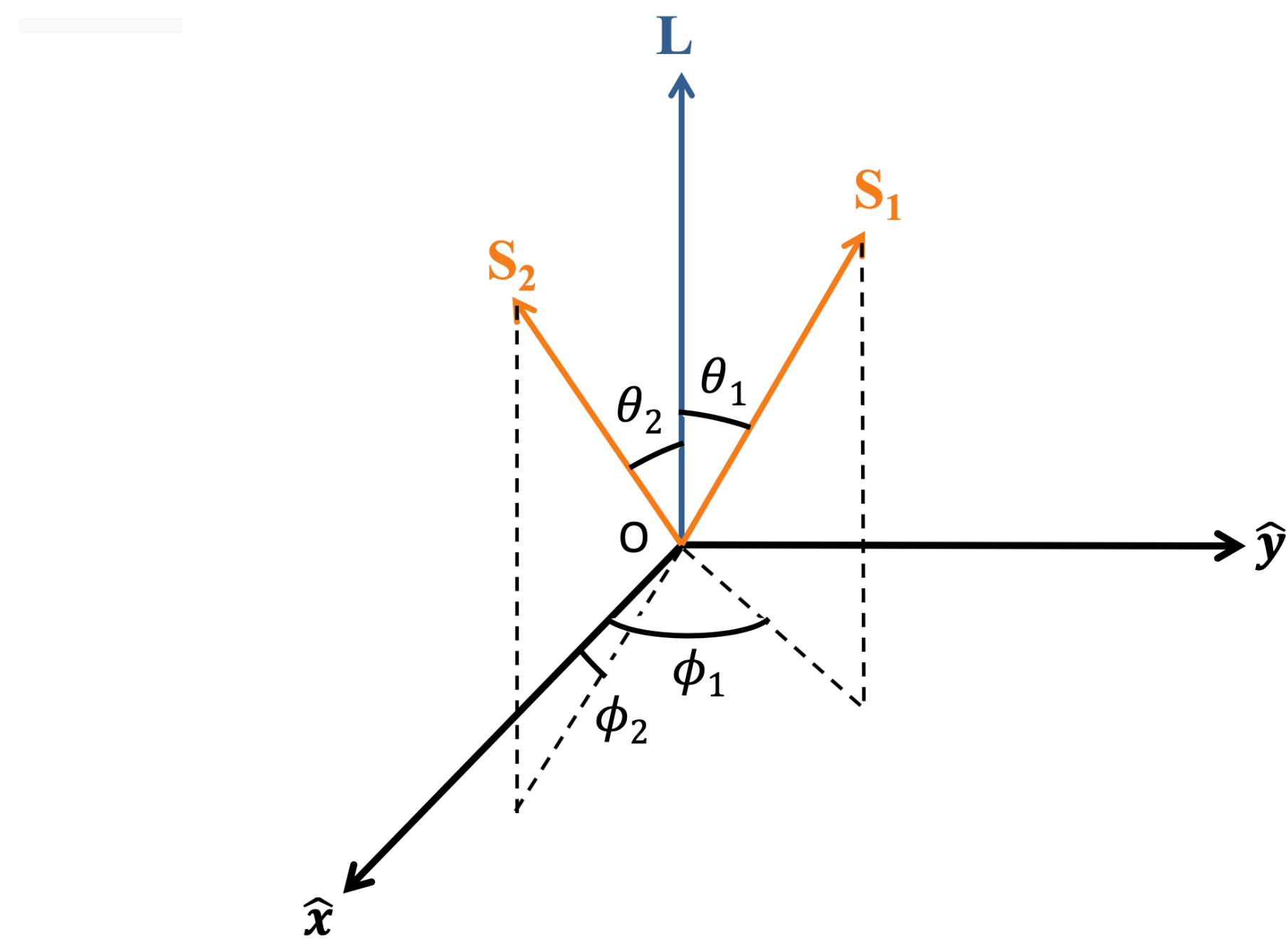


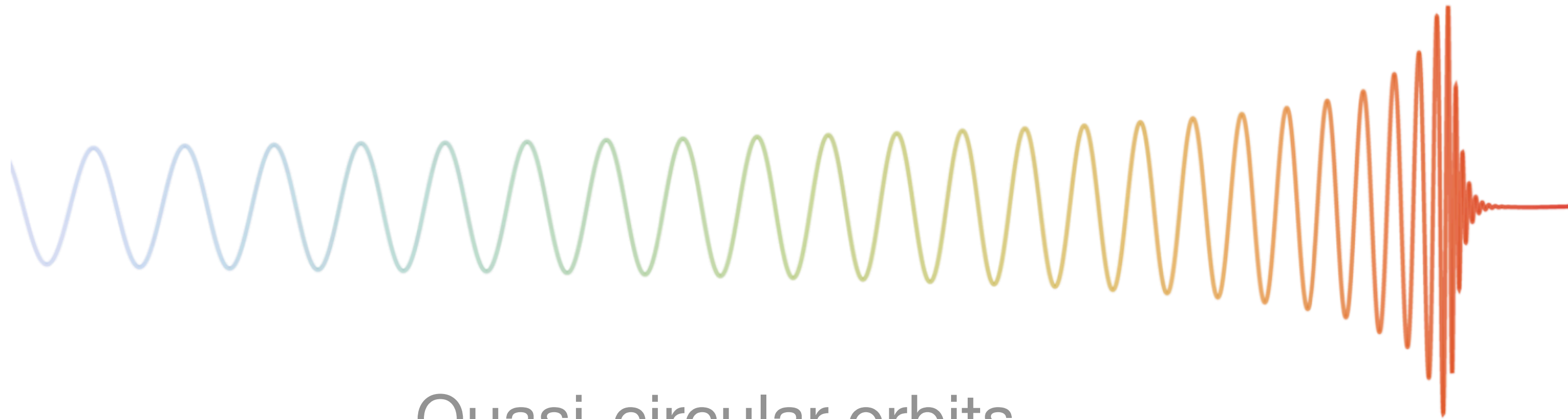
Quasi-circular orbits



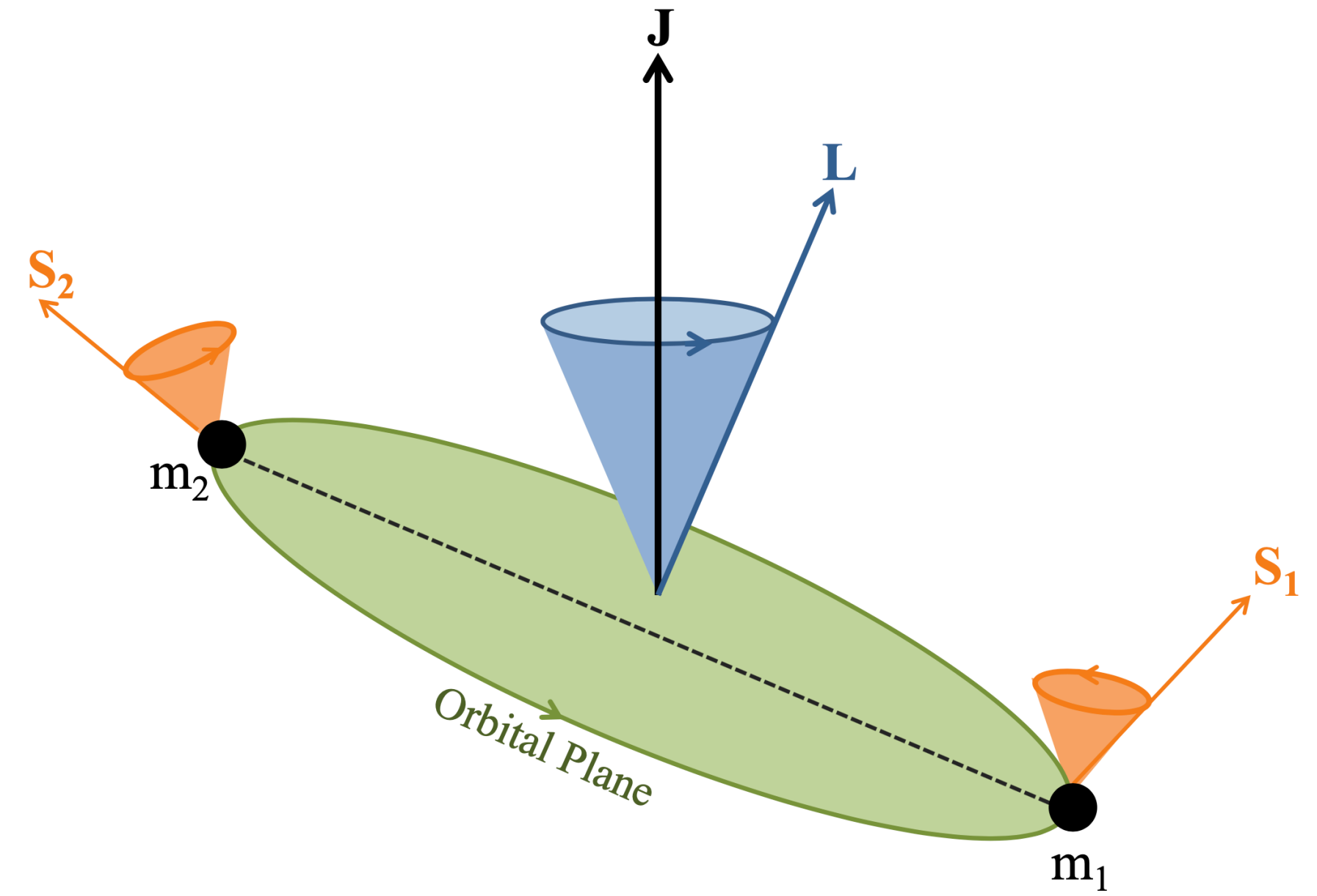
Intrinsic parameters: $m_1, m_2, \chi_1, \theta_1, \phi_1, \theta_2, \phi_2$

Extrinsic parameters: $D_L, \iota, \delta, \alpha, \psi, t_c, \phi_c$





Quasi-circular orbits



Intrinsic parameters: $m_1, m_2, \chi_1, \theta_1, \phi_1, \theta_2, \phi_2$

Chirp mass:

$$\mathcal{M}_c = \frac{(m_1 m_2)^{3/5}}{(m_1 + m_2)^{1/5}}$$

mass ratio:

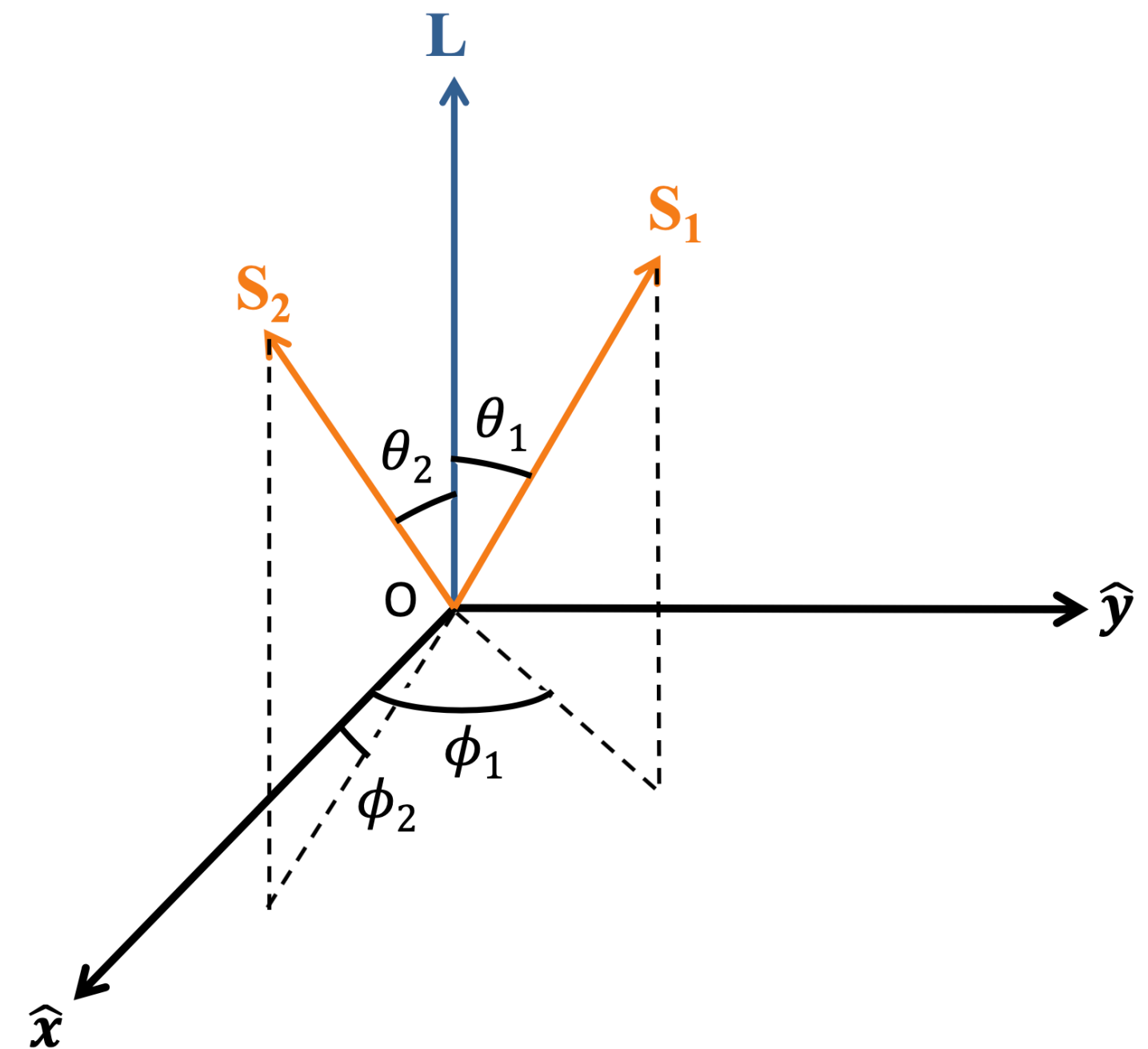
$$q = \frac{m_2}{m_1}$$

effective inspiral spin:

$$\chi_{\text{eff}} = \frac{m_1 \chi_1 \cos \theta_1 + m_2 \chi_2 \cos \theta_2}{m_1 + m_2}$$

effective precessing spin:

$$\chi_p = \max \left[\chi_1 \sin \theta_1, \left(\frac{3 + 4q}{4 + 3q} \right) q \chi_2 \sin \theta_2 \right]$$



Analysis Setup:

[More on detection and parameter estimation in Surabhi's Talk]

- GWTC-3:
 - events from O1, O2 and O3
 - 90 CBCs with $P_{\text{astro}} > 0.5$
- With FAR $< 0.25 \text{ yr}^{-1}$ in at least one detection pipeline: 2 BNSs, 2 NSBHs and 63 BBHs
 - High purity set of events whose selection biases are understood
 - Expect only 1 event to be not of astrophysical origin
- With FAR $< 1 \text{ yr}^{-1}$: 69 BBHs
 - relative proportion of background events remains below 10%
 - Expect only 4.6 events to be not of astrophysical origin
- NS and BH are distinguished based on EOS maximum NS mass

