

# ***Status of the Standard Model of Cosmology***

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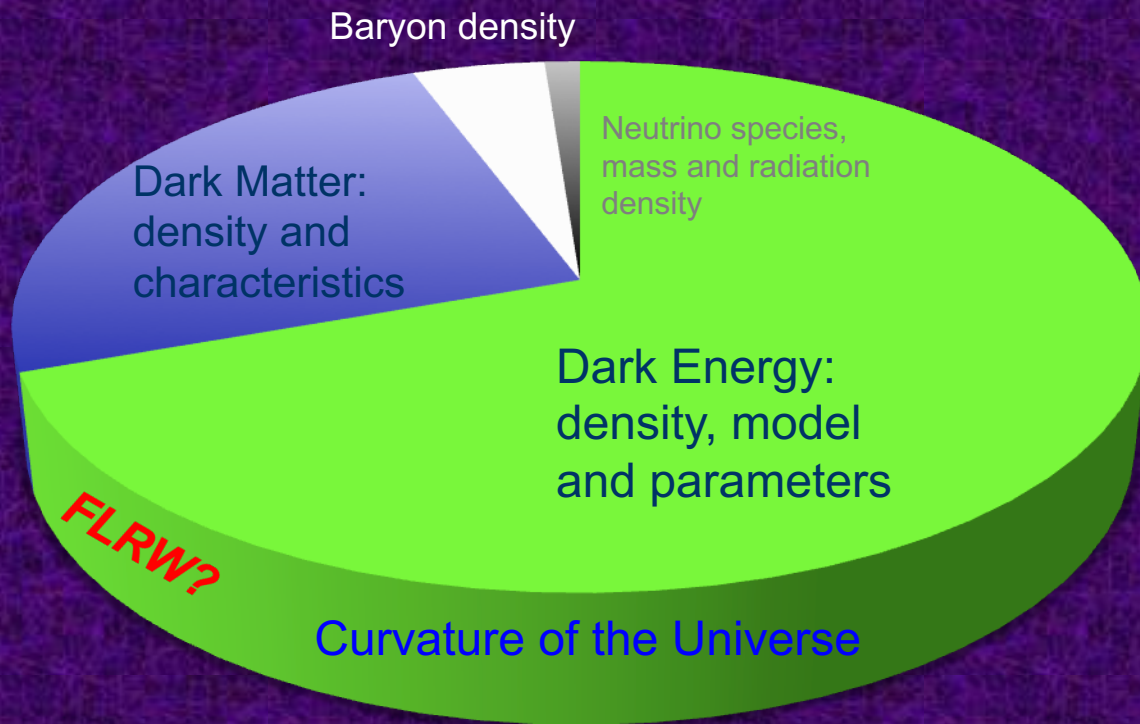
**University of Science and Technology (UST)**

**2 – 5 February 2022**

**Second Chennai Symposium on Gravitation and Cosmology**

# Era of Precision Cosmology

Combining theoretical works with new measurements and using statistical techniques to place sharp constraints on cosmological models and their parameters.



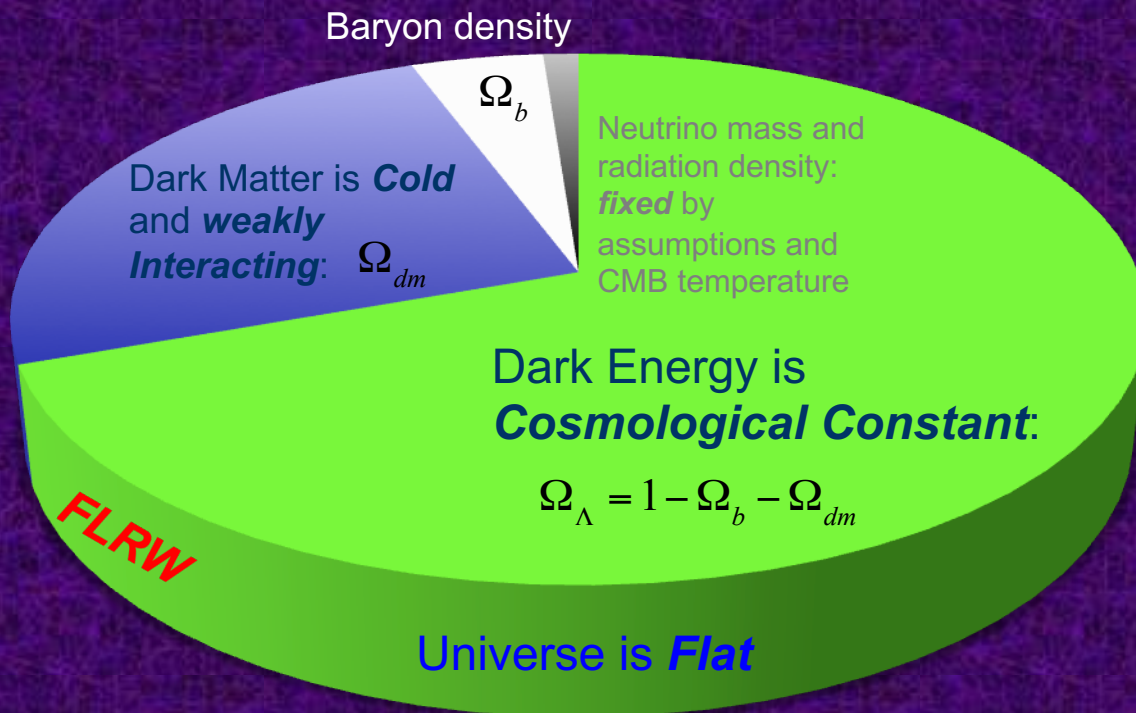
Initial Conditions:  
Form of the Primordial  
Spectrum and Model of  
Inflation and its Parameters

Epoch of reionization

Hubble Parameter and  
the Rate of Expansion

# Standard Model of Cosmology

Using measurements and statistical techniques to place sharp constraints on parameters of the standard cosmological model.



Initial Conditions:  
Form of the Primordial Spectrum is **Power-law**

$$n_s, A_s$$

Epoch of reionization

$$\tau$$

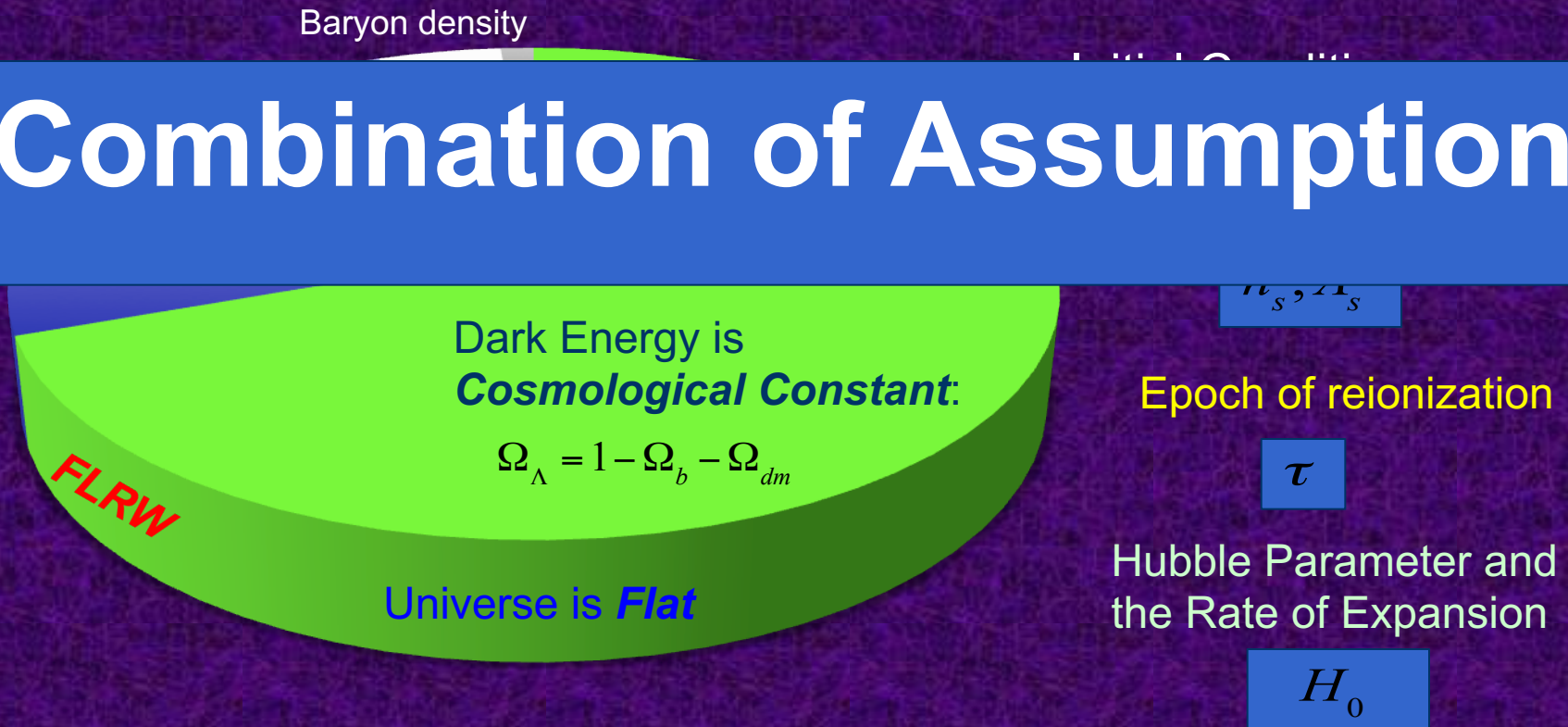
Hubble Parameter and the Rate of Expansion

$$H_0$$

# Standard Model of Cosmology

Using measurements and statistical techniques to place sharp constraints on parameters of the standard cosmological model.

## Combination of Assumptions



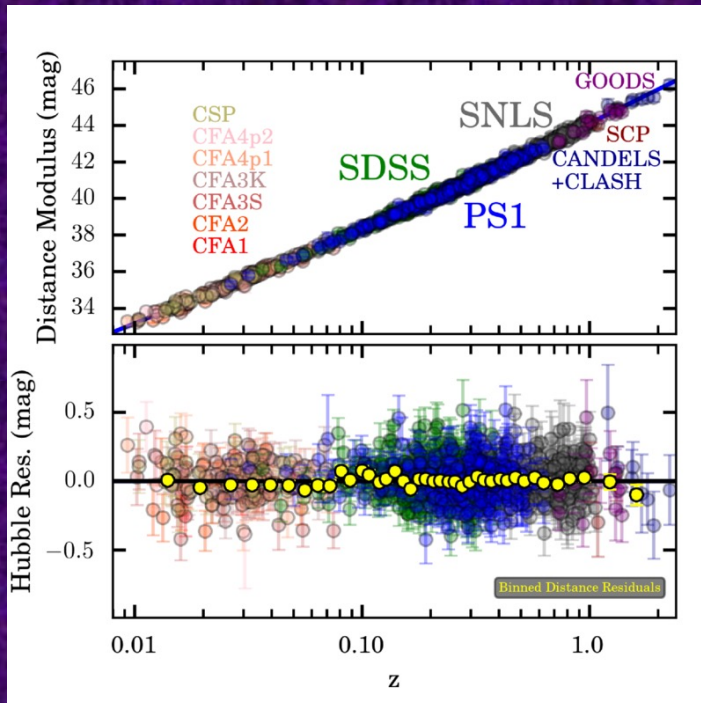


# Standard Model in 2022

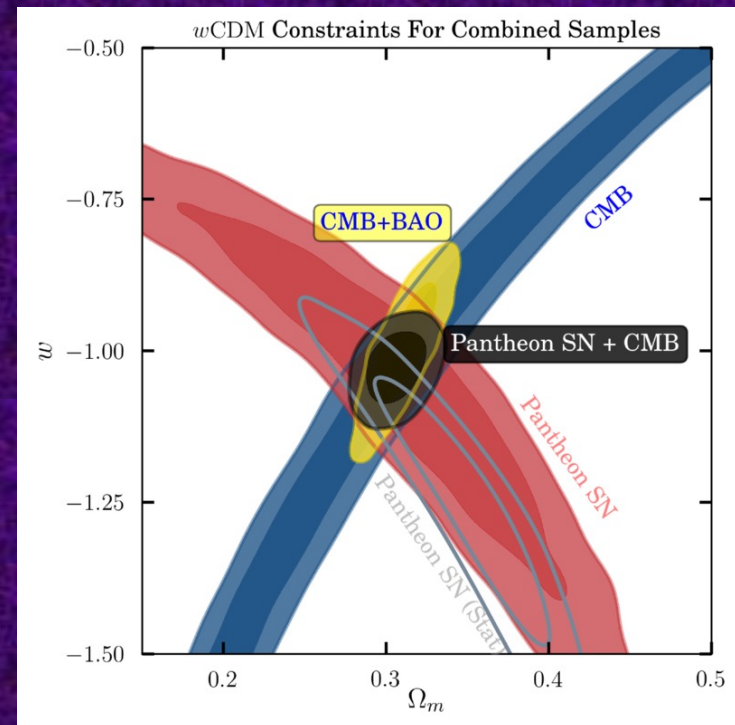
# SN Ia

**20 years after discovery of the acceleration of the universe:**

From 60 Supernovae Ia at cosmic distances, we now have ~1000 published distances, with better precision, better accuracy, out to  $z \sim 2.0$ . **Accelerating universe in proper concordance to the data.**