Population Analysis Framework

- Hierarchical Bayesian approach

- Marginalize over the uncertainty in the estimate of individual event parameters

$$\mathcal{L}(\{d\}, N_{\text{det}} | \Lambda, N_{\text{exp}}) \propto N^{N_{\text{det}}} e^{-N_{\text{exp}}} \prod_{i=1}^{N_{\text{det}}} \int \mathcal{L}(d_i | \theta) \pi(\theta | \Lambda) d\theta$$

$$N = \frac{N_{\text{exp}}}{\xi(\Lambda)}$$

$\xi(\Lambda)$: fraction of mergers that are detectable for a population with parameter Λ

$\mathcal{L}(d_i | \theta)$: single-event likelihood described by parameter set θ

$\pi(\theta | \Lambda)$: prior governing the population distribution on event parameters θ for a given value of hyperparameters Λ

Marginalizing the likelihood after imposing the a log-uniform prior on N

$$\mathcal{L}(\{d\} | \Lambda) \propto \prod_{i=1}^{N_{\text{det}}} \frac{\int \mathcal{L}(d_i | \theta) \pi(\theta | \Lambda) d\theta}{\xi(\Lambda)}$$

$\mathcal{L}(d_i | \theta)$ are computed using default prior $\pi_{\emptyset}(\theta)$, hence

$$\mathcal{L}(\{d\} | \Lambda) \propto \prod_{i=1}^{N_{\text{det}}} \frac{1}{\xi(\Lambda)} \left\langle \frac{\pi(\theta | \Lambda)}{\pi_{\emptyset}(\theta)} \right\rangle$$

Using this posterior on Λ can be computed

Population Model Assumptions

Parametric Mass Models: NS masses

- For analyses exclusively focused on the NS-containing events

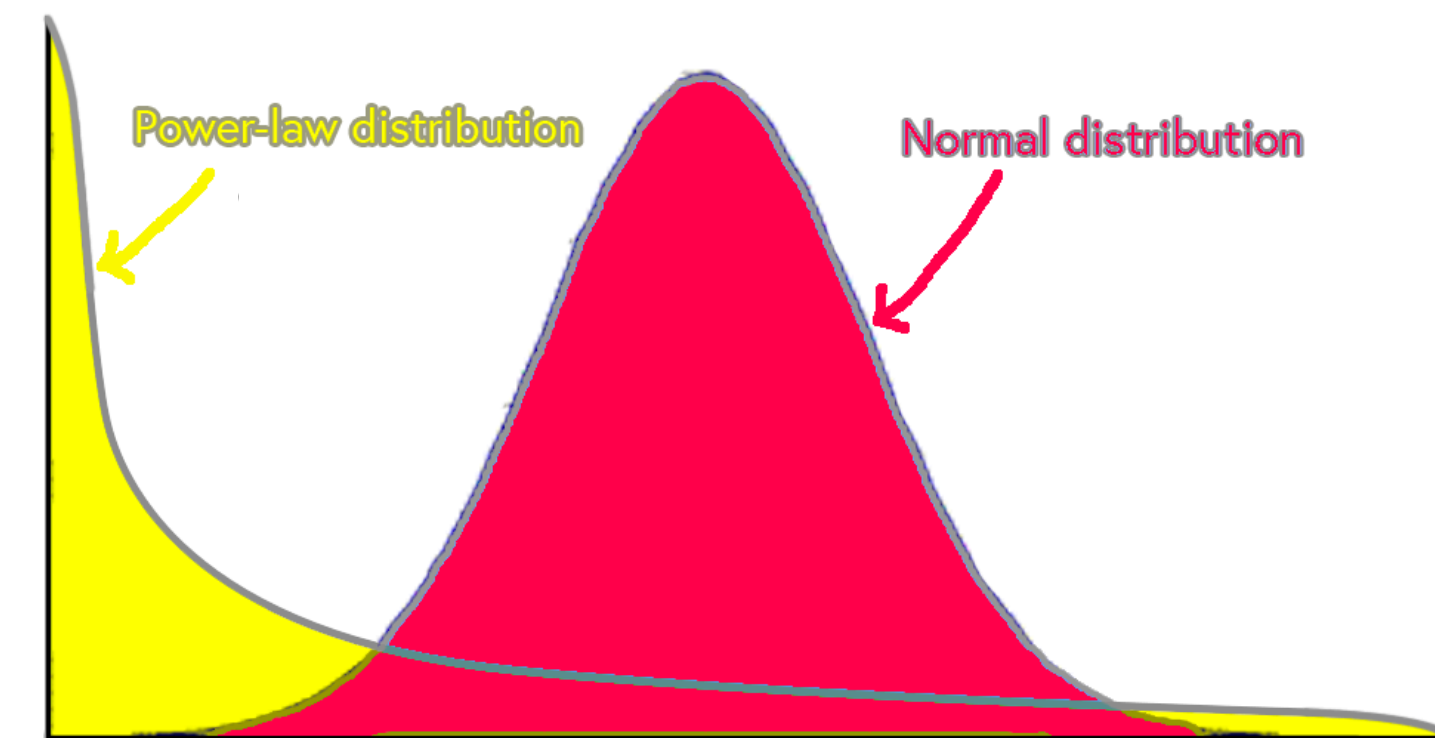
- **POWER**: Power Law

- **PEAK**: Gaussian

- With sharp minimum and maximum mass cutoffs

- Components of BNSs are drawn independently from the common NS mass distribution

- For NSBHs, we assume a uniform BH mass distribution and random pairing with NSs



Parametric Mass Models: BH masses

- Fiducial **Power Law + Peak (PP) model + redshift evolution**

$$p(m_1, q, z) \propto q^\beta p(m_1)(1+z)^{\kappa-1}$$

- Merger rate normalization is chosen such that

$$\mathcal{R}(z) = \frac{dN}{dV_c dt}(z) = \mathcal{R}_0(1+z)^\kappa$$

- The corresponding redshift distribution

$$p(z | \kappa) \propto \frac{1}{1+z} \frac{dV_c}{dz} (1+z)^\kappa$$

Parametric Mass Models: BH masses

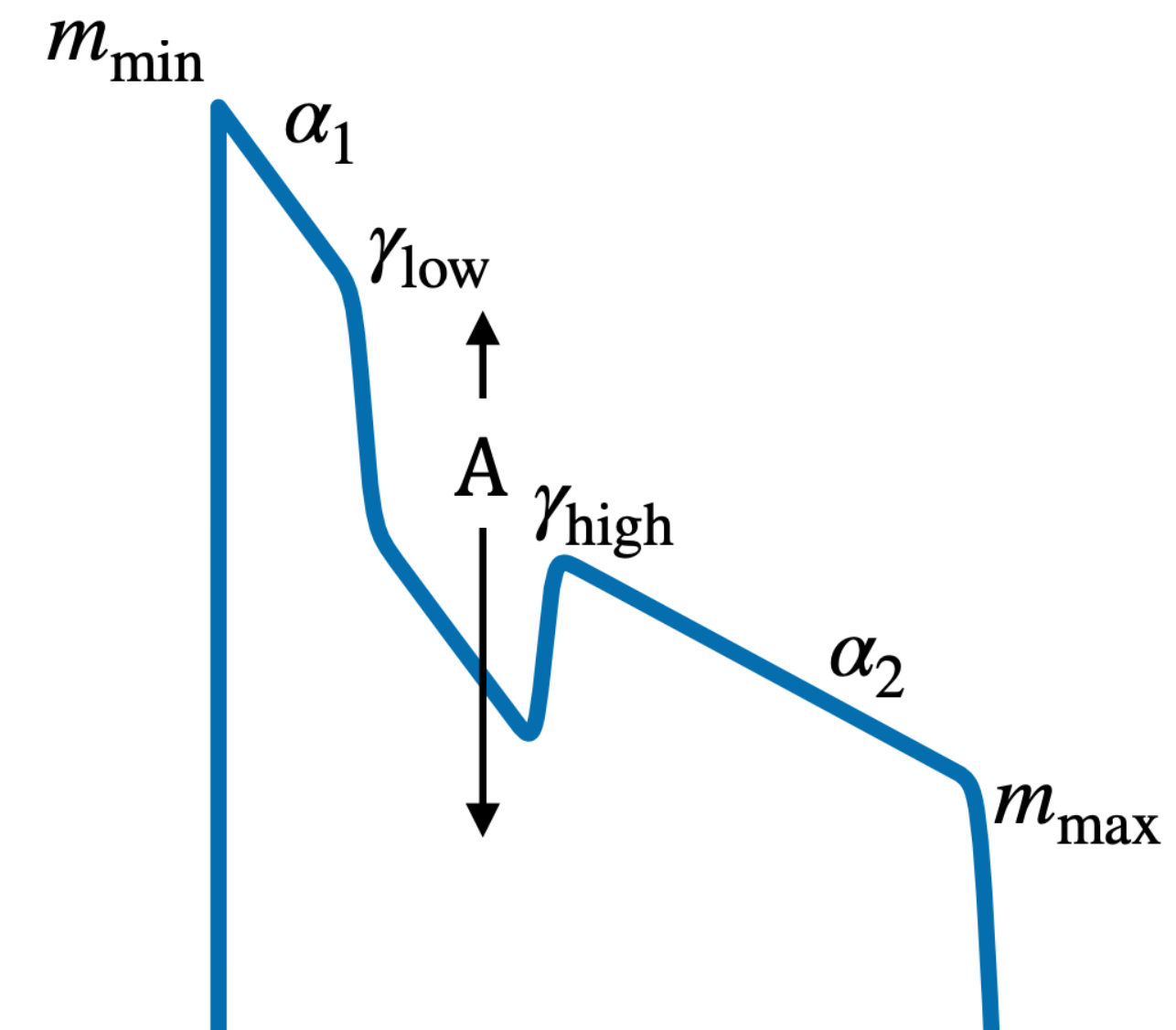
- Power Law + Dip + Break model (PDB)
- To fit the distribution of BH and NS masses, we use a parameterized model, consisting of a broken power law with a notch filter

$$p(m | \lambda) = n(m | M_{\text{low}}^{\text{gap}}, M_{\text{high}}^{\text{gap}}, A) \times l(m | m_{\text{max}}, \eta)$$

$$\times \begin{cases} m^{\alpha_1} & \text{if } m < M_{\text{high}}^{\text{gap}} \\ m^{\alpha_2} & \text{if } m > M_{\text{high}}^{\text{gap}} \\ 0 & \text{if } m > m_{\text{max}} \text{ or } m < m_{\text{min}} \end{cases}$$

notch filter with depth A applied between $M_{\text{low}}^{\text{gap}}$ and $M_{\text{high}}^{\text{gap}}$

low pass filter with powerlaw η applied at mass m_{max}



- Two pairing probability:
 - **Random:** $p(m_1, m_2 | \Lambda) \propto p(m = m_1 | \Lambda) p(m = m_2 | \Lambda) \Theta(m_2 < m_1)$
 - **power-law-in-mass-ratio:** $p(m_1, m_2 | \Lambda) \propto p(m = m_1 | \Lambda) p(m = m_2 | \Lambda) q^\beta \Theta(m_2 < m_1)$

BH Spin Models

- **Default spin model**

- Spin magnitude drawn from Beta distribution $p(\chi_i | \alpha_\chi, \beta_\chi) \propto \chi_i^{\alpha-1} (1 - \chi_i)^{\beta-1}$

- Spin tilts are mixture of isotropic and aligned

$$p(\cos \theta_i | \zeta, \sigma_t) = \frac{1}{2} (1 - \zeta) + \zeta \mathcal{N}_{[-1,1]}(\cos \theta_i; 1, \sigma_t)$$

4 model parameters

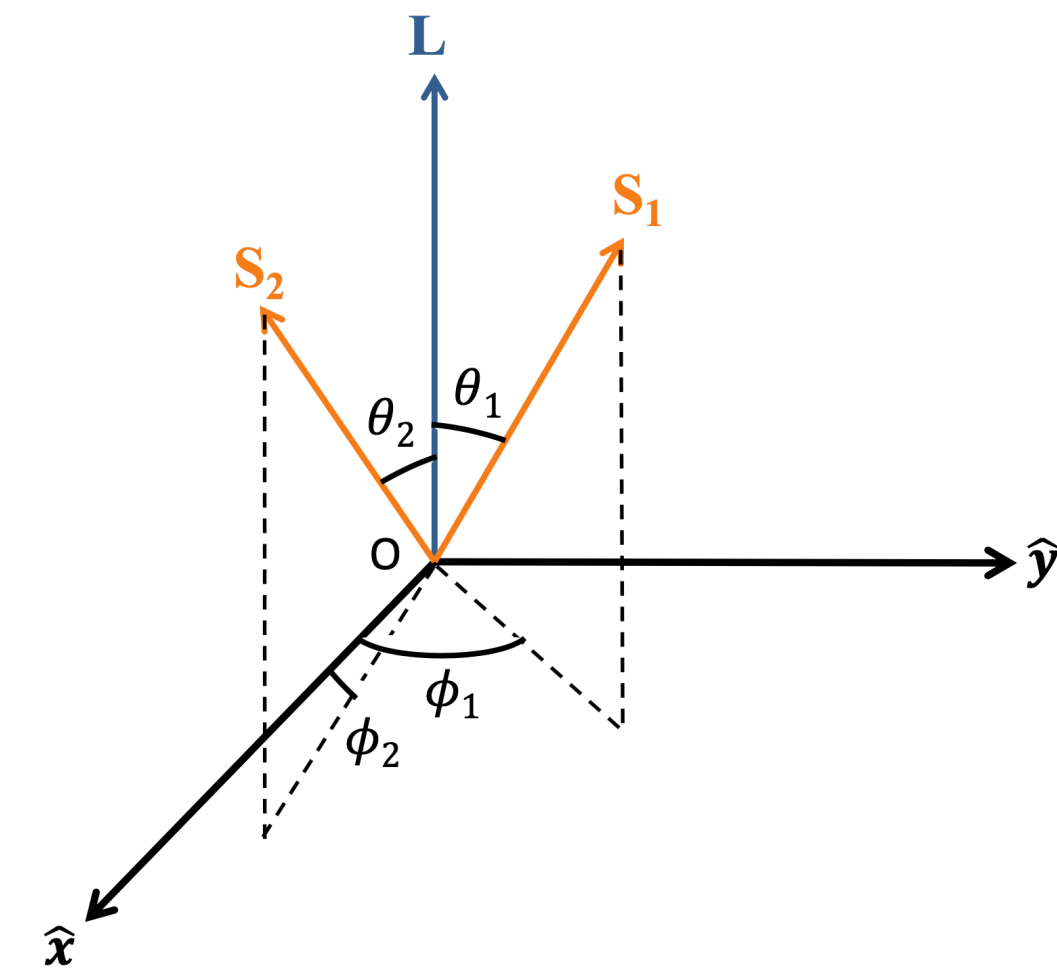
- **Gaussian spin model**

- Bivariate Gaussian in χ_{eff} and χ_p

$$p(\chi_{\text{eff}}, \chi_p | \mu_{\text{eff}}, \sigma_{\text{eff}}, \mu_p, \sigma_p, r) \propto \mathcal{N}(\chi_{\text{eff}}, \chi_p | \mu, \Sigma)$$

$$\mu = (\mu_{\text{eff}}, \mu_p) \text{ and } \Sigma = \begin{pmatrix} \sigma_{\text{eff}}^2 & r\sigma_{\text{eff}}\sigma_p \\ r\sigma_{\text{eff}}\sigma_p & \sigma_p^2 \end{pmatrix}$$