1048 spectroscopically confirmed SNIa



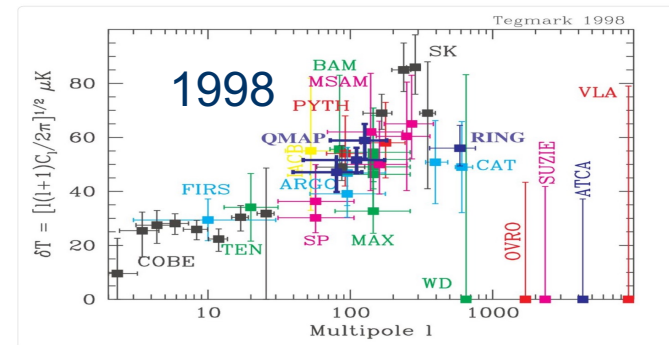
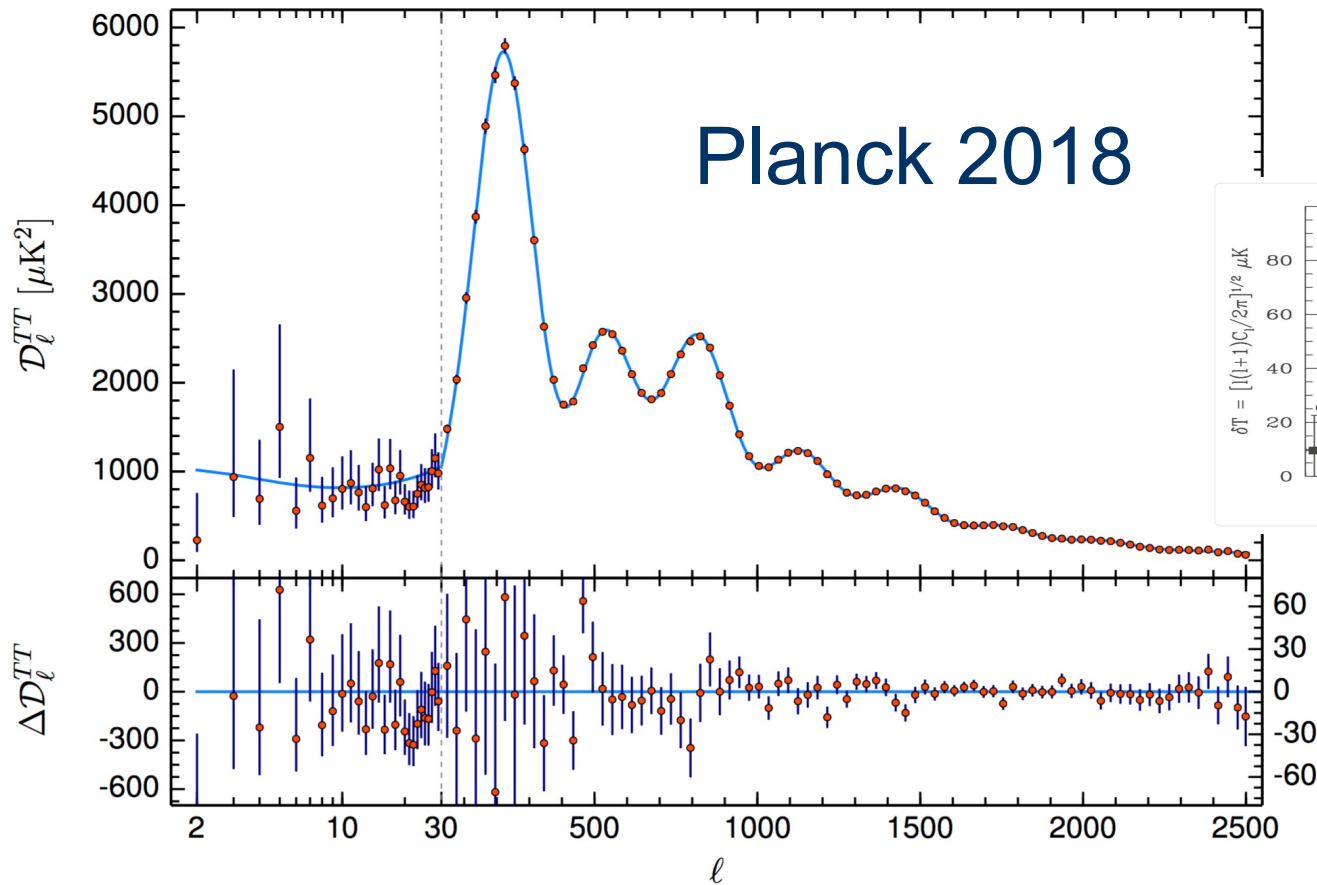
Pantheon Compilation  
Scolnic et al. (2018)

# Standard Model in 2022

# CMB

20 years after discovery of the acceleration of the universe:

**CMB directly points to acceleration.** Didn't even have acoustic peak in 1998!



# Standard Model in 2022

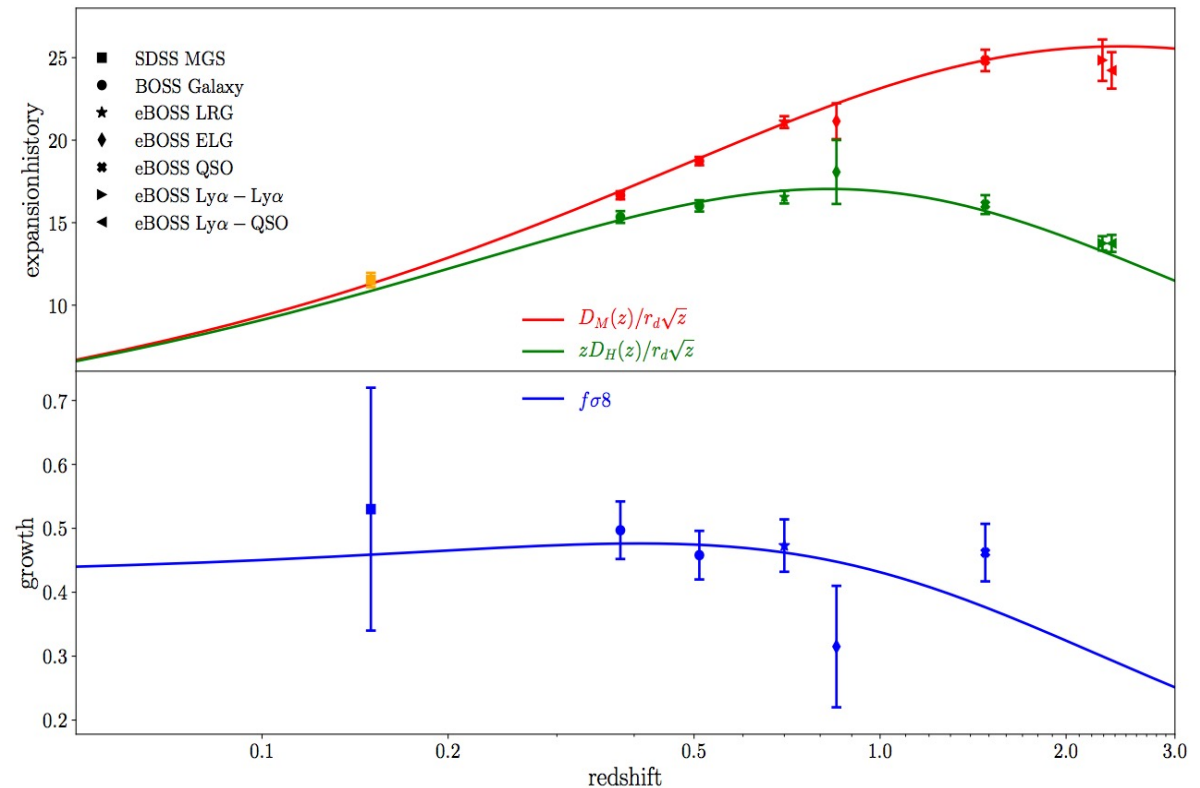
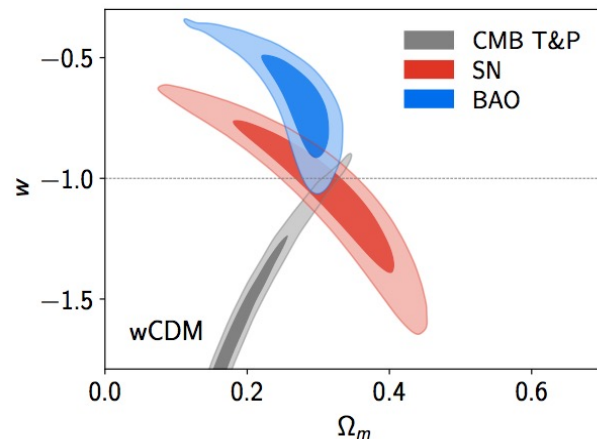
# LSS

**20 years after discovery of the acceleration of the universe:**

Large Scale Structure data is consistent with the standard model including Lambda dark energy and GR.

SDSS IV - eBOSS  
Final Cosmology  
Results




arXiv:2007.08991





# SDSS IV: Largest 3D Map of the Universe Ever Created

CNN World Africa Americas Asia Australia China Europe India Middle East United Kingdom

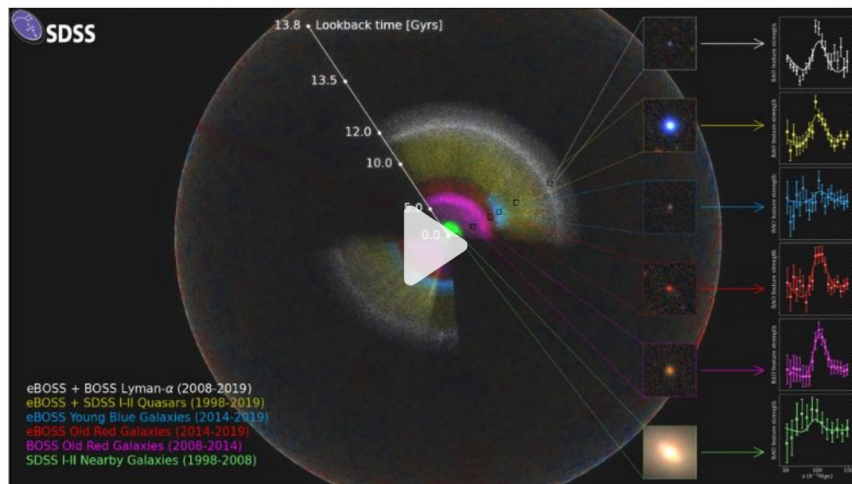
Edition   

## 11 billion years of history in one map: Astrophysicists reveal largest 3D model of the universe ever created



By **Joshua Berlinger** and **Jessie Yeung**, CNN

Updated 1748 GMT (0148 HKT) July 22, 2020



See a 3D model of the universe 01:17

**(CNN)** — A global consortium of astrophysicists have created the world's largest three-dimensional map of the universe, a project 20 years in the making that researchers say helps better explain the history of the cosmos.