5 model parameters



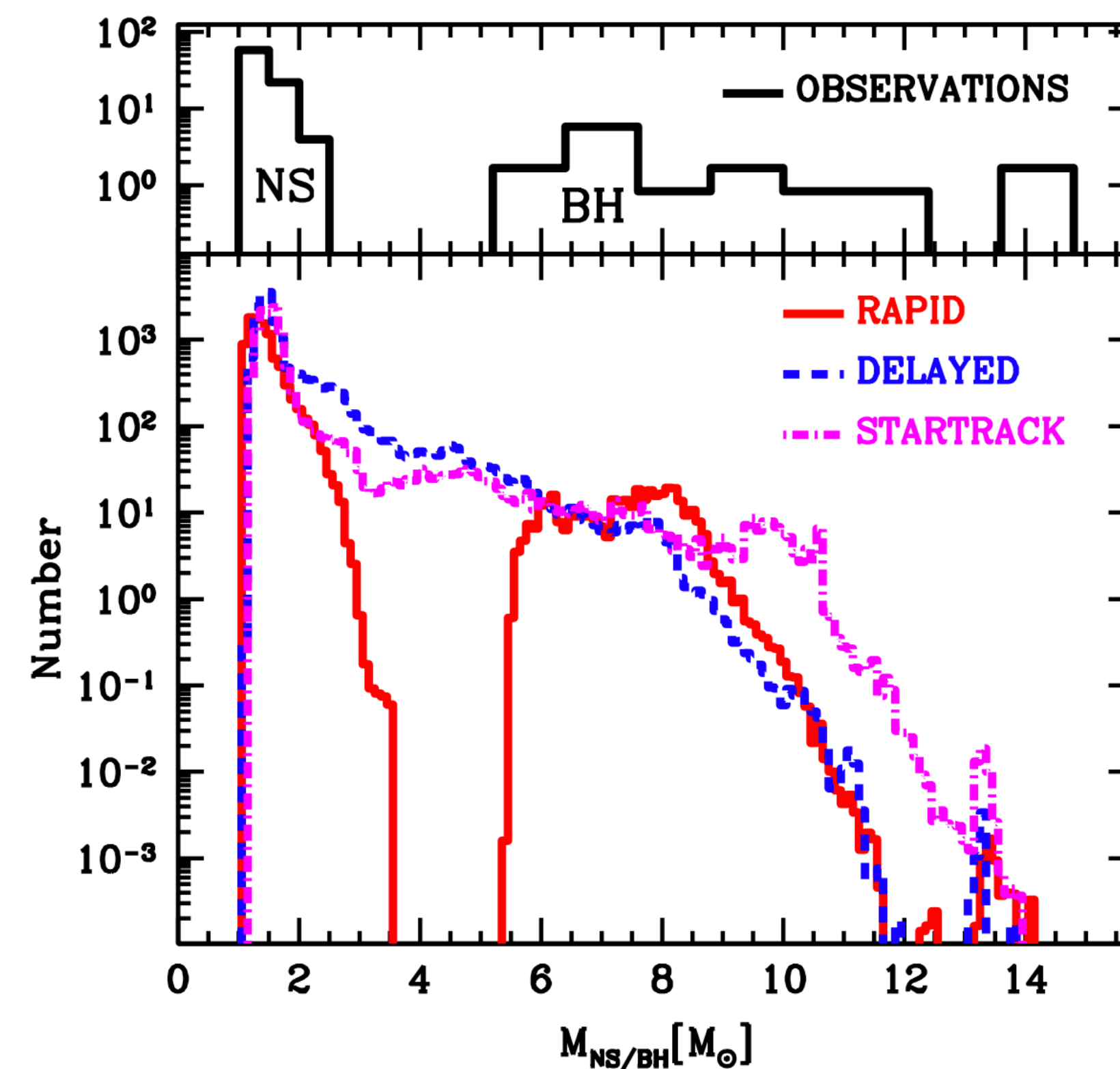
Merger Rates

	BNS	NSBH	BBH	NS-Gap	BBH-gap	Full
	$m_1 \in [1, 2.5]M_\odot$	$m_1 \in [2.5, 50]M_\odot$	$m_1 \in [2.5, 100]M_\odot$	$m_1 \in [2.5, 5]M_\odot$	$m_1 \in [2.5, 100]M_\odot$	$m_1 \in [1, 100]M_\odot$
	$m_2 \in [1, 2.5]M_\odot$	$m_2 \in [1, 2.5]M_\odot$	$m_2 \in [2.5, 100]M_\odot$	$m_2 \in [1, 2.5]M_\odot$	$m_2 \in [2.5, 5]M_\odot$	$m_2 \in [1, 100]M_\odot$
PDB (pair)	960^{+1740}_{-700}	59^{+81}_{-38}	$25^{+10}_{-7.0}$	41^{+69}_{-30}	$9.3^{+18.7}_{-7.6}$	1100^{+1700}_{-750}
PDB (ind)	250^{+640}_{-196}	170^{+150}_{-89}	$22^{+9.0}_{-6.0}$	29^{+55}_{-23}	$10^{+15}_{-8.0}$	470^{+830}_{-300}
MS	470^{+1430}_{-413}	57^{+123}_{-42}	42^{+88}_{-20}	$3.7^{+20.3}_{-3.4}$	$0.17^{+55.83}_{-0.16}$	650^{+1550}_{-460}
BGP	99^{+260}_{-86}	32^{+62}_{-25}	33^{+16}_{-10}	$2.1^{+33.0}_{-2.1}$	$5.1^{+12.0}_{-4.0}$	180^{+260}_{-110}
MERGED	13 – 1900	7.4 – 320	16 – 130	0.029 – 84	0.0095 – 56	71 – 2200

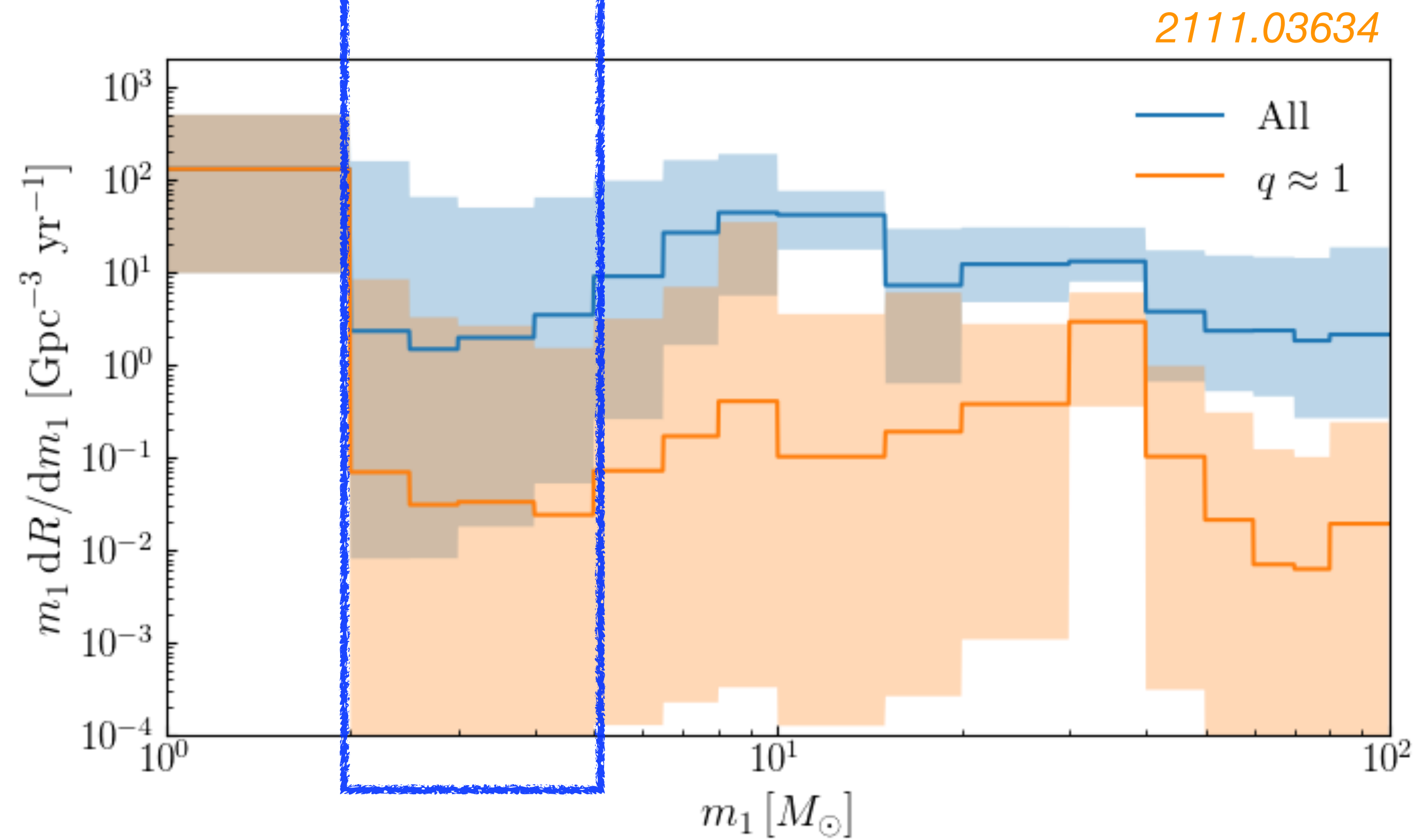
- Self consistent measure of merger rate of all detected CBCs
- Subdivided into astrophysically interesting mass ranges
- Constant co-moving volume merger rate density
- BBH merger rates are consistent with previously published estimates
- For BNS/NSBH, the inferred rate depends on the presumed mass distribution
- Different approaches arrive at different binary mass distributions between $1 M_\odot$ and $2.5 M_\odot$
- Highlights the importance of modeling systematics when drawing inferences about populations with few confident members

Lower mass gap

- NSs are expected to have a maximum mass of $\sim 3 M_{\odot}$
- Heaviest NS observed to date has mass $2.01 \pm 0.04 M_{\odot}$
- PSR J0740+6620 ‘may’ host a $\sim 2.07\text{-}2.08 M_{\odot}$ NS
- X-ray observations found a dearth of objects in the $3 - 5 M_{\odot}$ range
- Population synthesis models with rapid supernova instabilities can not produce BHs of mass $< 5 M_{\odot}$
- Thus, we don’t expect to observe binaries with component masses in $\sim 3\text{-}5 M_{\odot}$ in GWs
 - provided they are formed in a way similar to the binaries observed with EM radiation



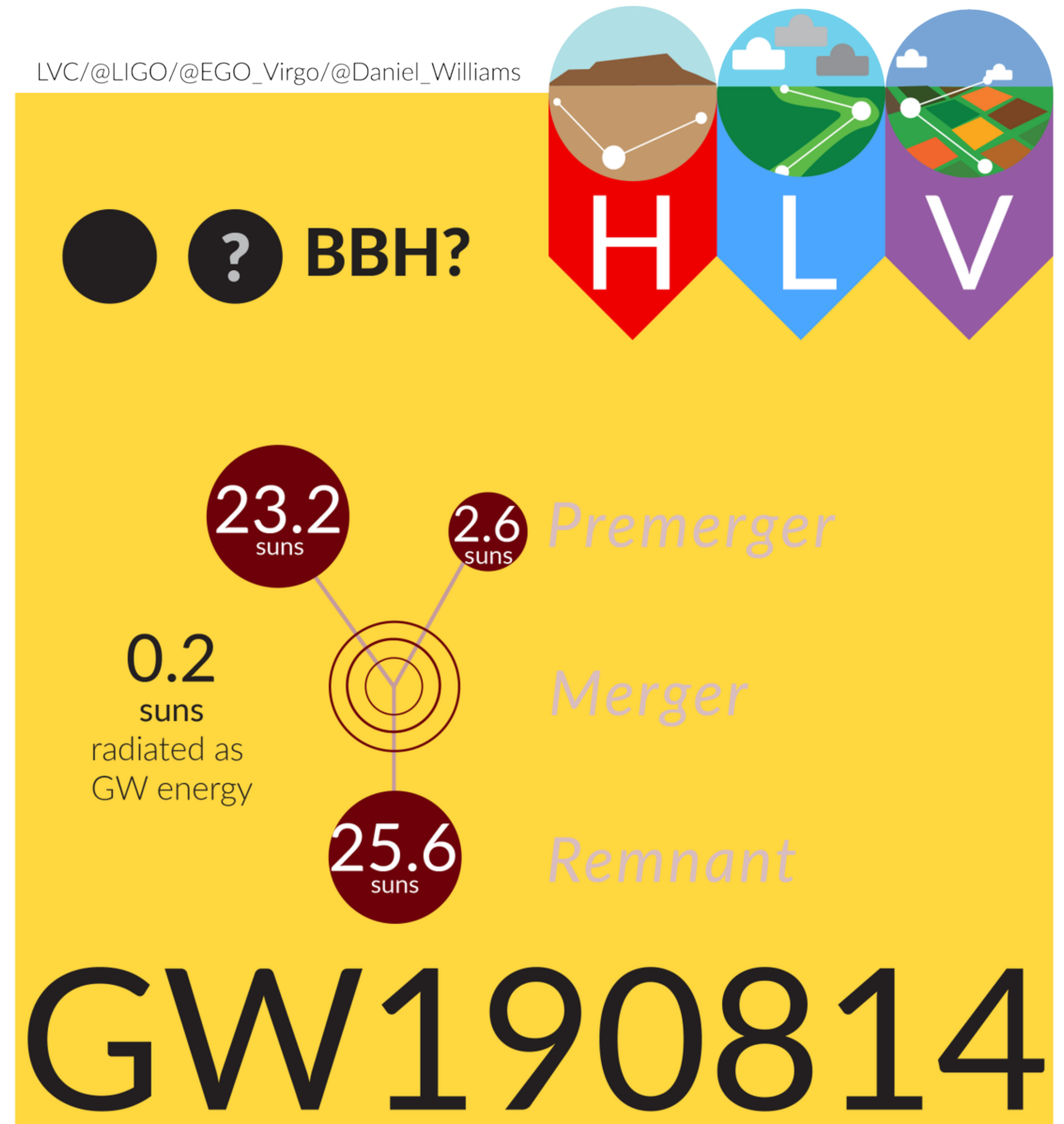
Belczynski et al, 2012



- A reduction in the rate above NS masses
- Unable to confidently infer absence or presence of a subsequent rise in merger rates from lower mass gap masses
- Neither find evidence for nor rule out the existence of a two-sided lower mass gap
- Rates in mass gap are 1 or 2 order of magnitude different; GW data suggest two distinct populations of compact objects
- If a lower mass gap does exist, it may not be totally empty

Possible ways to populate this gap

- Remnants of binary neutron stars
(Gupta et al, 2020)
- Hierarchical merger of stellar few-body systems
(Safarzadeh et al, 2020, Lu et al, 2020)
- BHs of primordial origin (García-Bellido, 2019)
- Still a mystery that what the secondary of GW190814 is?
- Primary of GW190425 ($m_1 \in [1.61, 2.52]M_{\odot}$) could be a low-mass gap BH



Masses

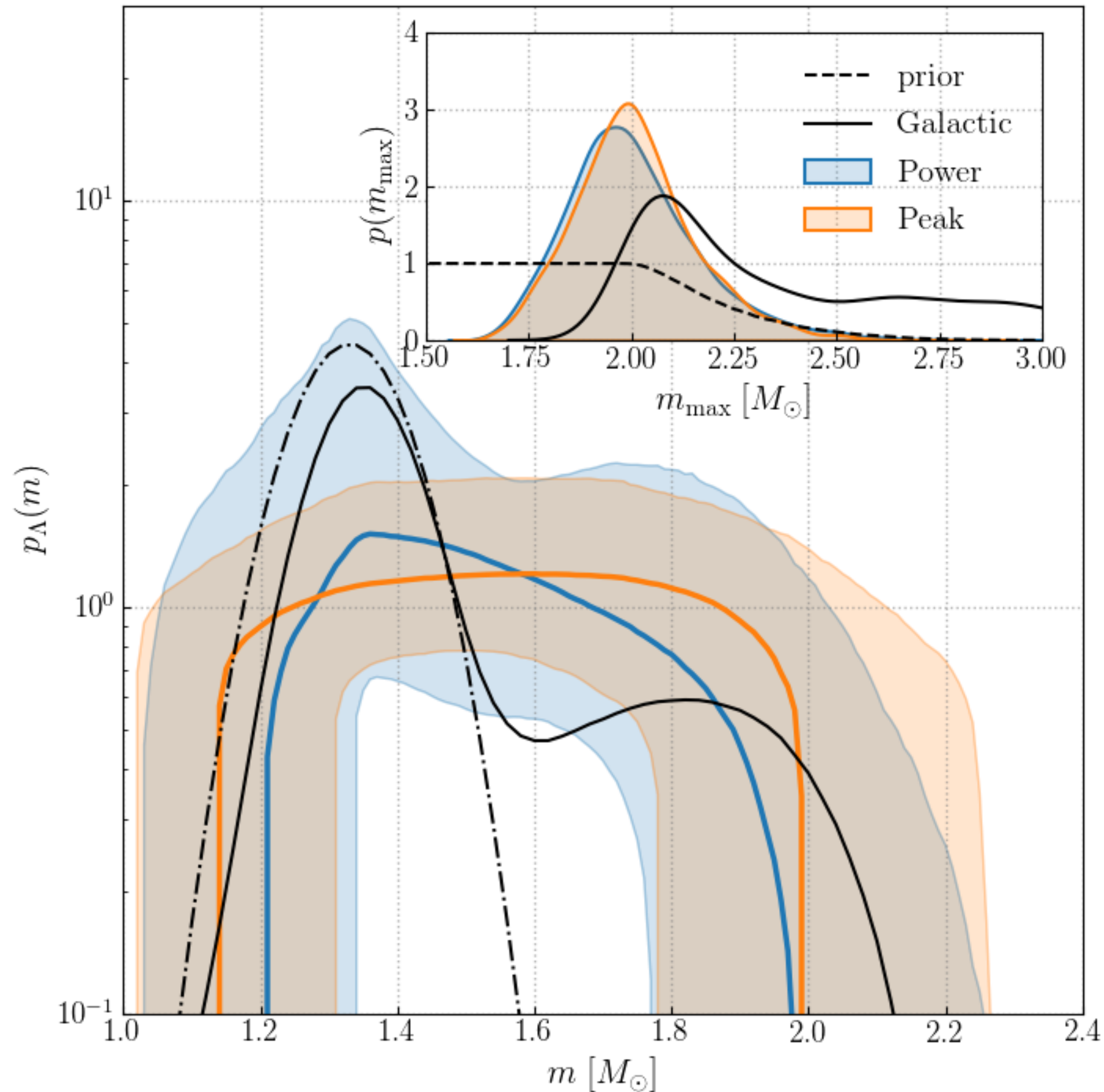
NS masses in binaries

- **Classification criteria:** probability that at least one of the component masses is less than the maximum NS mass > 50%

- $M_{\text{max,TOV}} = 2.21^{+0.31}_{-0.21} M_{\odot}$ from 2106.05313 based on pulsar timing, GW and X-ray observations of NSs

Name	$\text{FAR}_{\text{min}} \text{ (yr}^{-1}\text{)}$	$P(m < M_{\text{max,TOV}})$	$P(m < M_{\text{low}}^{\text{gap}})$	Classification
GW170817	$< 1 \times 10^{-5}$	0.99	0.98	BNS
GW190425	3.38×10^{-02}	0.68	0.73	BNS
GW190814	$< 1 \times 10^{-5}$	0.06	0.19	BBH
GW200105	2.04×10^{-01}	0.94	0.74	NSBH
GW200115	$< 1 \times 10^{-5}$	0.95	0.97	NSBH
GW190426	9.12×10^{-01}	0.82	–	NSBH
GW190917	6.56×10^{-01}	0.56	–	NSBH

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Power: $\alpha = -2.0^{+5.1}_{-7.0}$

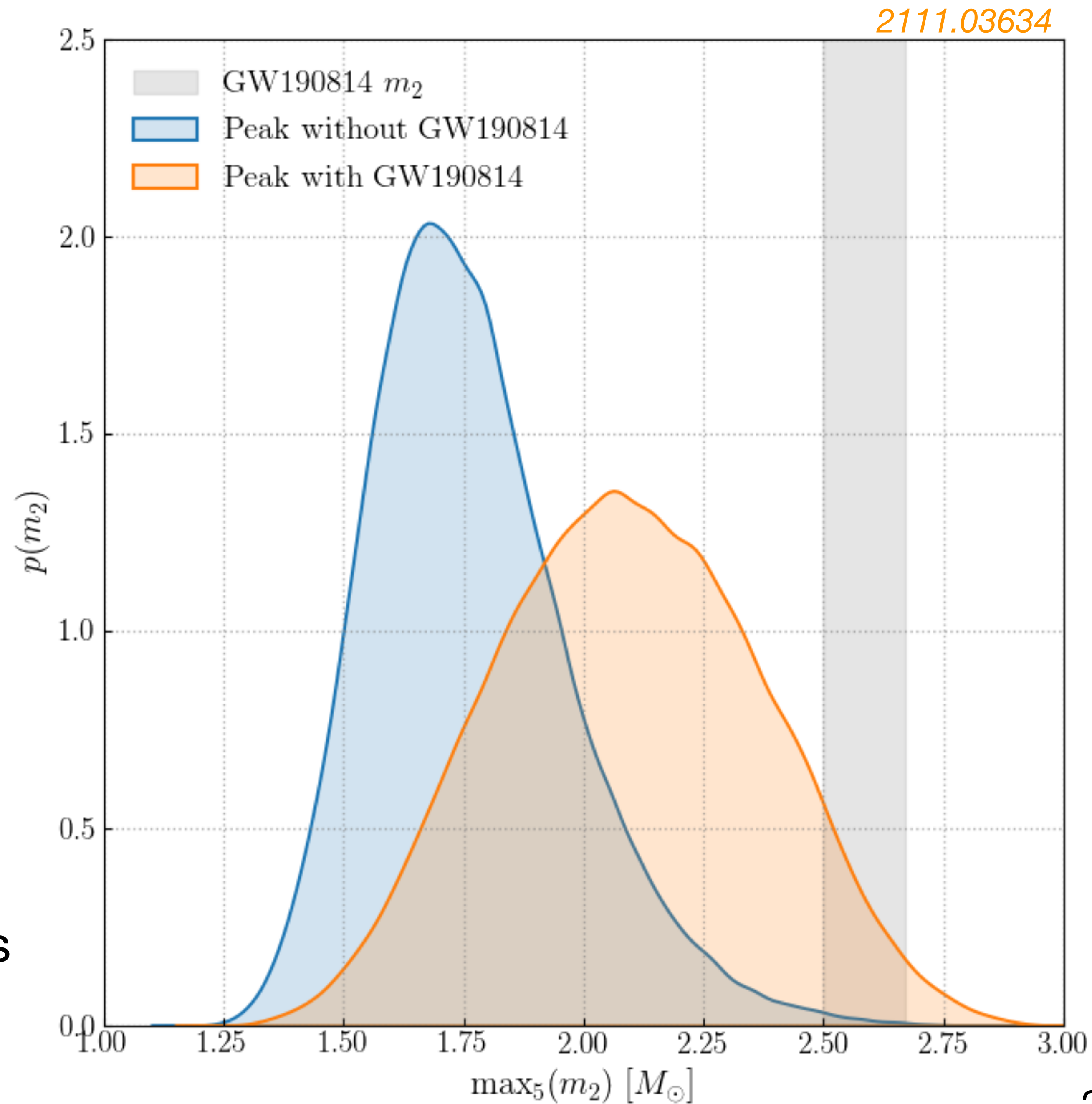
Peak: $\sigma = 1.1^{+0.8}_{-0.8} M_{\odot}$ and $\mu = 1.5^{+0.4}_{-0.4} M_{\odot}$

- GW observations to date do not support a NS mass distribution with a pronounced single peak
- In contrasts with the Galactic BNS subpopulation whose mass distribution is sharply peaked around $1.35 M_{\odot}$
- Mass distribution of NSs observed in GWs is broader and has greater support for high-mass NSs
- Galactic NS population distribution has a double-peaked shape

$$m_{\min} = 1.2^{+0.1}_{-0.2} M_{\odot} \quad m_{\max} = 2.0^{+0.3}_{-0.2} M_{\odot}$$

GW190814 is an outlier from the secondary masses in BNS and NSBH systems

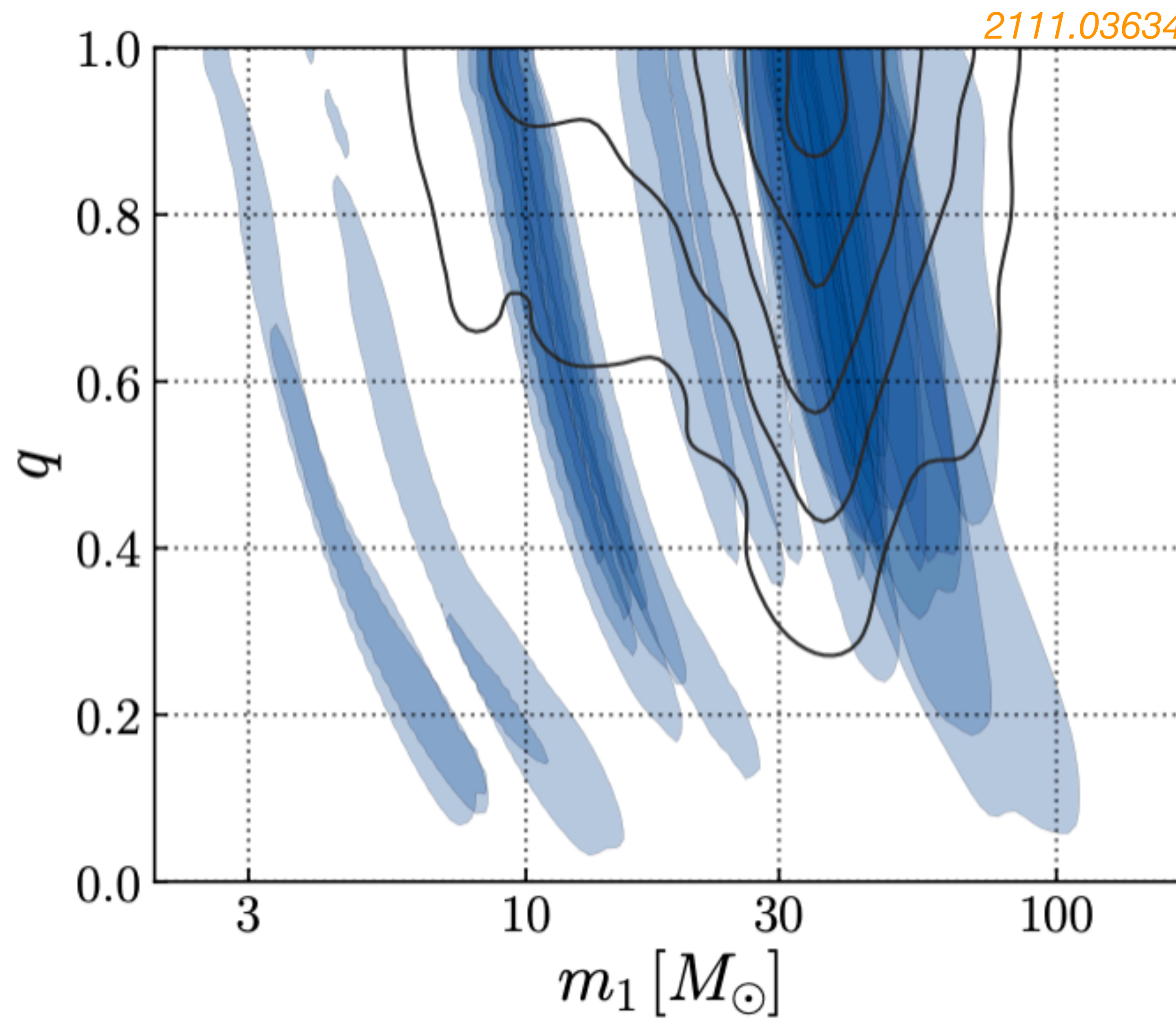
$\max_5(m_2)$: the largest observed secondary mass after 2 BNS observations and 3 NSBH observations