### News & buzz



'Black Is King': Beyoncé's visual album is a feast of fashion...



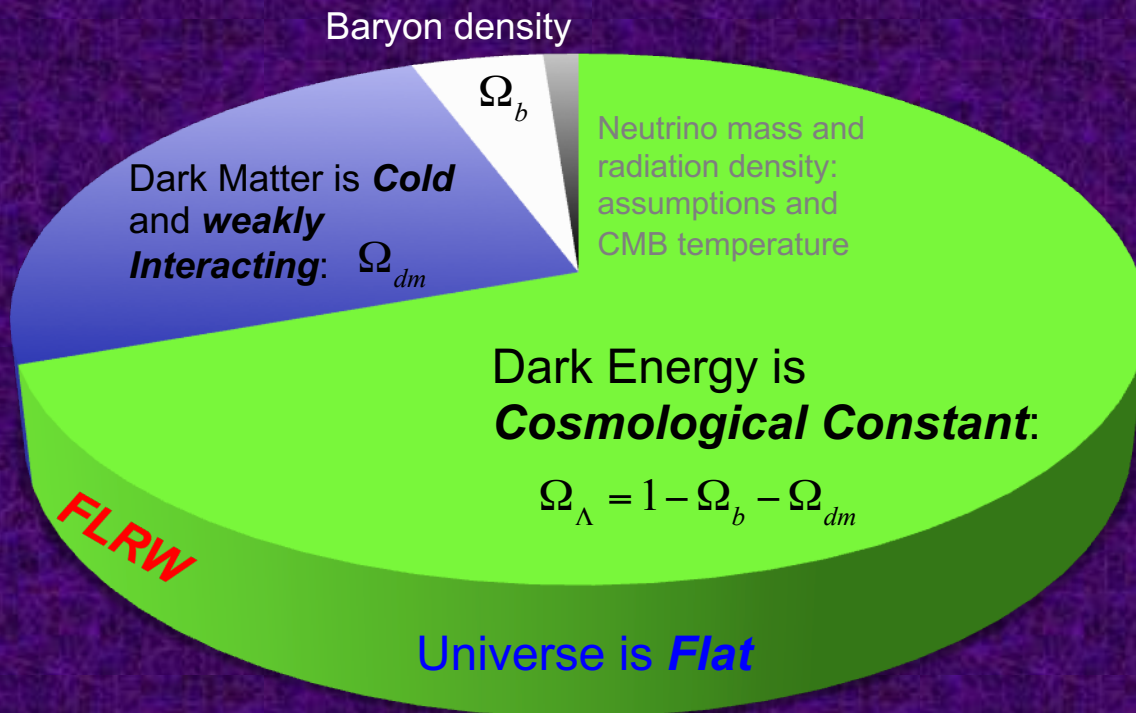
What you need to know about coronavirus on Friday, July 31

Ad closed by Google



# Standard Model of Cosmology

combination of *reasonable* assumptions, but.....



Initial Conditions:  
Form of the Primordial Spectrum is **Power-law**

$$n_s, A_s$$

Epoch of reionization

$$\tau$$

Hubble Parameter and the Rate of Expansion

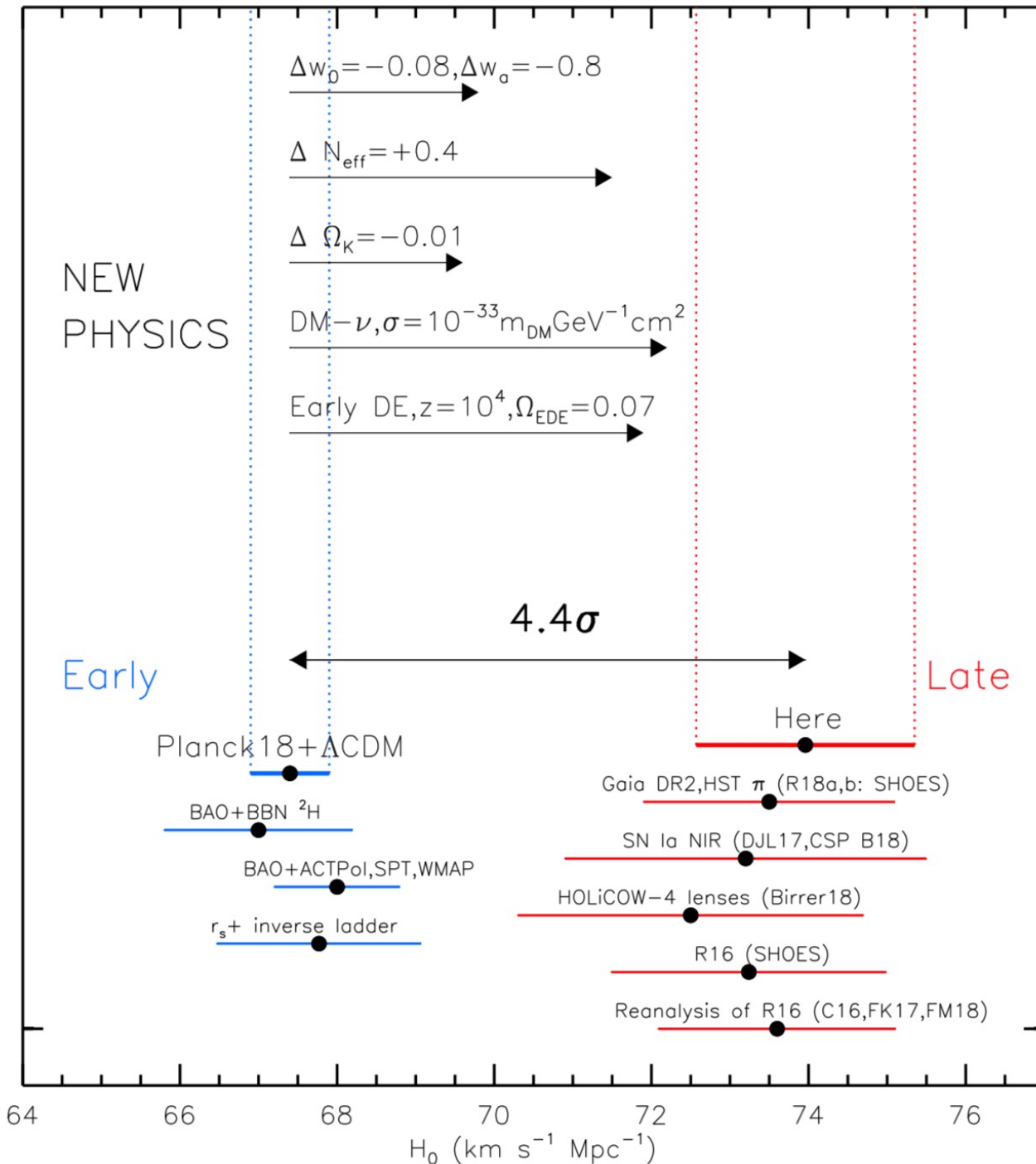
$$H_0$$

# Persistent Tensions in the Standard Model



*Local estimation of the Hubble constant seems to be substantially higher than the expected values fitting the standard  $\Lambda$ CDM model to CMB or LSS.*

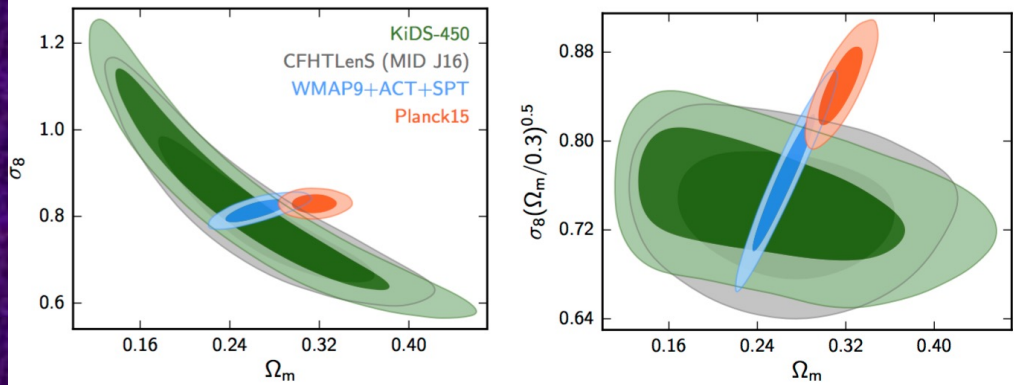
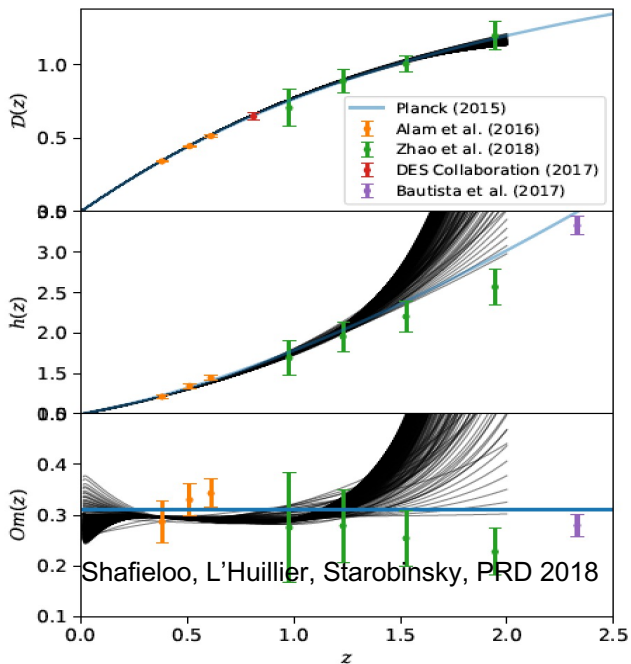
***67 or 74?***