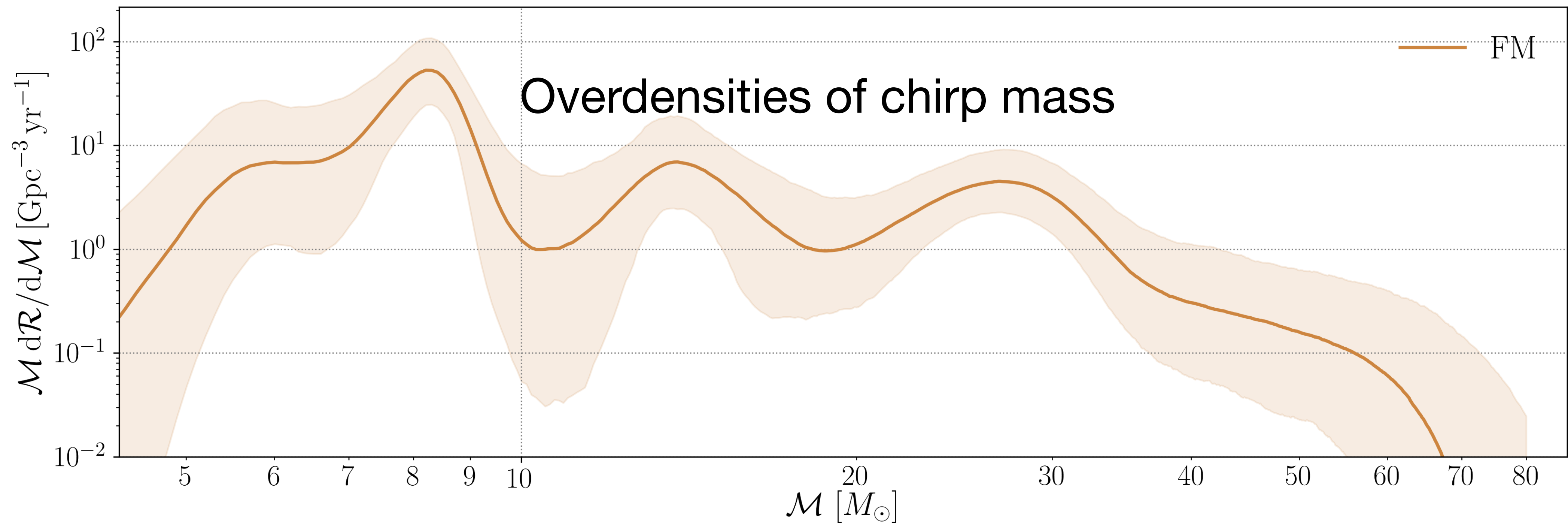
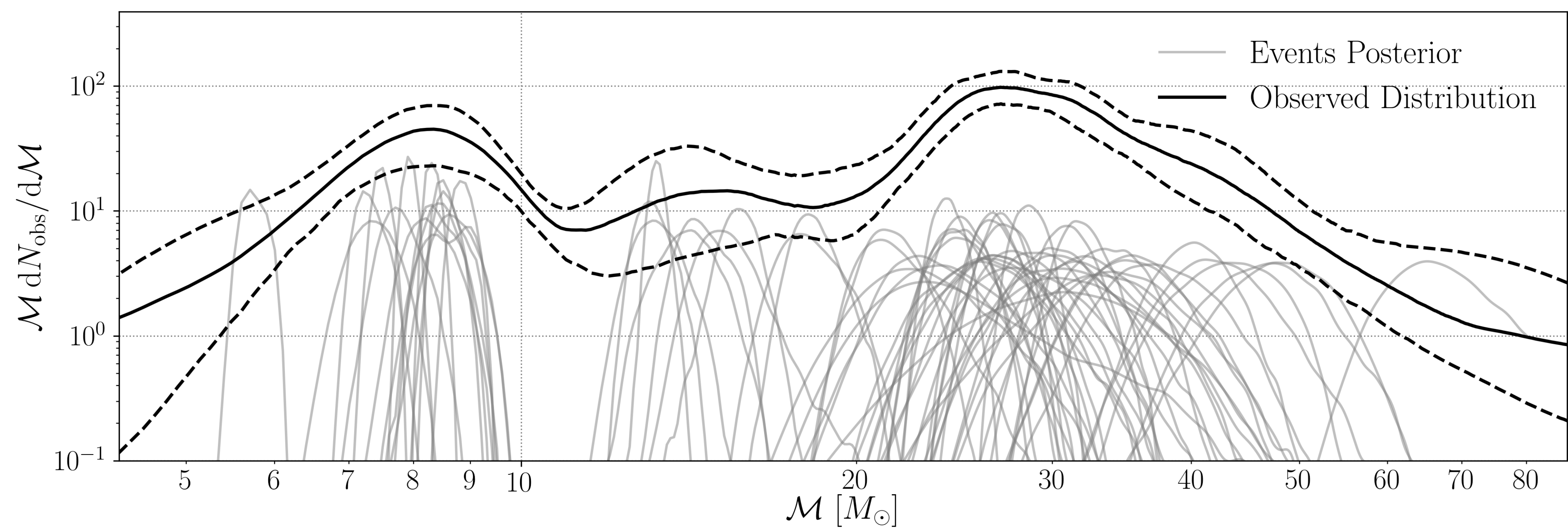


BH masses in binaries

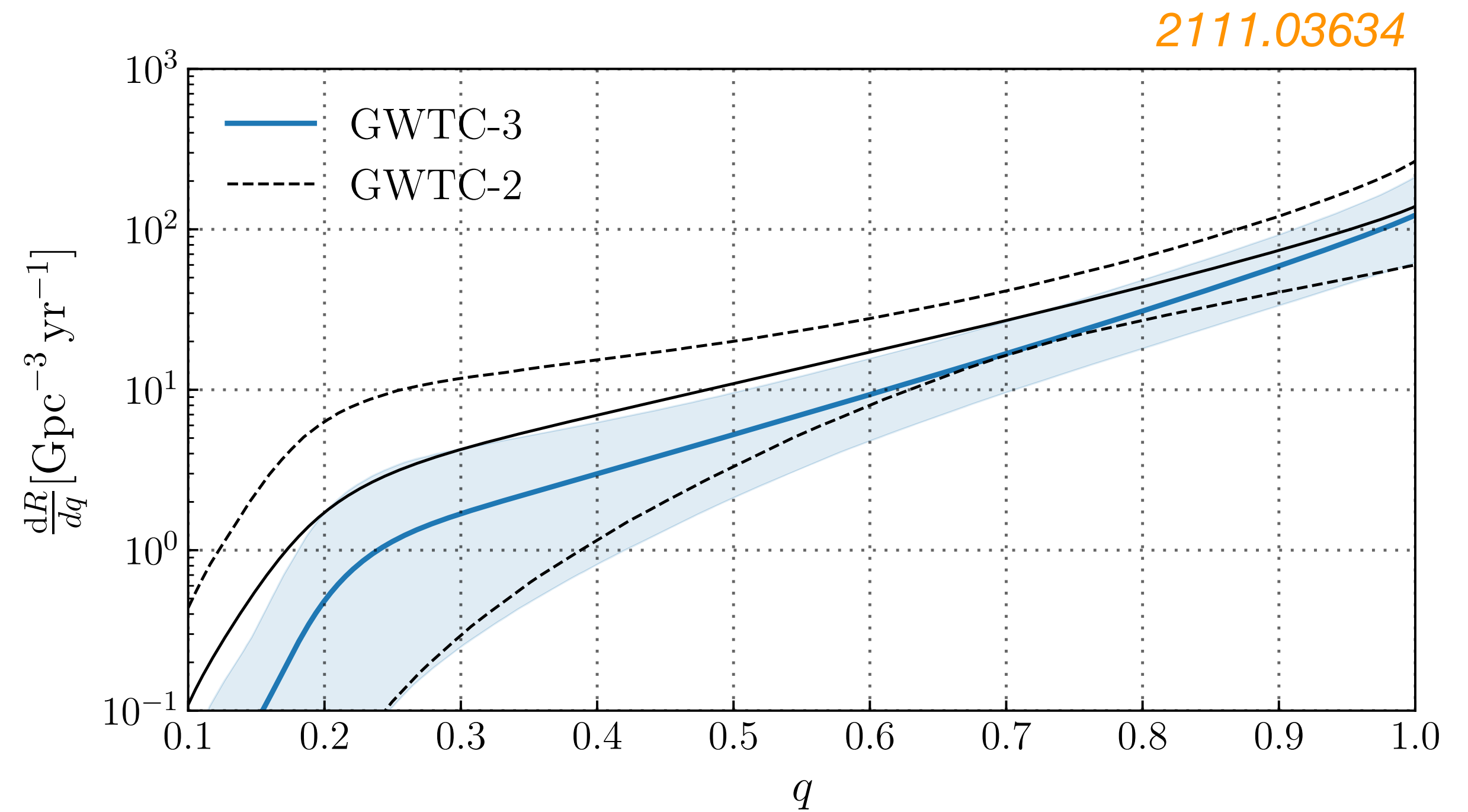
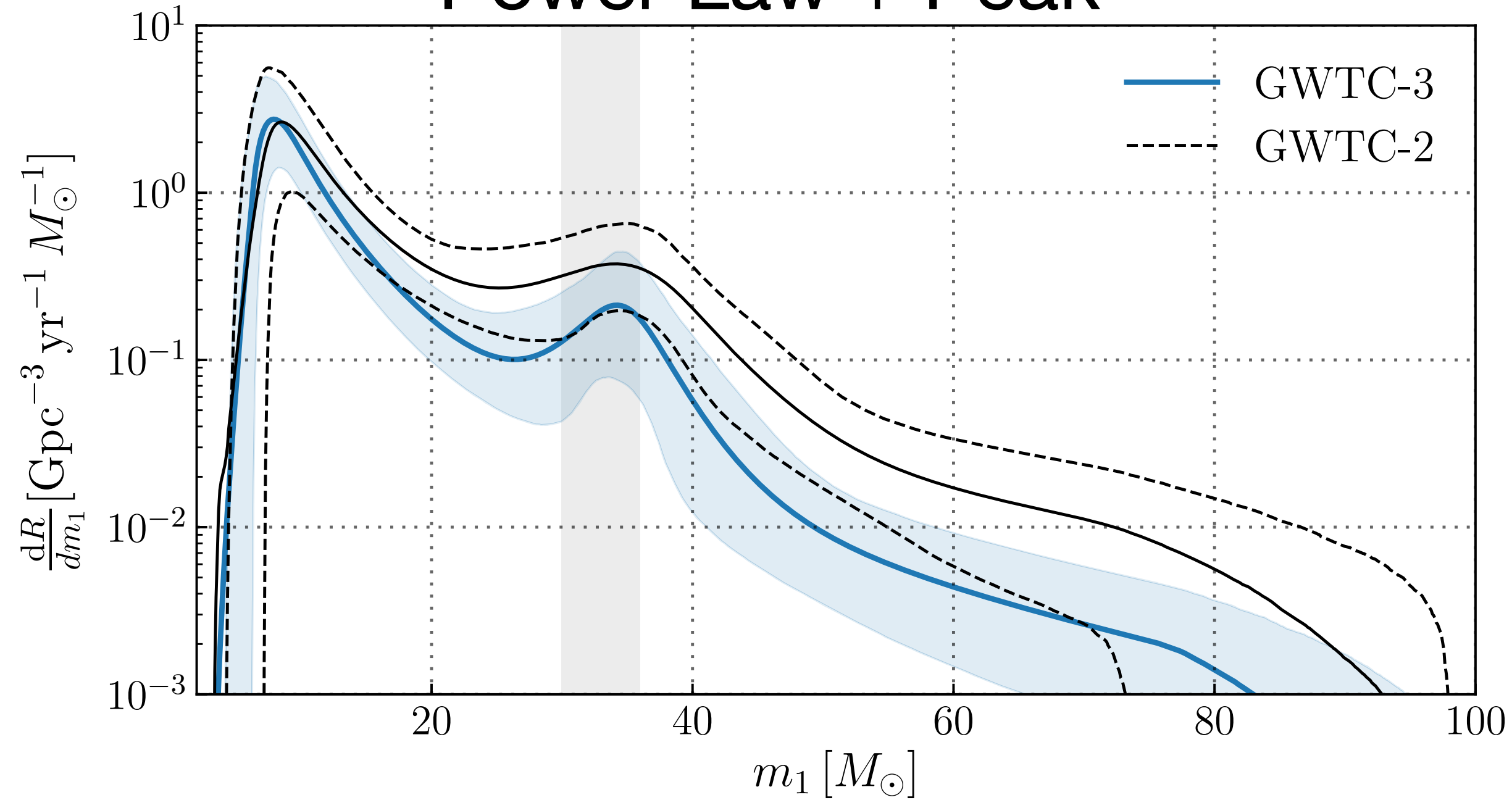
FAR threshold of 1 yr^{-1} and redshift dependence

BH mass distribution is consistent with GWTC-2





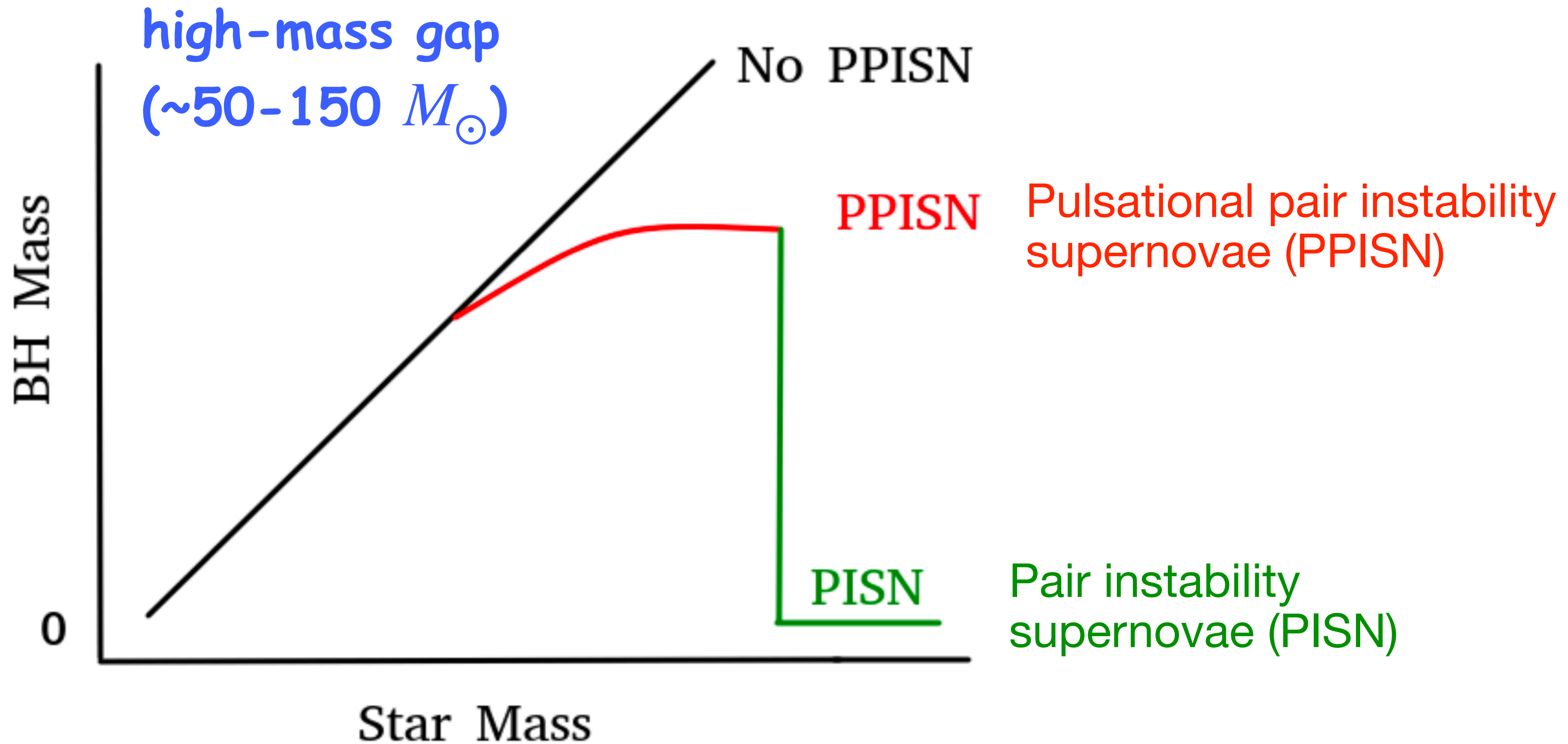
Power Law + Peak



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- The inferred mass spectrum decays more rapidly
- Expected because new observations in GWTC-3 contain a greater fraction of lower mass systems
- The inferred mass ratio distribution is less peaked towards equal mass binaries compared to GWTC-2
- Inconclusive evidence for an upper mass gap ($\sim 50\text{-}150 M_\odot$)

High-mass gap: what theory says?



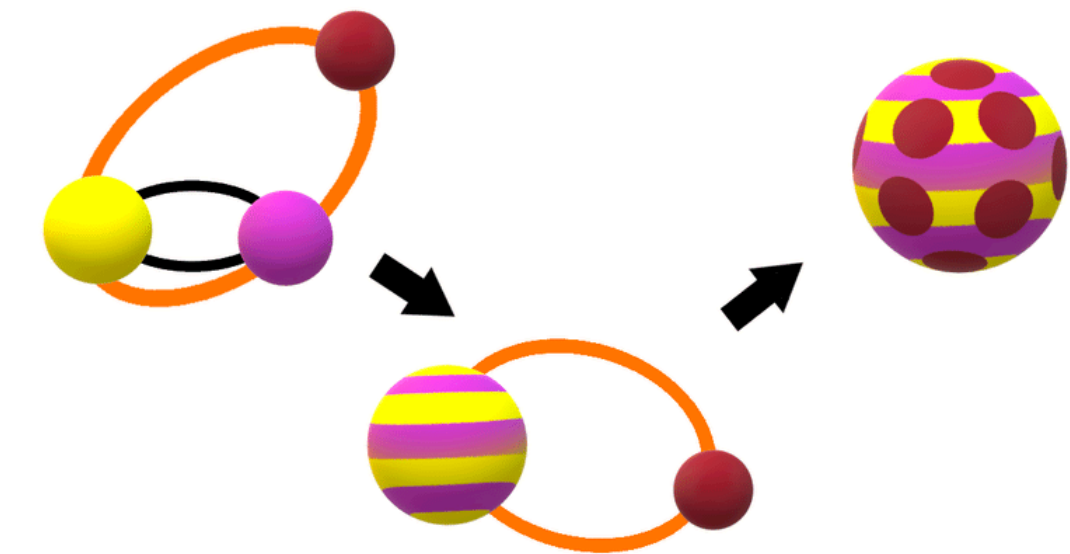
Inconclusive evidence for upper mass gap

- A gap is defined as a rapid decline and a rapid rise in merger rate at significantly higher mass
- No evidence is found for such a gap
- The PPISN mass gap could start at higher mass than theory expects
- Or the high-mass binaries in GWTC-3 could be formed in a way that avoids PPISN

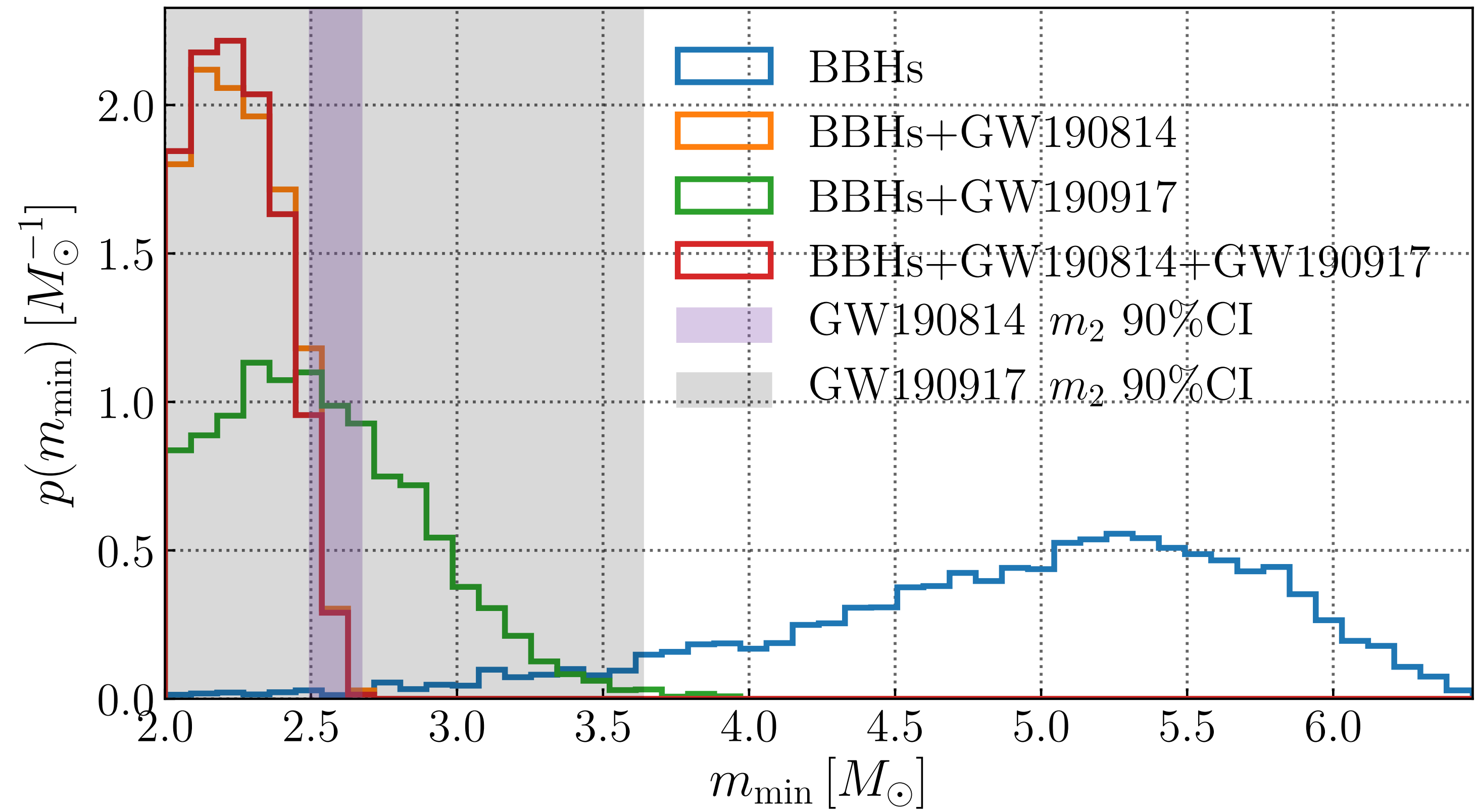
Possible ways to populate this gap

[More in Vishal and Parthapratim's Talks]

- Hierarchical BBH mergers
- Stellar mergers
- BH remnants of population III stars
- Stellar triples in the field of the galaxy
- Growth via accretion in an Active Galactic Nuclei (AGN)



GW190814 and GW190917
are outliers from the
secondary masses in BBH
systems

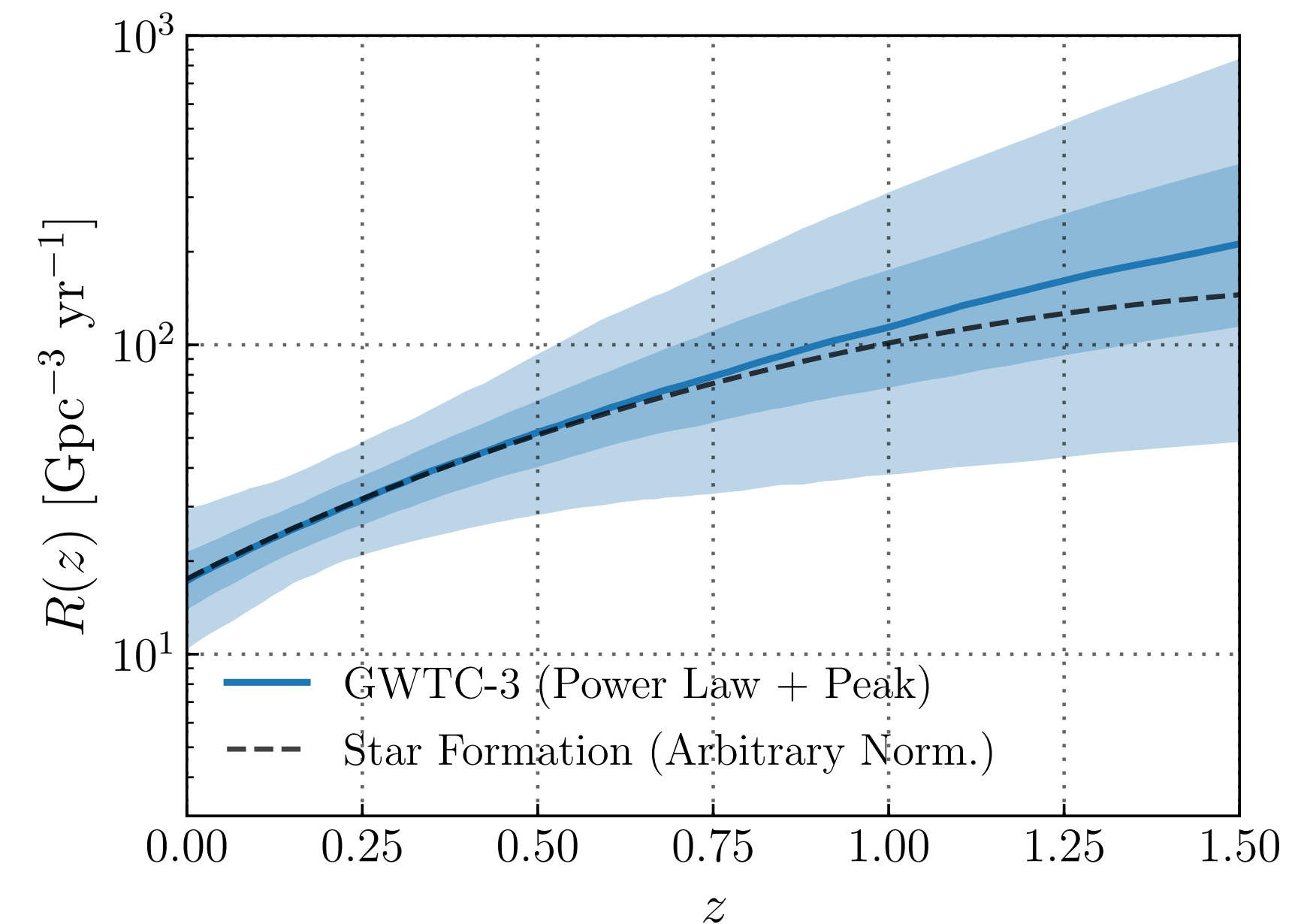
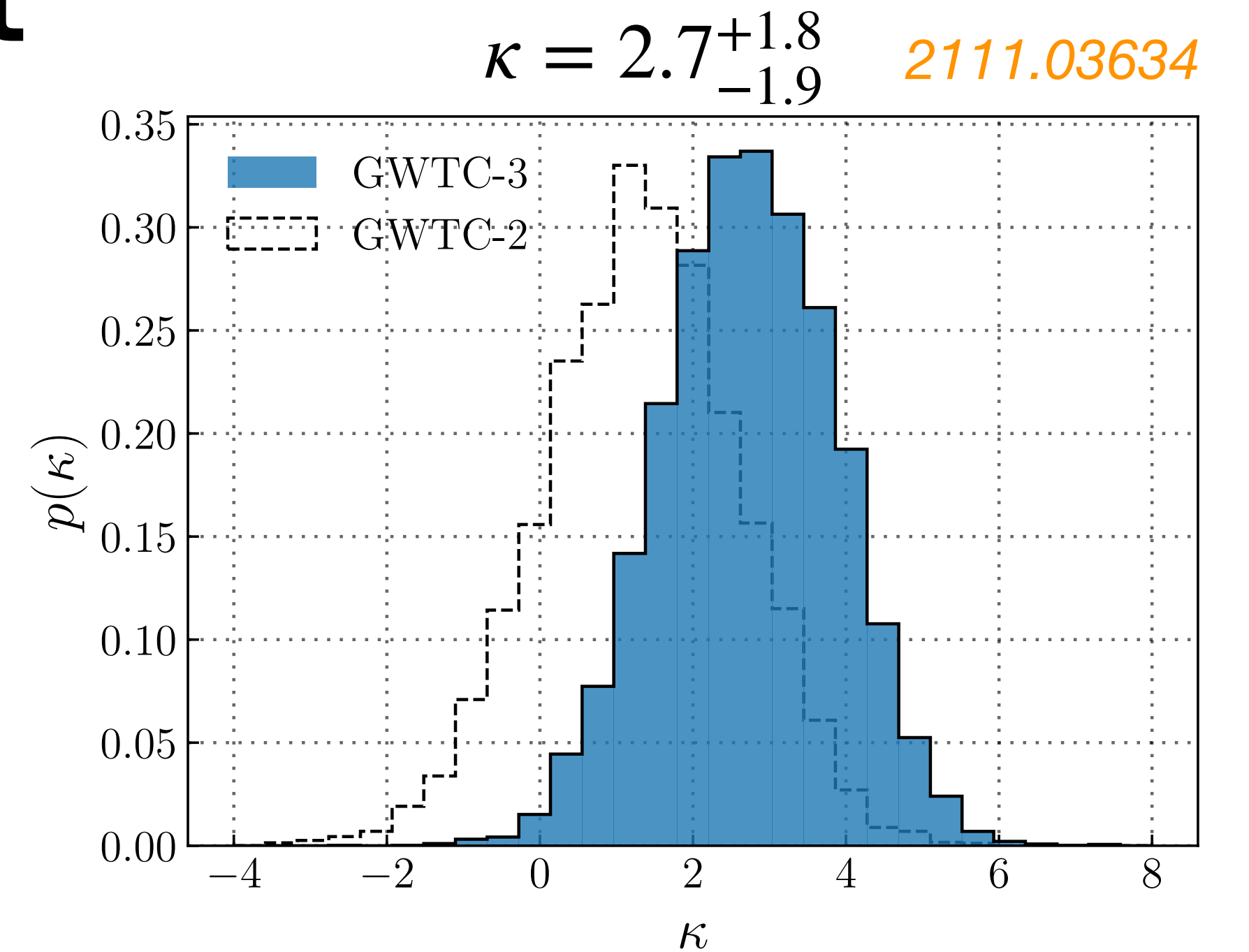