## Tensions in the Standard Model

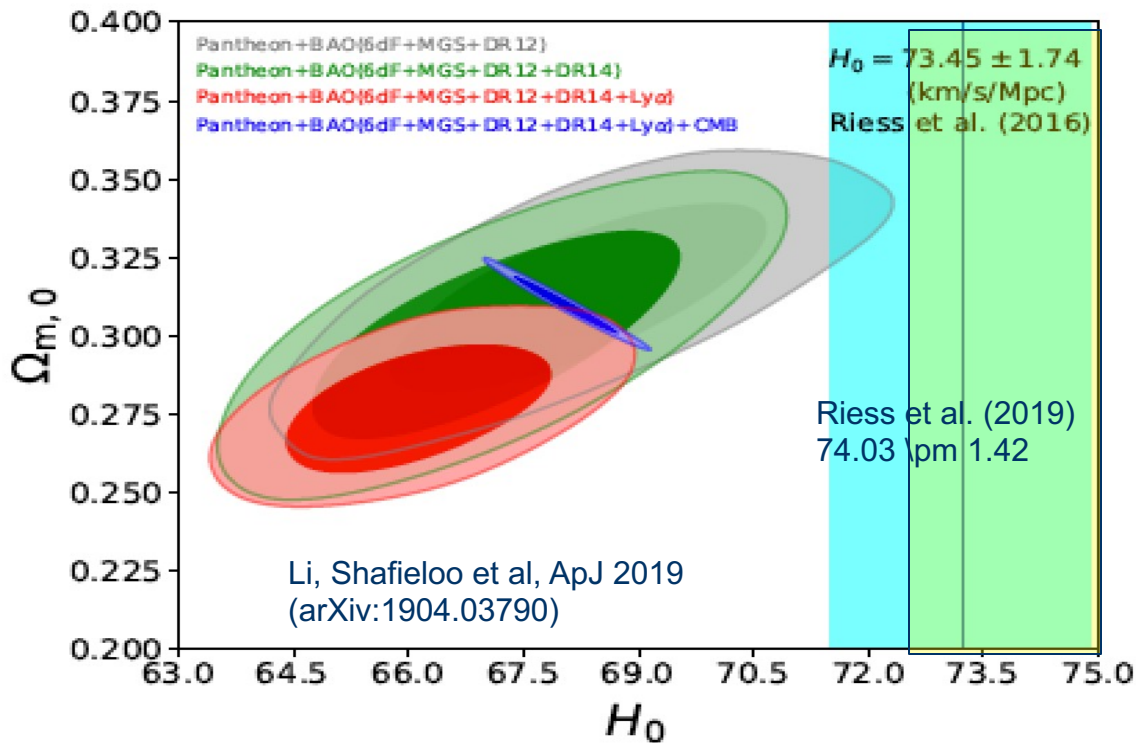
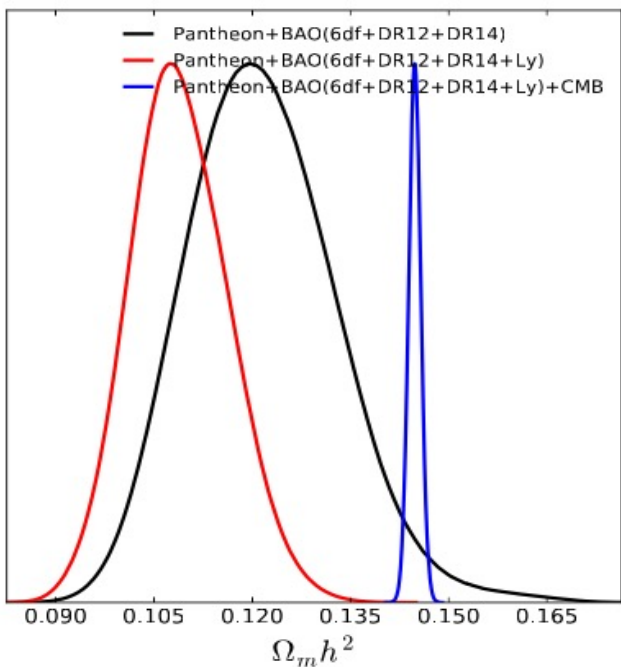
Riess et al,  
arXiv:1903.07603



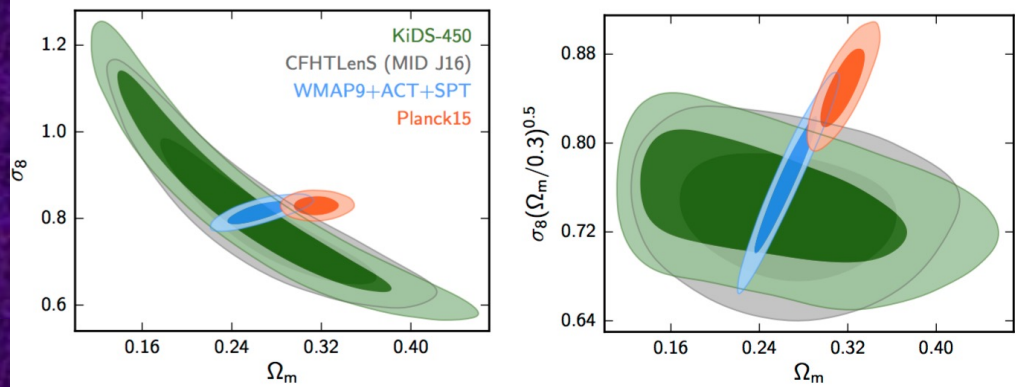
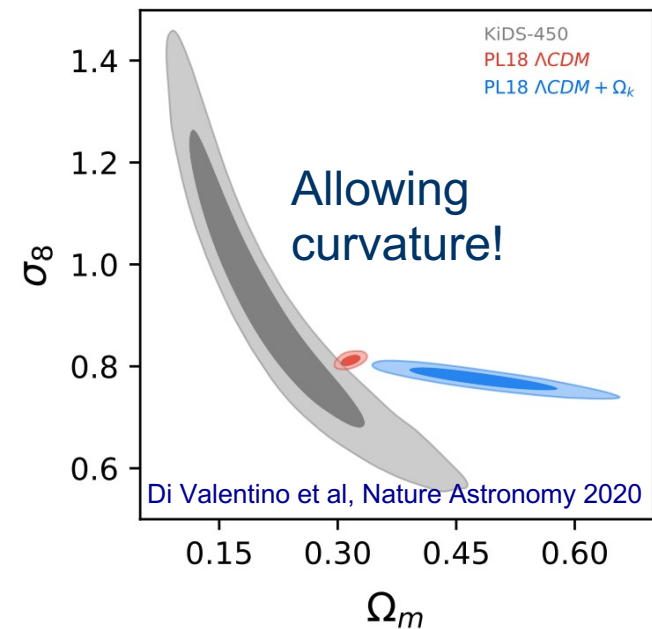


Hildebrandt et al, MNRAS 2017

**It is not only about  $H_0$  and CMB.** Low  $H(z)r_d$  is suggested by BAO and low matter density by WL.

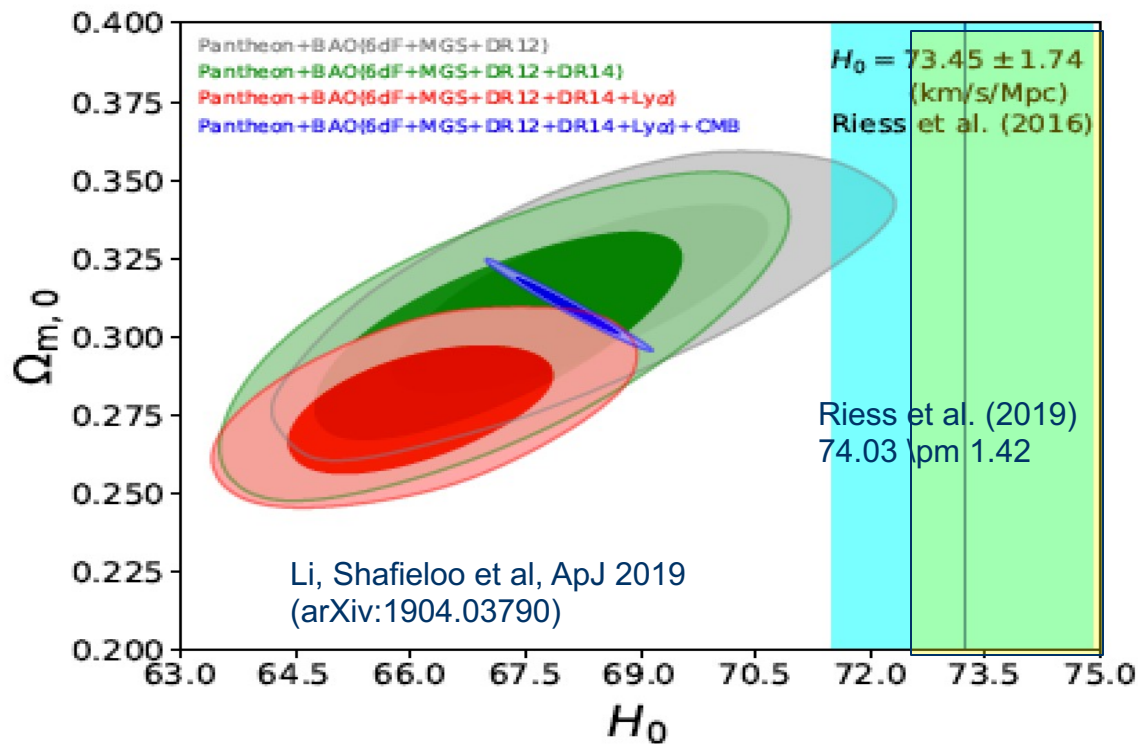
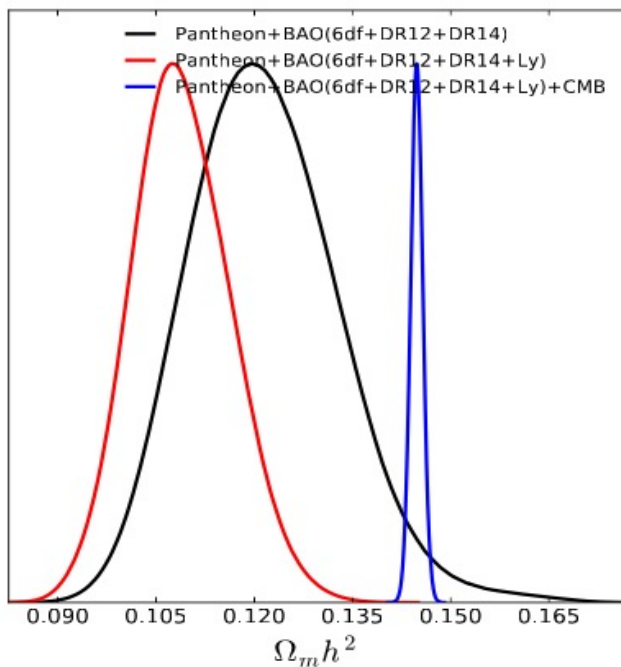






Hildebrandt et al, MNRAS 2017

**It is not only about  $H_0$  and CMB.** Low  $H(z)r_d$  is suggested by BAO and low matter density by WL.



# How to go **beyond** the standard model of cosmology?



- Finding features/deviations in the data beyond the flexibility of the standard model using model-independent reconstructions.

- Falsifying the standard model using litmus tests.

- Finding tension among different independent data assuming the standard model (making sure there is no systematic).

- Introducing theoretical/phenomenological models that can explain the data better (**statistically significant**) than the standard model.

# 2014

# Om<sub>h</sub>2

Important discovery if no systematic in the SDSS Quasar BAO data

## Model Independent Evidence for Dark Energy Evolution from Baryon Acoustic Oscillation

$$Om_{h2}(z_1, z_2) = \frac{H^2(z_2) - H^2(z_1)}{(1+z_2)^3 - (1+z_1)^3} = \Omega_{0m} H_0^2$$

Only for Flat LCDM

Sahni, Shafieloo, Starobinsky, ApJ Lett 2014

$$Om_{h2} = 0.1426 \pm 0.0025$$

LCDM+Planck  
k+WP

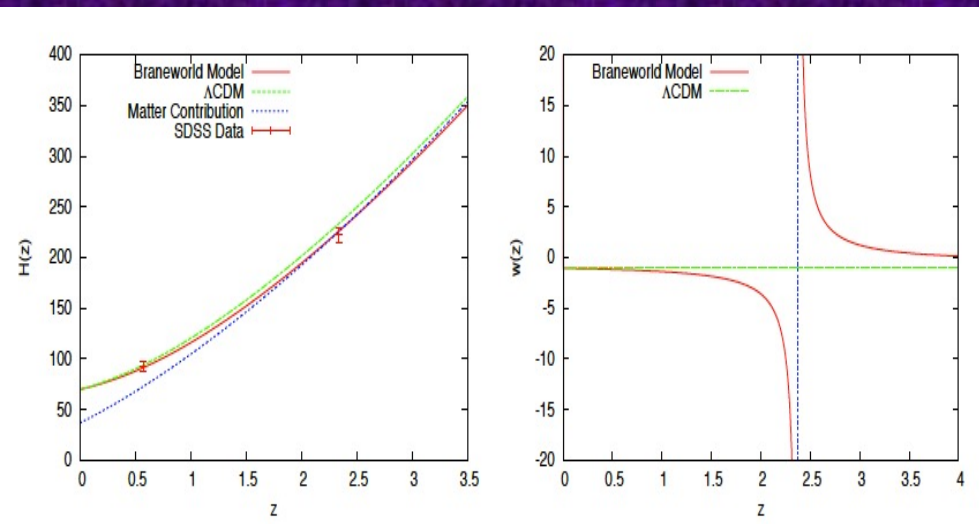
$$Om_{h2}(z_1; z_2) = 0.124 \pm 0.045$$

$$Om_{h2}(z_1; z_3) = 0.122 \pm 0.010$$

$$Om_{h2}(z_2; z_3) = 0.122 \pm 0.012$$

BAO+H0

H(z = 0.00) = 70.6 ± 3.3 km/sec/Mpc  
 H(z = 0.57) = 92.4 ± 4.5 km/sec/Mpc  
 H(z = 2.34) = 222.0 ± 7.0 km/sec/Mpc