m_{\min} : minimum recovered BH mass

Evolution of rates with redshift

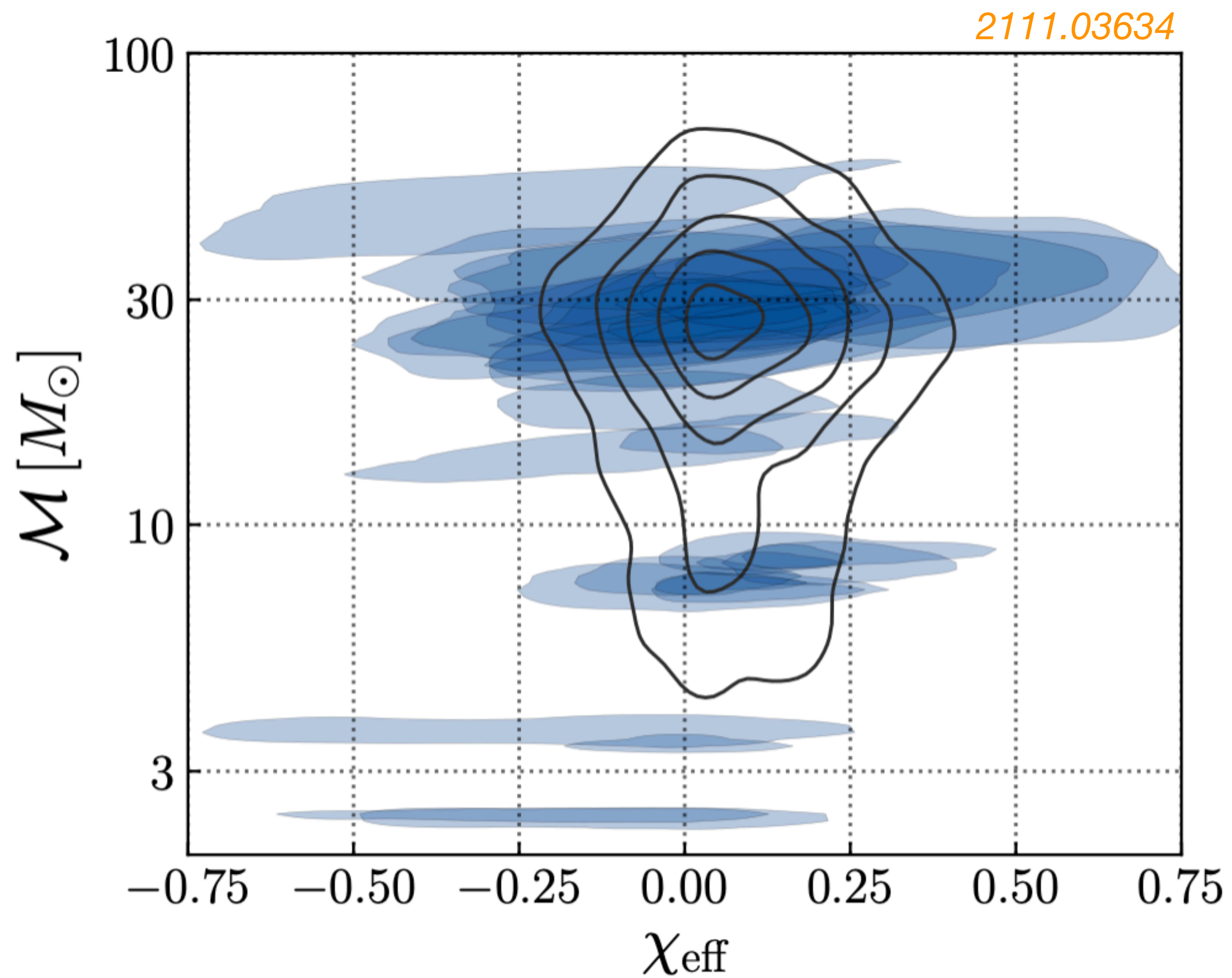
$$\mathcal{R}(z) = \frac{dN}{dV_c dt}(z) = \mathcal{R}_0(1+z)^\kappa$$

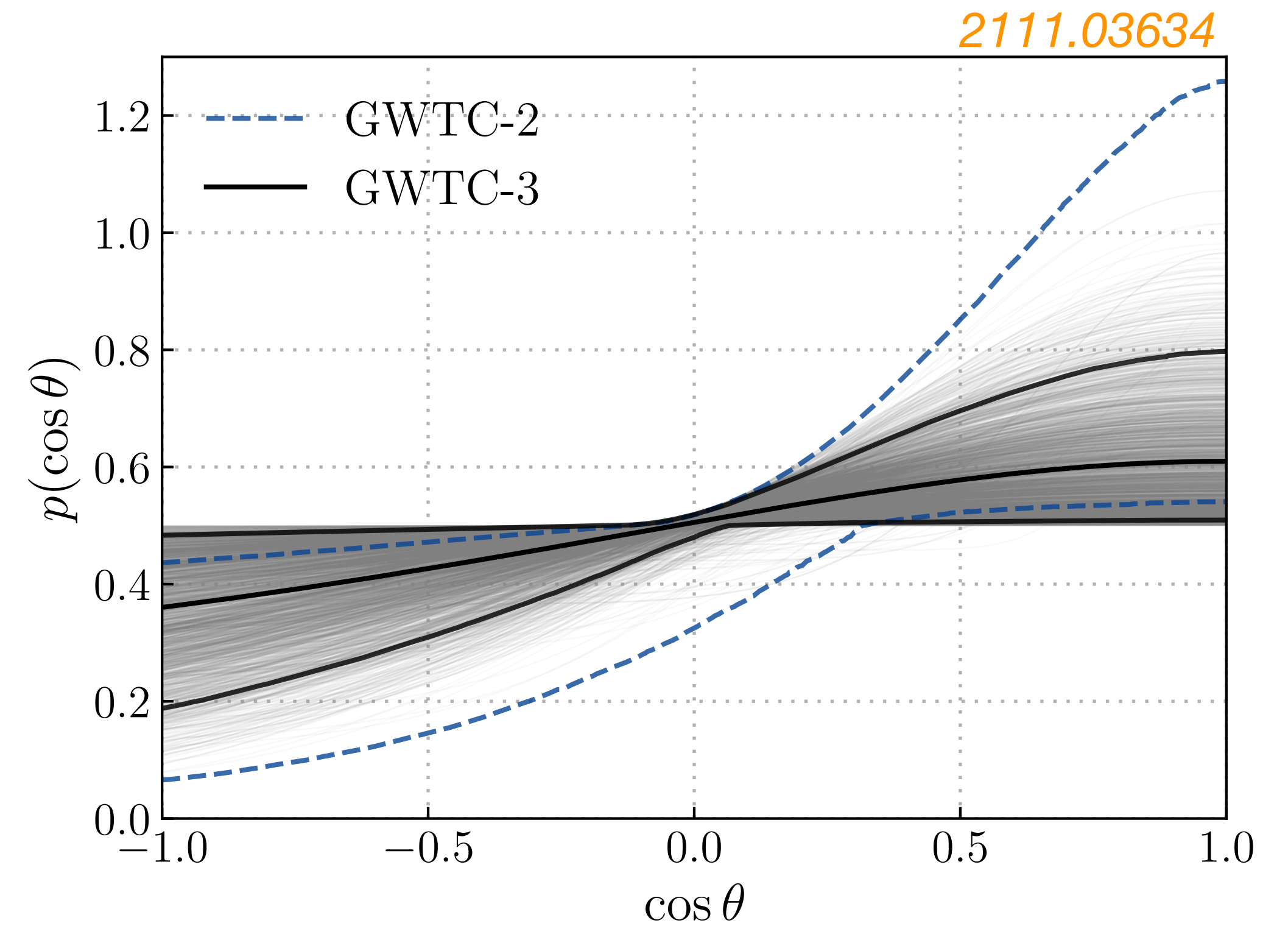
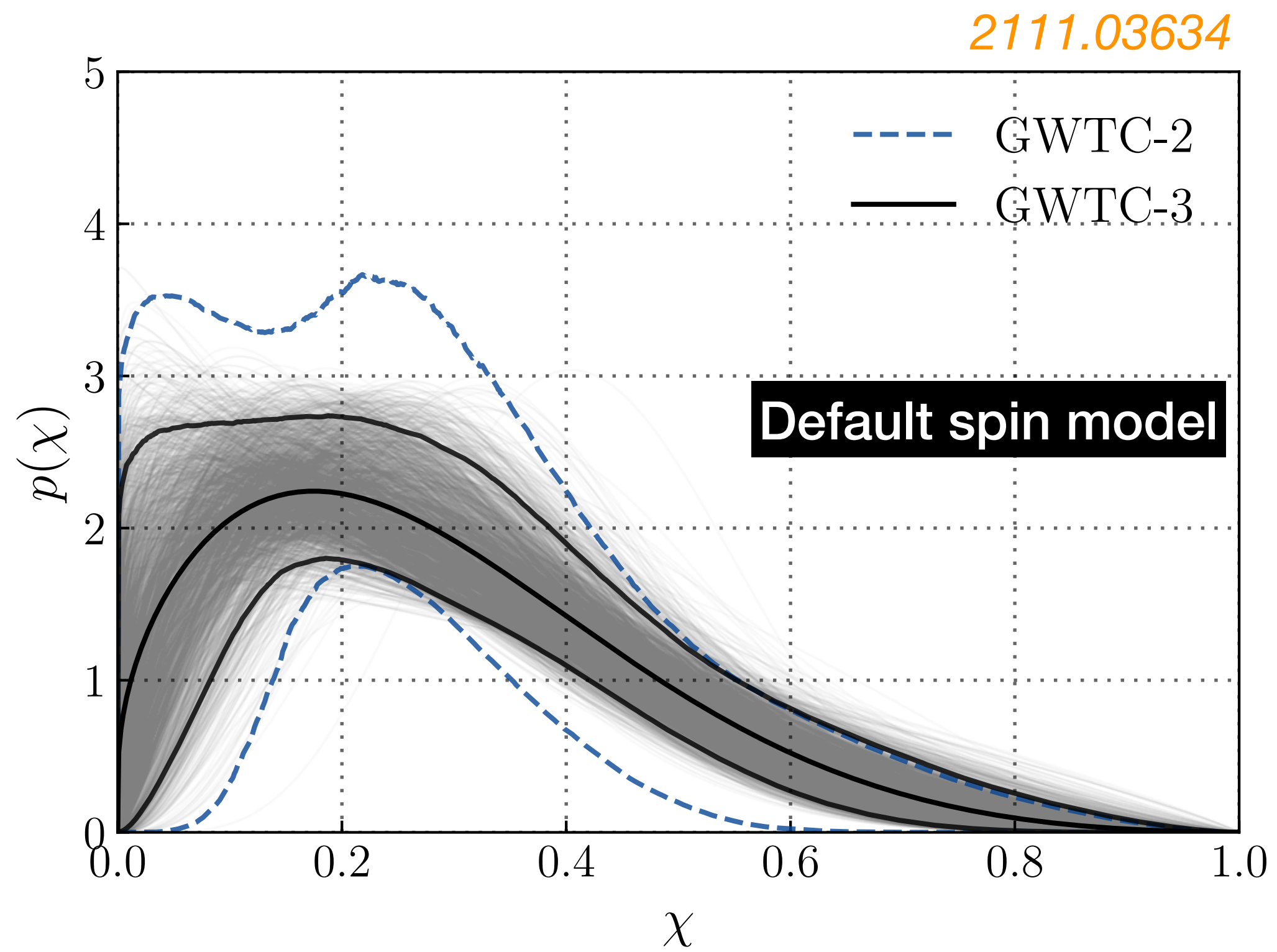
- Initially there was a preference for a rate that increased with redshift but still consistent with a non-evolving merger rate
- But with GWTC-3 we are confident that BBH rate is evolving with redshift



Spin distribution in BBHs

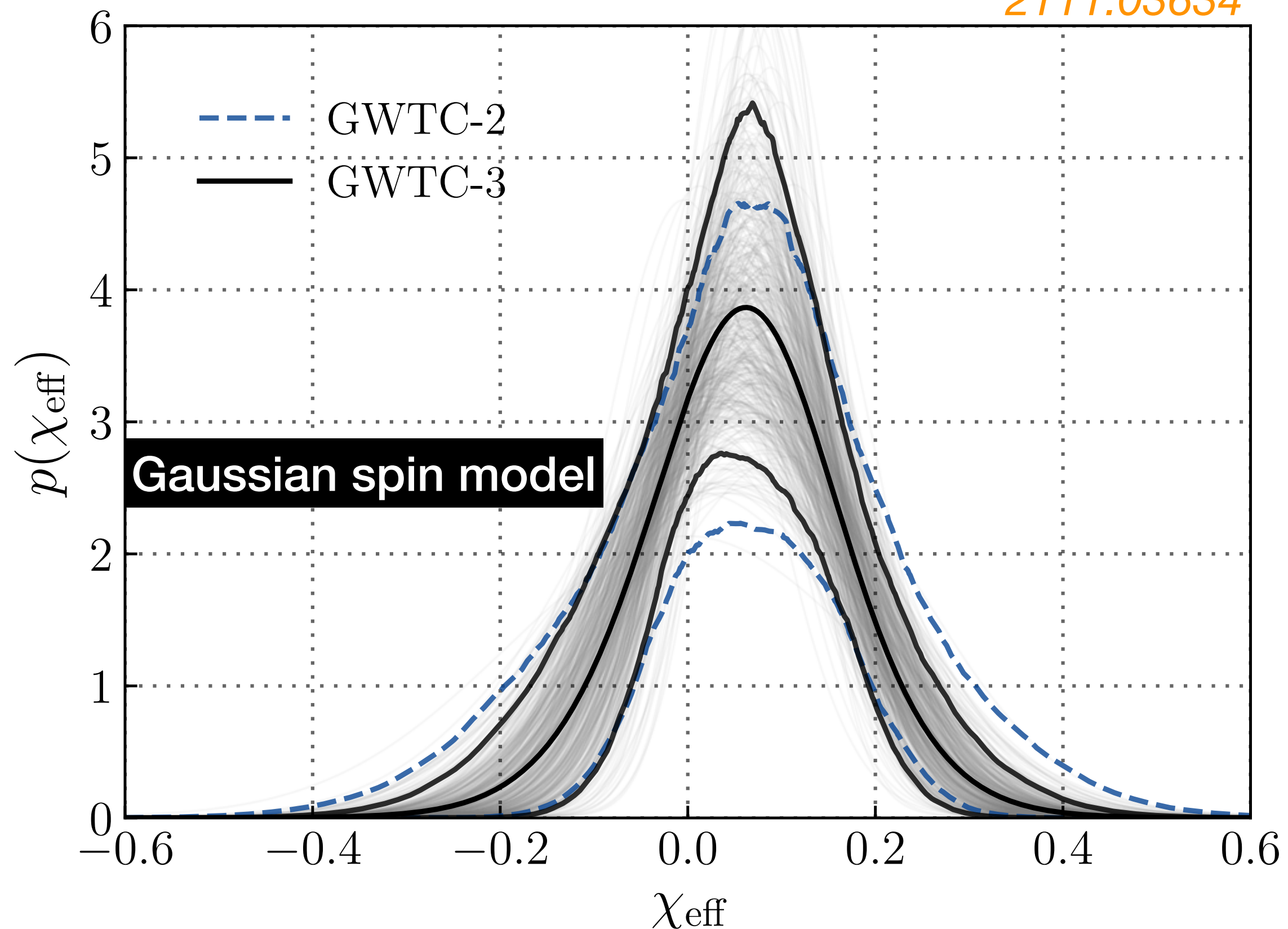
BBH spin distribution is consistent with GWTC-2



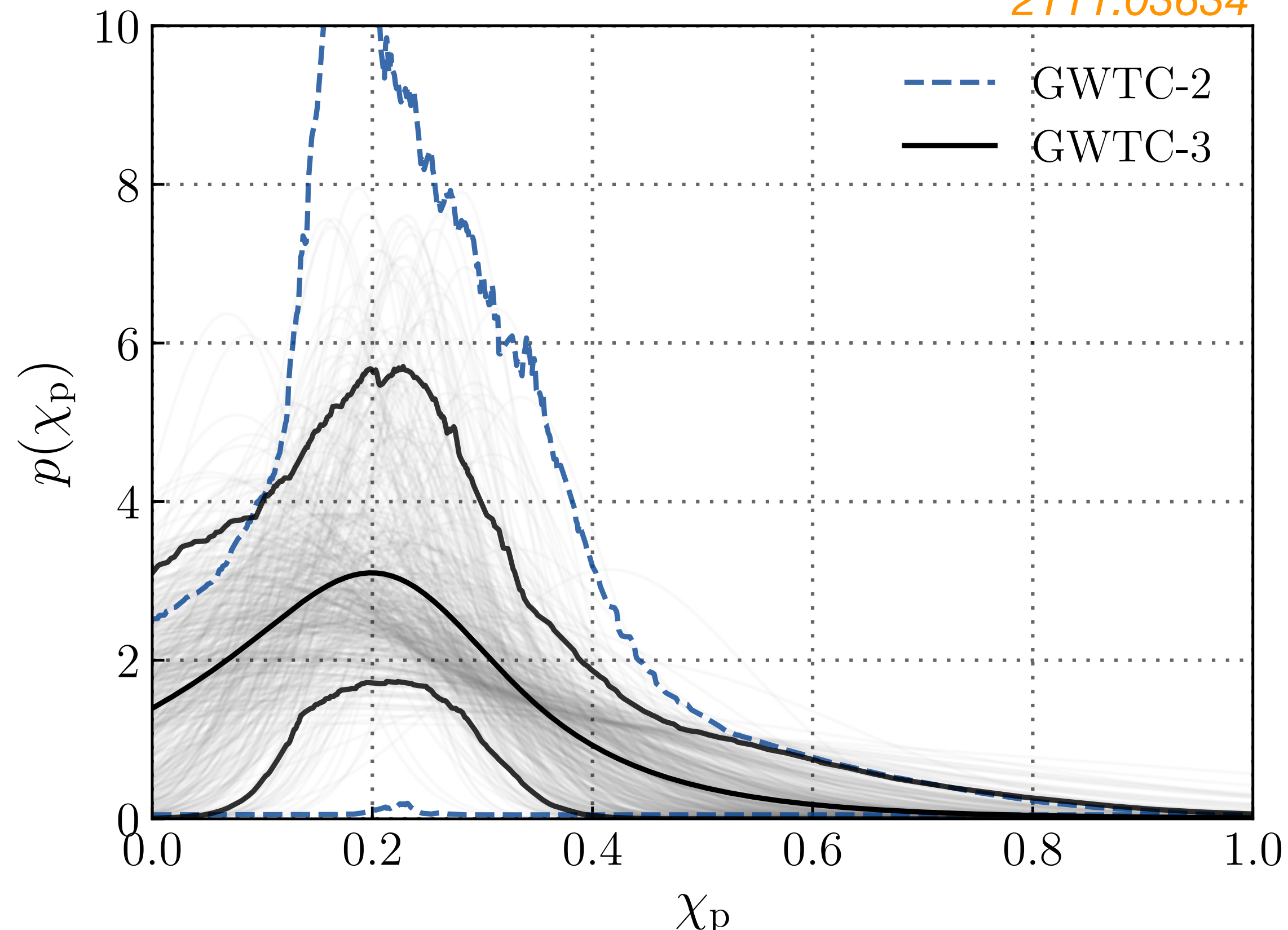


Again excluded the case of perfect spin-orbit alignment and now data strongly favor a broad or isotropic distribution of spin tilts

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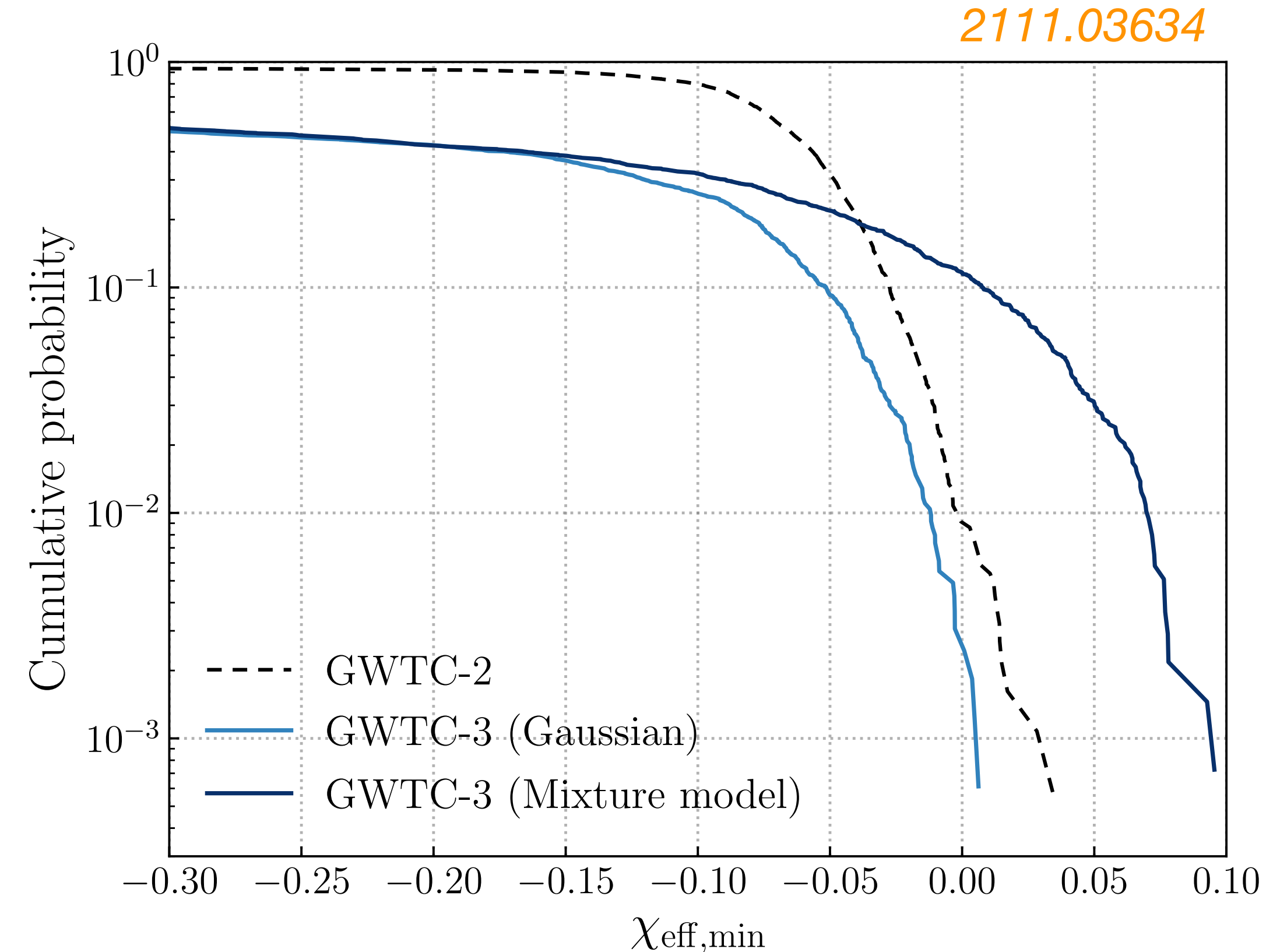
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- As with GWTC-2 we again infer a χ_{eff} distribution compatible with small but non-vanishing spins, with a mean centered at $0.06^{+0.04}_{-0.05}$
- χ_p measurements can be explained either by a broad distribution centered at $\chi_p = 0$, or a narrow distribution centered at $\chi_p \approx 0.2$

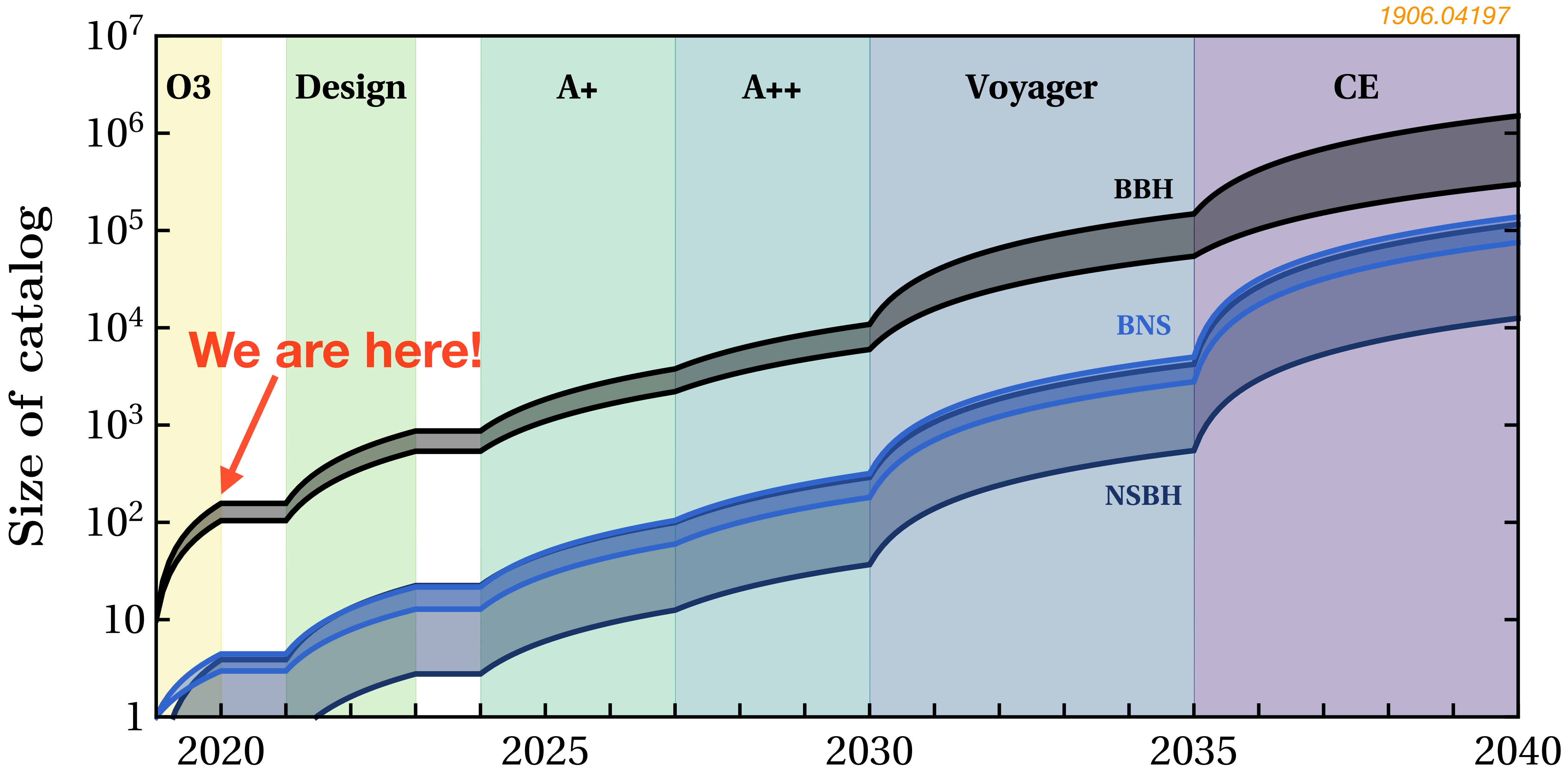
Evidence of extreme spin-orbit misalignment

- Spin tilts $> 90^\circ$ unlikely for BBH formation from isolated stellar progenitors (Kalogera, 2000)
- $\chi_{\text{eff}} < 0$ would serve as a strong indicator of dynamical interaction during BBH evolution
- Extended the Gaussian model to truncate χ_{eff} on the range $\chi_{\text{eff,min}} \leq \chi_{\text{eff}} \leq 1$ (rather than $-1 \leq \chi_{\text{eff}} \leq 1$) and hierarchically measured $\chi_{\text{eff,min}}$
- $\chi_{\text{eff,min}} < 0$ at 99.8% credibility
- There were objection that unless BBH spin models are expanded to allow the existence of a secondary subpopulation with vanishingly small spins and spins allowed to correlate with other BBH parameters like the mass ratio
- Repeat the inference of $\chi_{\text{eff,min}}$ but under an expanded model that allows for a narrow subpopulation of BBHs with extremely small χ_{eff}
- Data still prefer a negative $\chi_{\text{eff,min}}$ but with lower significance, $\chi_{\text{eff,min}} < 0$ at 88.4% credibility



Summary

- Mass and spin distributions are consistent with GWTC-2
- More BBHs with preferentially negatively aligned spins but it could be by chance as well
- The BBH merger rate density increases with redshift
- A relative dearth of observations with component masses between 3 and 5 M_{\odot}
- No strong evidence for lower and higher mass gaps
- The inferred NS mass distribution, albeit based on a limited sample of observations, does not exhibit a peak at 1.35 M_{\odot}
- GW190814 is an outlier for the secondary mass of BNS/NSBH and BBH population



- LIGO-Virgo-KAGRA

- Stellar mass NS/BH merger up to redshift $z \sim 1$

- 2G: Voyager (Livingston, Hanford, Pisa, Hingoli, Kamioka)

- 4-5 times better sensitivity, detections up to redshift $z \sim 10$

- 3G: Einstein Telescope, Cosmic Explorer

- 20 times better sensitivity, detections up to redshift $z \sim 30$

- Other: LISA, TianQin, DECIGO, Pulsar Timing array

- Explore lower frequency regime and new sources



Loud Future for
GW science

Thank You!