# 2021

# Om<sub>h</sub>2

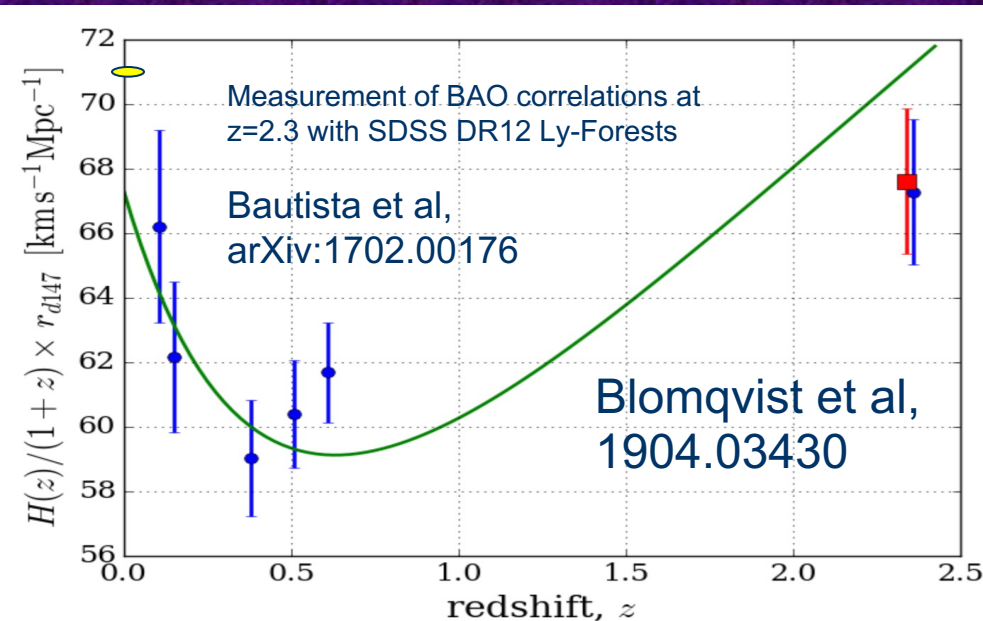
No systematic yet found,

## Model Independent Evidence for Dark Energy Evolution from Baryon Acoustic Oscillation

$$Om_{h2}(z_1, z_2) = \frac{H^2(z_2) - H^2(z_1)}{(1+z_2)^3 - (1+z_1)^3} = \Omega_{0m} H_0^2$$

Only for LCDM

Sahni, Shafieloo, Starobinsky, ApJ Lett 2014



$$Om_{h2} = 0.1426 \pm 0.0025$$

LCDM+Planck  
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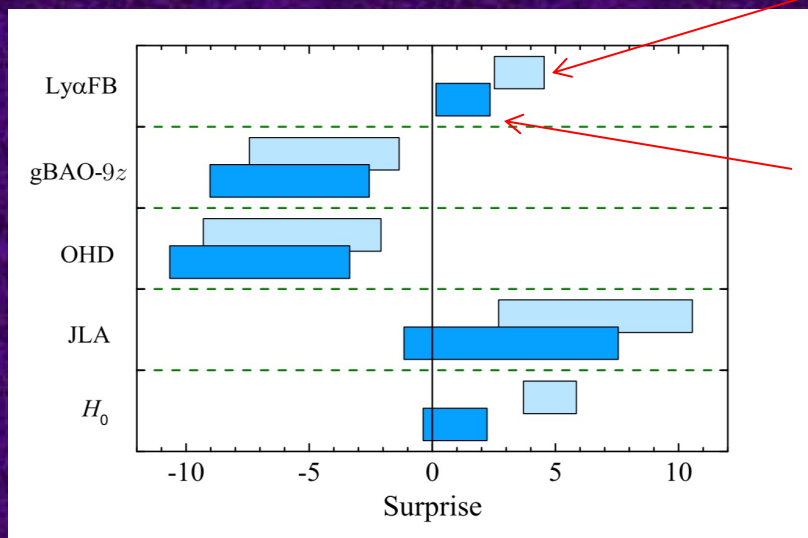
$$H(z = 2.34) = 222.0 \pm 7.0 \text{ km/sec/Mpc}$$



# Comparing different data assuming a particular model

Zhao et al, Nature Astronomy, 2017

$$T \equiv \frac{S}{\Sigma} = \frac{(\theta_1 - \theta_2)^T \mathcal{C}_1^{-1} (\theta_1 - \theta_2) - \text{Tr}(\mathcal{C}_2 \mathcal{C}_1^{-1} + \mathbb{I})}{\sqrt{\text{Tr}(\mathcal{C}_2 \mathcal{C}_1^{-1} + \mathbb{I})^2}},$$



LCDM

w(z)CDM

Acronym	Meaning	References
P15	The <i>Planck</i> 2015 CMB power spectra	[6]
JLA	The JLA supernovae	[28]
6dF	The 6dFRS (6dF) BAO	[29]
MGS	The SDSS main galaxy sample BAO	[30]
$P(k)$	The WiggleZ galaxy power spectra	[31]
WL	The CFHTLenS weak lensing	[32]
$H_0$	The Hubble constant measurement	[10]
OHD	$H(z)$ from galaxy age measurements	[33]
gBAO-3z	3-bin BAO from BOSS DR12 galaxies	[34]
gBAO-9z	9-bin BAO from BOSS DR12 galaxies	[35, 36]
Ly $\alpha$ FB	The Ly $\alpha$ forest BAO measurements	[2, 9]
B	P15 + JLA + 6dF + MGS	
ALL12	The combined dataset used in [27]	
ALL16-3z	B + $P(k)$ + WL + $H_0$ + OHD + gBAO-3z + Ly $\alpha$ FB	
ALL16	B + $P(k)$ + WL + $H_0$ + OHD + gBAO-9z + Ly $\alpha$ FB	
DESI++	P15 + mock DESI BAO [49] + mock SN [50]	

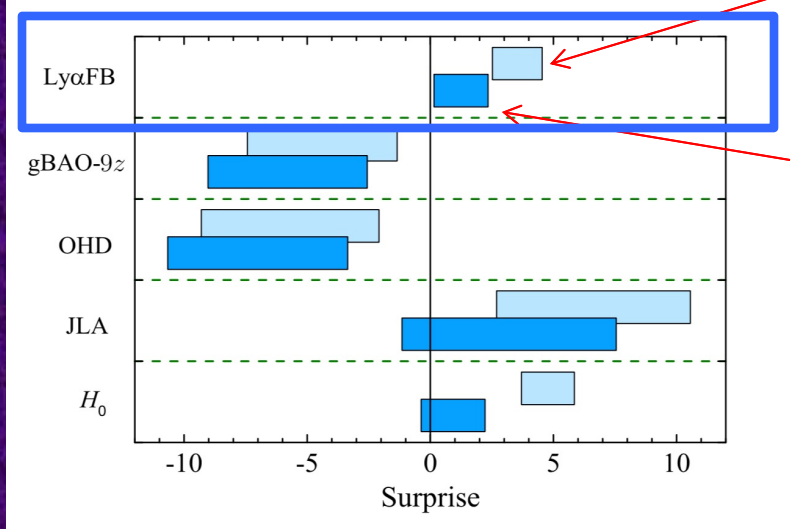
Kullback-Leibler (KL) divergence to quantify the degree of tension between different datasets assuming a model.

For LCDM;  $H_0$ , LyFB and JLA measurements are in tension with the combined dataset, with tension values of  $T = 4.4, 3.5, 1.7$ .

# Comparing different data assuming a particular model

Zhao et al, Nature Astronomy, 2017

$$T \equiv \frac{S}{\Sigma} = \frac{(\theta_1 - \theta_2)^T C_1^{-1} (\theta_1 - \theta_2) - \text{Tr}(C_2 C_1^{-1} + \mathbb{I})}{\sqrt{\text{Tr}(C_2 C_1^{-1} + \mathbb{I})^2}},$$



Bautista et al, [1702.00176]  
Blomqvist et al, [1904.03430]

Found no systematic/mistake in the previous measurement

Dataset	Description	Reference
gBAO-3z	3-bin BAO from BOSS DR12 galaxies	[34]
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ALL16	B+P(k)+WL+H <sub>0</sub> +OHD+gBAO-9z+LyαFB	
DESI++	P15 + mock DESI BAO [49] + mock SN [50]	

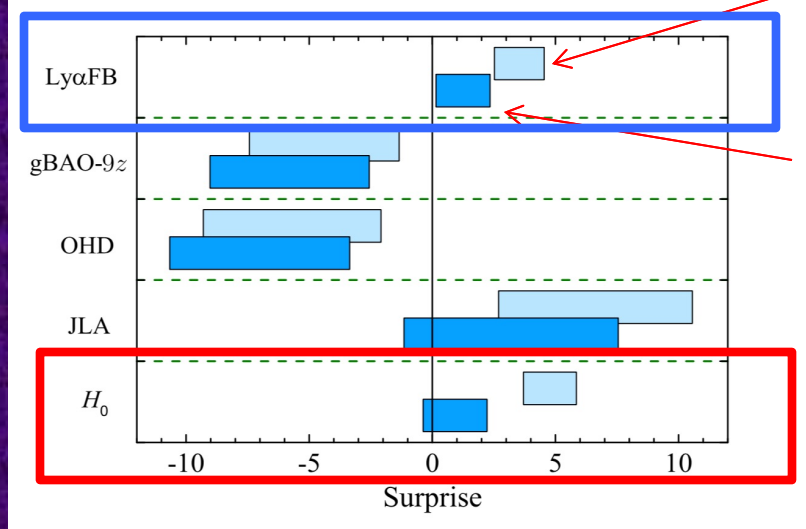
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Kullback-Leibler (KL) divergence to quantify the degree of tension between different datasets assuming a model.

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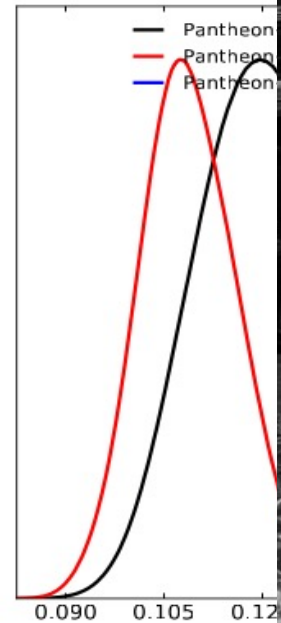
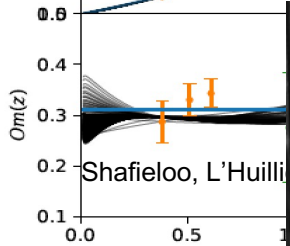
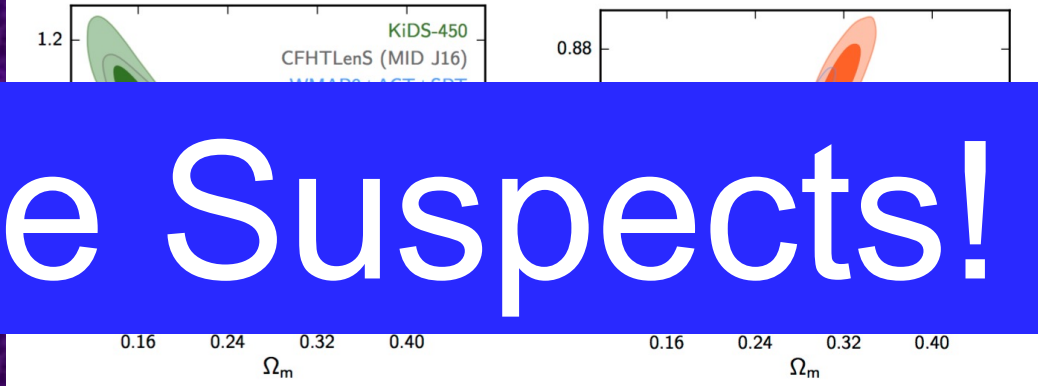
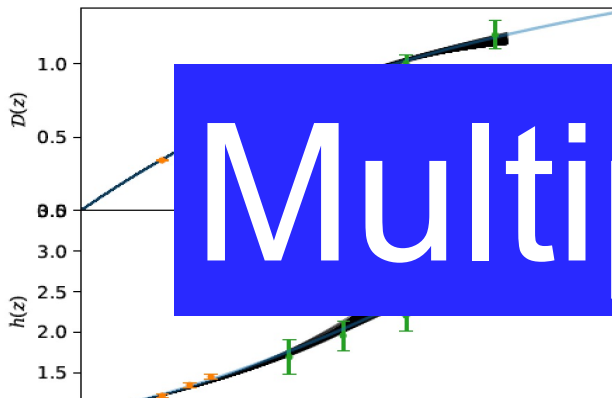
Follin & Knox [1707.01175]  
Zhang et al, [1706.07573]

Both agrees with Riess et al 2016 H<sub>0</sub> measurement

New H<sub>0</sub> measurement Riess et al 2019  
**(situation has become worse)**



# Multiple Suspects!



And Then There Were None (1945),  
Rene Clair [Based on a novel by Agatha Christie]

with  $H(z)r_d$  is  
by WL.

$3.45 \pm 1.74$   
km/s/Mpc  
et al. (2016)

et al. (2019)  
from 1.42

73.5 75.0



# How to resolve the tensions?



- **Statistical fluctuations** (*probably not anymore, some tensions are at high significance*)
- **Systematic in one or some of the data?** [Highly possible considering complications of the tensions that all cannot be resolved by minimal modifications.]

(Li, Shafieloo, Sahni, Starobinsky, ApJ 2019)

- **Extended models and/or new physics**

**Caution:** extended models with more degrees of freedom result to larger confidence contours which looks like there are better consistencies (more overlap between larger contours). [OK to do that but better to avoid over-selling!] *If current observations are reliable, most of these models will be ruled out by future observations. Central values matter!*

(Present)

## ***Standard Model of Cosmology***

Universe is Flat

Universe is Isotropic

Universe is Homogeneous

Dark Energy is Lambda ( $w=-1$ )

Power-Law primordial spectrum ( $n_s=\text{const}$ )

Dark Matter is cold

All within framework of FLRW

(Present)

## ***Standard Model of Cosmology***

Universe is Flat

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Power-Law primordial spectrum ( $n_s=\text{const}$ )

Dark Matter is cold

All within framework of FLRW

Does LCDM need  
modification?

Which part?



(Present)

## ***Standard Model of Cosmology***

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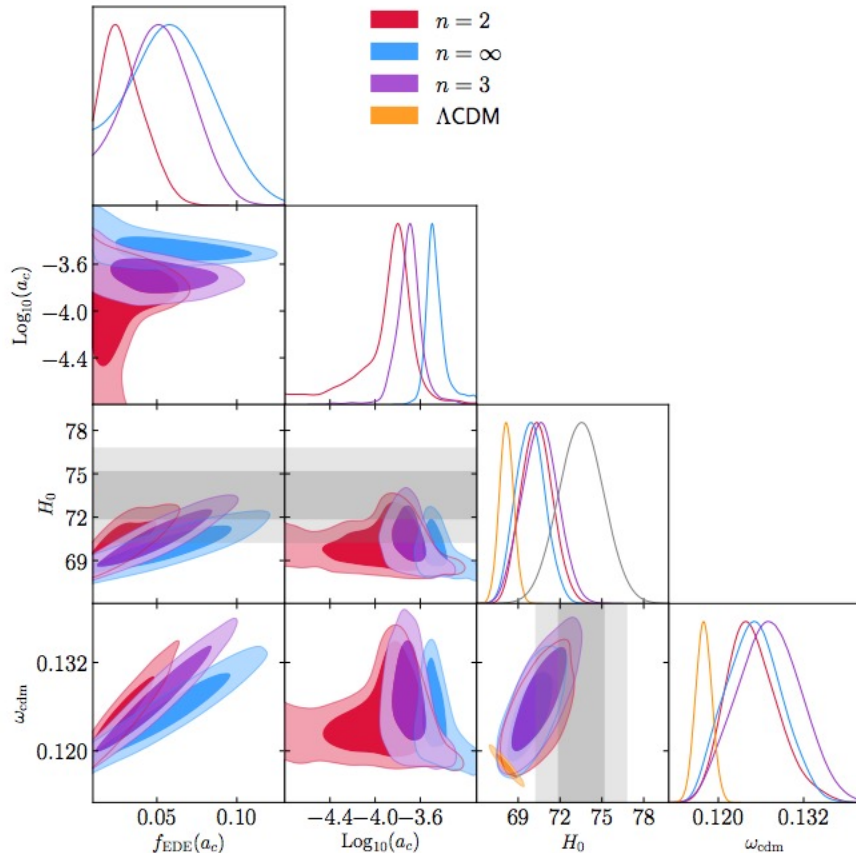
Example of an extended model:

# Early Dark Energy

$$r_d = \frac{c}{\sqrt{3}} \int_0^{1/(1+z_{\text{drag}})} \frac{da}{a^2 H(a) \sqrt{1 + \frac{3\Omega_b}{4\Omega_r} a}}$$

Decreasing  $r_d$  by having substantial early dark energy:

Allows having similar  $H_0 r_d$  with higher  $H_0$  [few extra dof]



$$\Omega_\varphi(a) = \frac{2\Omega_\varphi(a_c)}{(a/a_c)^{3(w_n+1)} + 1},$$

$$w_\varphi(z) = \frac{1 + w_n}{1 + (a_c/a)^{3(1+w_n)}} - 1.$$

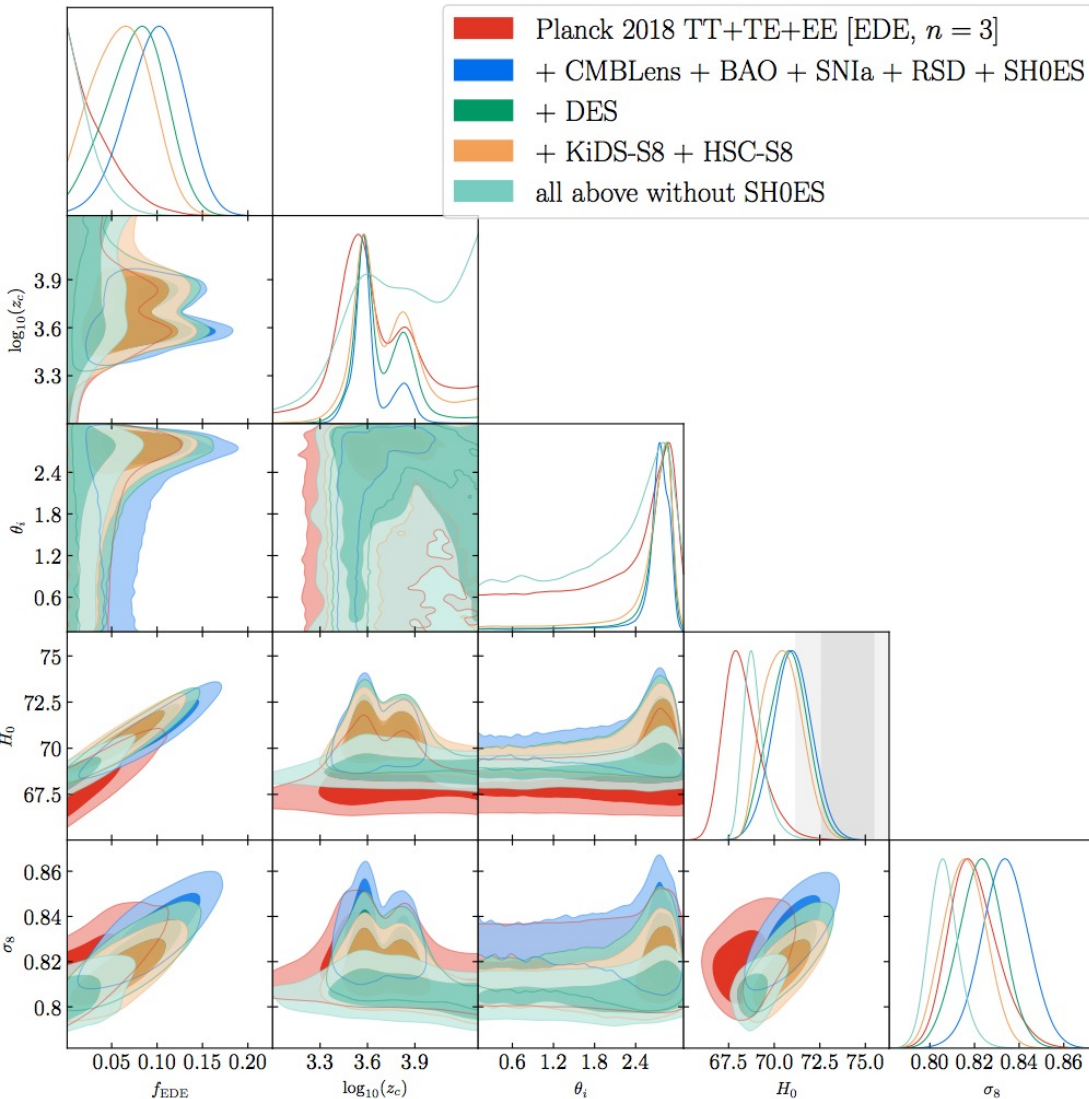
$$w_n = (n-1)/(n+1)$$

Poulin et al, Phys. Rev. Lett 2019

Example of an extended model:

# Early Dark Energy

**Tension is not really resolved.**



Constraints from *Planck* 2018 data only: TT+TE+EE

Parameter	$\Lambda$ CDM	EDE ( $n = 3$ )
$\ln(10^{10} A_s)$	$3.044 (3.055) \pm 0.016$	$3.051 (3.056) \pm 0.017$
$n_s$	$0.9645 (0.9659) \pm 0.0043$	$0.9702 (0.9769)_{-0.0069}^{+0.0071}$
$100\theta_s$	$1.04185 (1.04200) \pm 0.00029$	$1.04164 (1.04168) \pm 0.00034$
$\Omega_b h^2$	$0.02235 (0.02244) \pm 0.00015$	$0.02250 (0.02250) \pm 0.00020$
$\Omega_c h^2$	$0.1202 (0.1201) \pm 0.0013$	$0.1234 (0.1268)_{-0.0030}^{+0.0031}$
$\tau_{\text{reio}}$	$0.0541 (0.0587) \pm 0.0076$	$0.0549 (0.0539) \pm 0.0078$
$\log_{10}(z_c)$	—	$3.66 (3.75)_{-0.24}^{+0.28}$
$f_{\text{EDE}}$	—	$< 0.087 (0.068)$
$\theta_i$	—	$> 0.36 (2.96)$
$H_0$ [km/s/Mpc]	$67.29 (67.44) \pm 0.59$	$68.29 (69.13)_{-1.00}^{+1.02}$
$\Omega_m$	$0.3162 (0.3147) \pm 0.0083$	$0.3145 (0.3138) \pm 0.0086$
$\sigma_8$	$0.8114 (0.8156) \pm 0.0073$	$0.8198 (0.8280)_{-0.0107}^{+0.0109}$
$S_8$	$0.8331 (0.8355) \pm 0.0159$	$0.8393 (0.8468) \pm 0.0173$
$\log_{10}(f/\text{eV})$	—	$26.57 (26.36)_{-0.36}^{+0.39}$
$\log_{10}(m/\text{eV})$	—	$-26.94 (-26.90)_{-0.53}^{+0.58}$

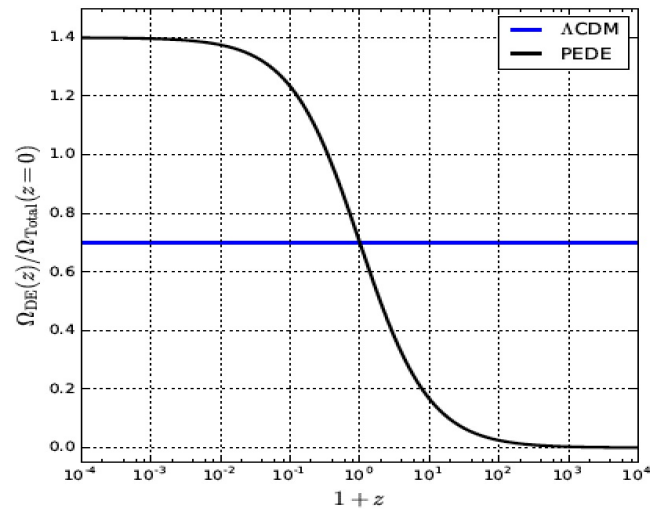
Hill et al, PRD 2020,  
arXiv:2003.07355



# Strategy

- Its always fun to do something exciting in physical cosmology. **Lets attempt to kill Lambda** by introducing a challenger.
- **One or some of the data might have systematics.** Investing on a model to fully satisfy all current observations and resolving all tensions might not be the best strategy.
- **Gambling is fun. I choose CMB and local H0 measurements** as two completely independent data that are showing most significant tensions within the framework of the LCDM as the main observations. The new model has to satisfy these two simultaneously.
- **I target the near future and not now.** If current data is reliable, the proposed model should decisively rule out Lambda with near future data that would have higher precision. The model should satisfy CMB and prefer high H0 (and not just being consistent with current estimations).
- It **should be simple phenomenological model, but better to have some hints for theory** or theoretical implications.

# Phenomenologically Emergent Dark Energy ( PEDE)

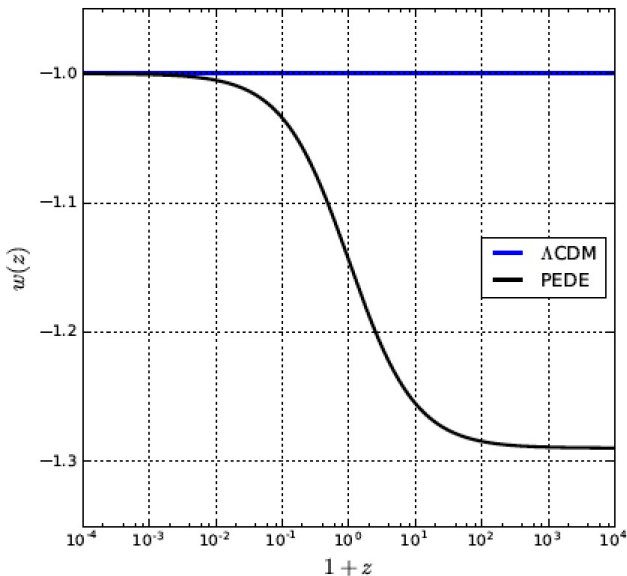


No Dark Energy in the past and it acts as an emergent phenomena:

Allows lower rate of expansion in the past and higher rate of expansion at late times

$$\Omega_{DE}(z) = \Omega_{DE,0} \times [1 - \tanh(\log_{10}(1+z))]$$

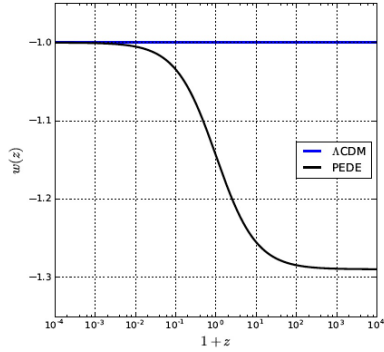
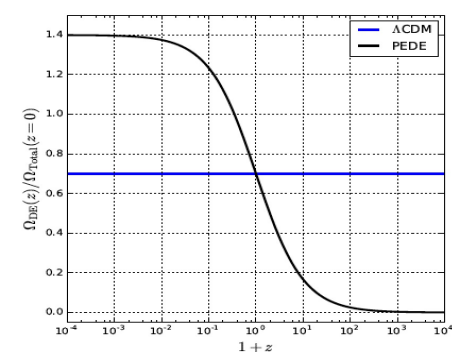
$$\begin{aligned} w(z) &= -\frac{1}{3\ln 10} \times \frac{1 - \tanh^2[\log_{10}(1+z)]}{1 - \tanh[\log_{10}(1+z)]} - 1 \\ &= -\frac{1}{3\ln 10} \times (1 + \tanh[\log_{10}(1+z)]) - 1. \end{aligned}$$



Li and Shafieloo, ApJ Lett 2019

# Phenomenologically Emergent Dark Energy (PEDE)

Model	Data Parameters	Pantheon+BAO			Pantheon+BAO+Ly $\alpha$ +CMB		
		No $H_0$ Prior	$2\sigma$ $H_0$ Prior	$1\sigma$ $H_0$ Prior	No $H_0$ Prior	$2\sigma$ $H_0$ Prior	$1\sigma$ $H_0$ Prior
$\Lambda$ CDM	$\Omega_m$	$0.299^{+0.047}_{-0.043}$	$0.335^{+0.040}_{-0.036}$	$0.347^{+0.041}_{-0.036}$	$0.311^{+0.016}_{-0.014}$	$0.271^{+0.002}_{-0.003}$	$0.256^{+0.002}_{-0.002}$
	$H_0$	$66.94^{+3.721}_{-3.256}$	$71.19^{+1.890}_{0.0}$	$72.61^{+1.617}_{-0.000}$	$67.91^{+1.074}_{1.150}$	$71.19^{+0.271}_{0.000}$	$72.61^{+0.200}_{0.000}$
	$\chi^2_{bf}$	1046.94	<b>1054.76</b>	<b>1060.25</b>	1056.12	<b>1112.28</b>	<b>1168.98</b>
	DIC	1051.00	<b>1058.88</b>	<b>1064.27</b>	1062.35	<b>1127.03</b>	<b>1195.07</b>
CPL	$\Omega_m$	$0.285^{+0.113}_{-0.180}$	$0.332^{+0.071}_{-0.050}$	$0.350^{+0.050}_{-0.043}$	$0.307^{+0.026}_{-0.021}$	$0.286^{+0.007}_{-0.011}$	$0.274^{+0.006}_{-0.009}$
	$H_0$	$64.84^{+14.49}_{-16.12}$	$71.30^{+5.561}_{-0.117}$	$72.70^{+2.746}_{-0.091}$	$68.49^{+2.302}_{-2.680}$	$71.19^{+1.277}_{-0.002}$	$72.61^{+0.918}_{-0.004}$
	$w_0$	$-0.82^{+0.193}_{-0.541}$	$-1.08^{+0.422}_{-0.347}$	$-1.05^{+0.350}_{-0.347}$	$-0.98^{+0.267}_{-0.218}$	$-1.07^{+0.259}_{-0.240}$	$-1.13^{+0.274}_{-0.206}$
	$w_a$	$0.675^{+0.547}_{-3.103}$	$-0.11^{+1.510}_{-3.192}$	$-0.46^{+1.830}_{-2.686}$	$-0.16^{+0.816}_{-1.189}$	$-0.20^{+0.986}_{-1.249}$	$-0.11^{+0.728}_{-1.391}$
	$\chi^2_{bf}$	1044.98	<b>1048.84</b>	<b>1049.66</b>	1055.52	<b>1066.85</b>	<b>1080.83</b>
	DIC	1052.59	<b>1054.46</b>	<b>1056.23</b>	1065.48	<b>1085.06</b>	<b>1128.50</b>
PEDE	$\Omega_m$	$0.341^{+0.045}_{-0.041}$	$0.341^{+0.041}_{-0.037}$	$0.341^{+0.041}_{-0.030}$	$0.291^{+0.015}_{-0.016}$	$0.289^{+0.002}_{-0.014}$	$0.274^{+0.002}_{-0.006}$
	$H_0$	$72.84^{+3.814}_{-3.530}$	$73.01^{+3.371}_{-1.8231}$	$72.79^{+2.652}_{-0.186}$	$71.02^{+1.452}_{-1.368}$	$71.19^{+1.306}_{-0.001}$	$72.61^{+0.651}_{-0.000}$
	$\chi^2_{bf}$	1050.04	<b>1050.04</b>	<b>1050.04</b>	1071.12	<b>1071.20</b>	<b>1080.40</b>
	DIC	1052.01	<b>1053.33</b>	<b>1052.98</b>	1091.15	<b>1091.65</b>	<b>1100.94</b>



**Current:**  
LCDM is still better

**Near Future:**  
PEDE rules out Lambda

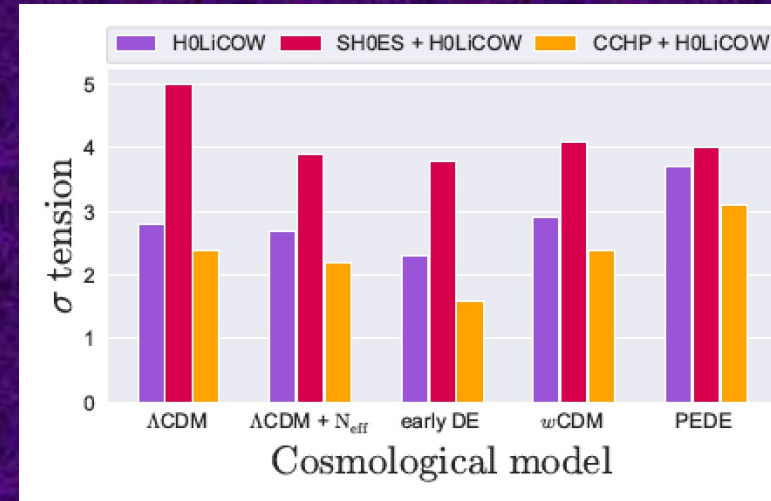
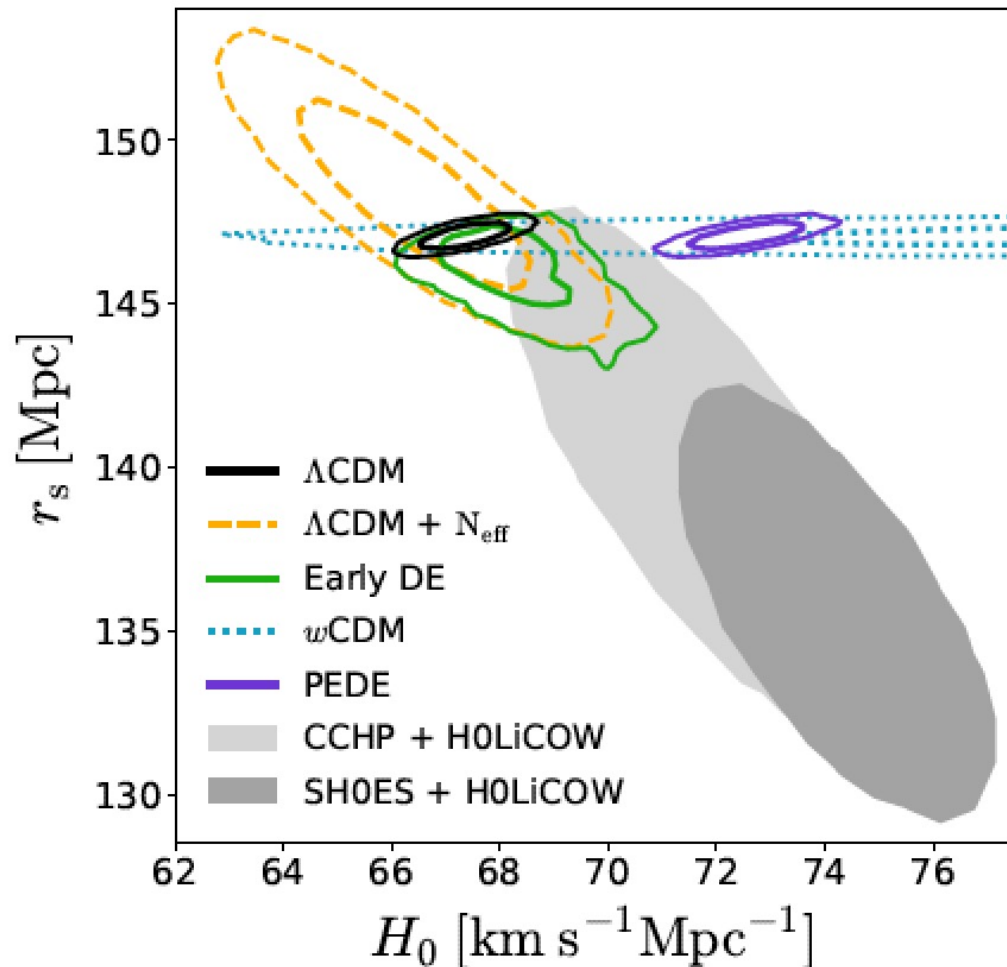
Li and Shafieloo, ApJ Lett 2019 (arXiv:1906.08275)

$$p_D = \overline{\chi^2(\theta)} - \chi^2(\bar{\theta}).$$

$$DIC \equiv D(\theta) + 2p_D = \overline{D(\theta)} + p_D,$$



# Comparing candidates



Arendse et al, arXiv:1909.07986

H0LiCOW Collaboration

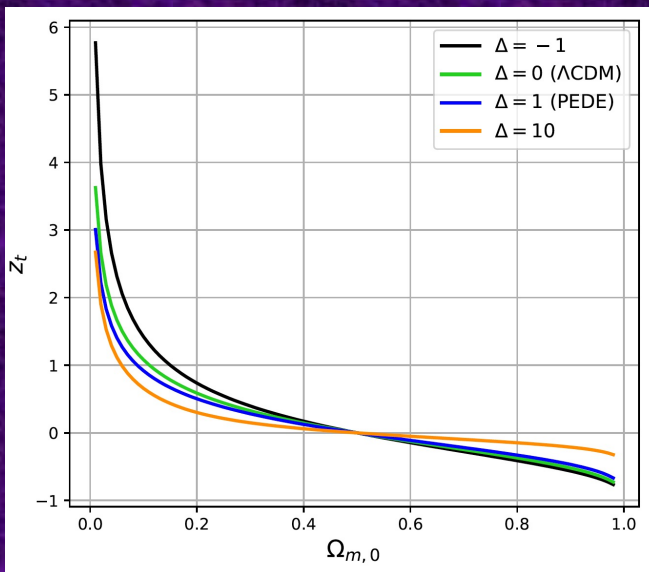
# Generalized Emergent Dark Energy (GEDE)

$$\tilde{\Omega}_{\text{DE}}(z) = \Omega_{\text{DE},0} \frac{1 - \tanh\left(\Delta \times \log_{10}\left(\frac{1+z}{1+z_t}\right)\right)}{1 + \tanh\left(\Delta \times \log_{10}(1+z_t)\right)}$$

$$w(z) = -\frac{\Delta}{3 \ln 10} \times \left(1 + \tanh\left(\Delta \times \log_{10}\left(\frac{1+z}{1+z_t}\right)\right)\right) - 1.$$

*-Has one degree of freedom for DE sector*

*-LCDM and PEDE are both included at special limits*



$$\Delta = 0$$

LCDM

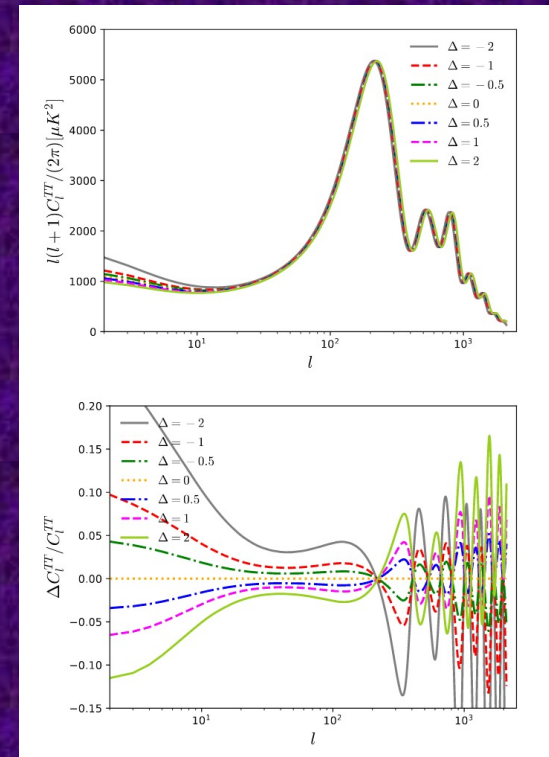
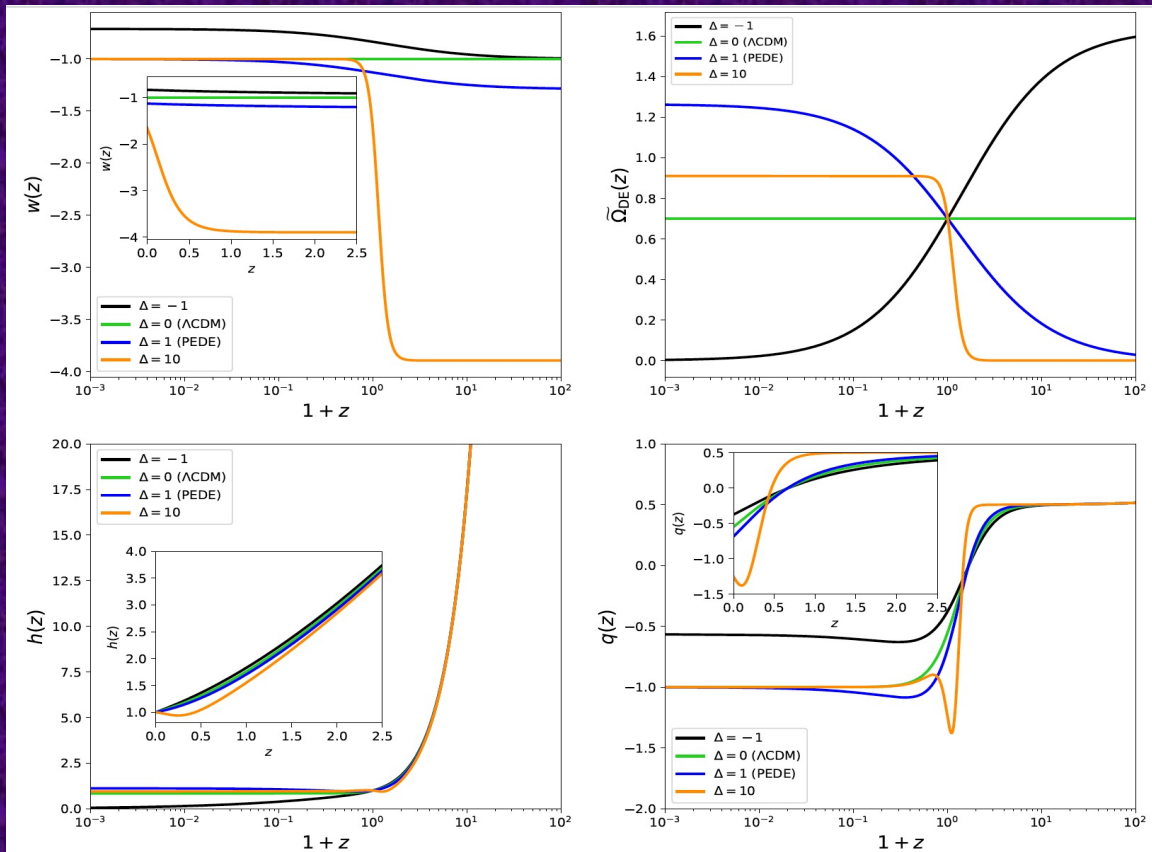
$$\Delta = 1$$

PEDE

$$\Omega_{\text{DE}}(z_t) = \Omega_{m,0}(1+z_t)^3$$

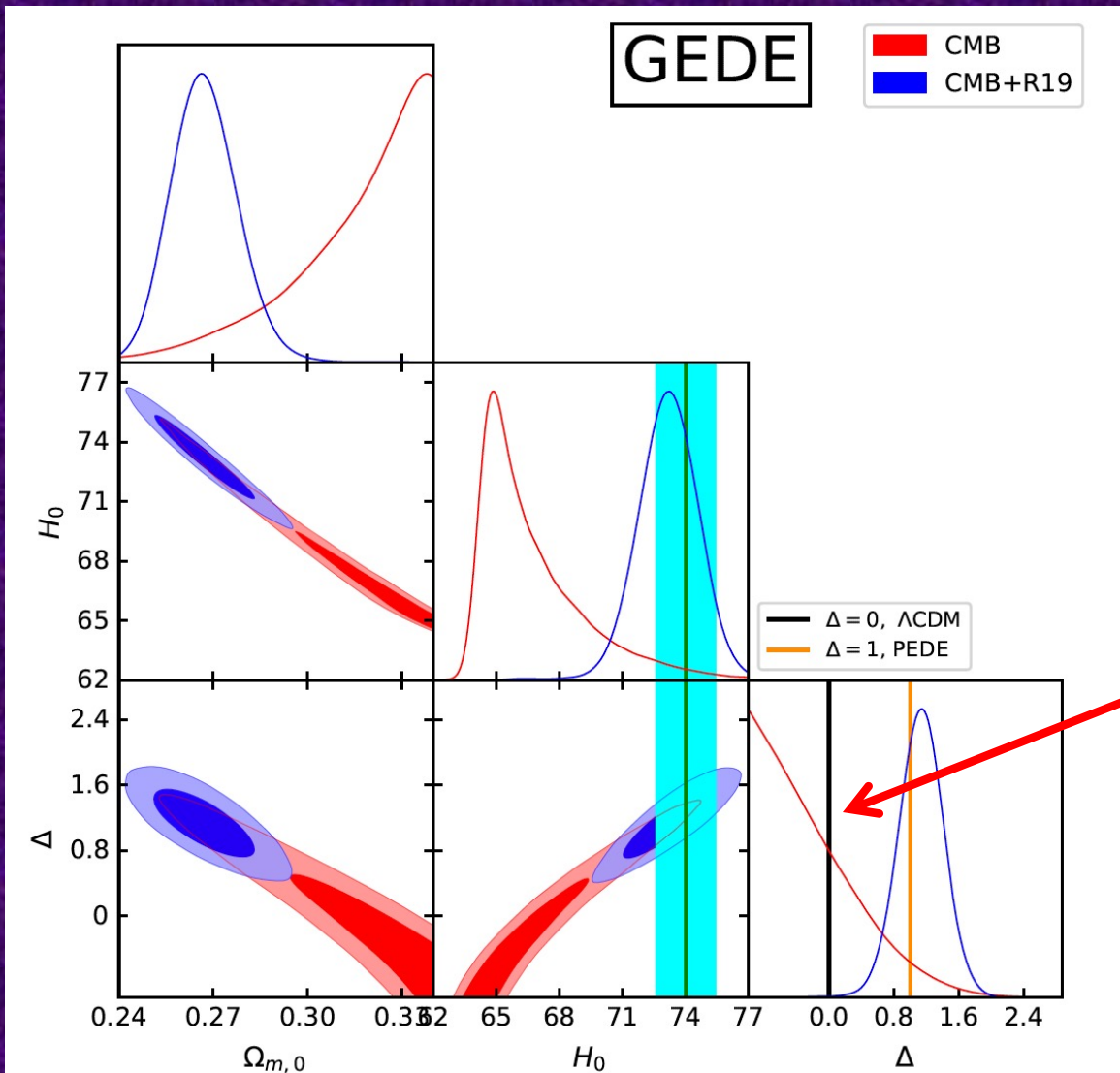
# Generalized Emergent Dark Energy (GEDE)

Accommodates various forms and can be confronted with various data





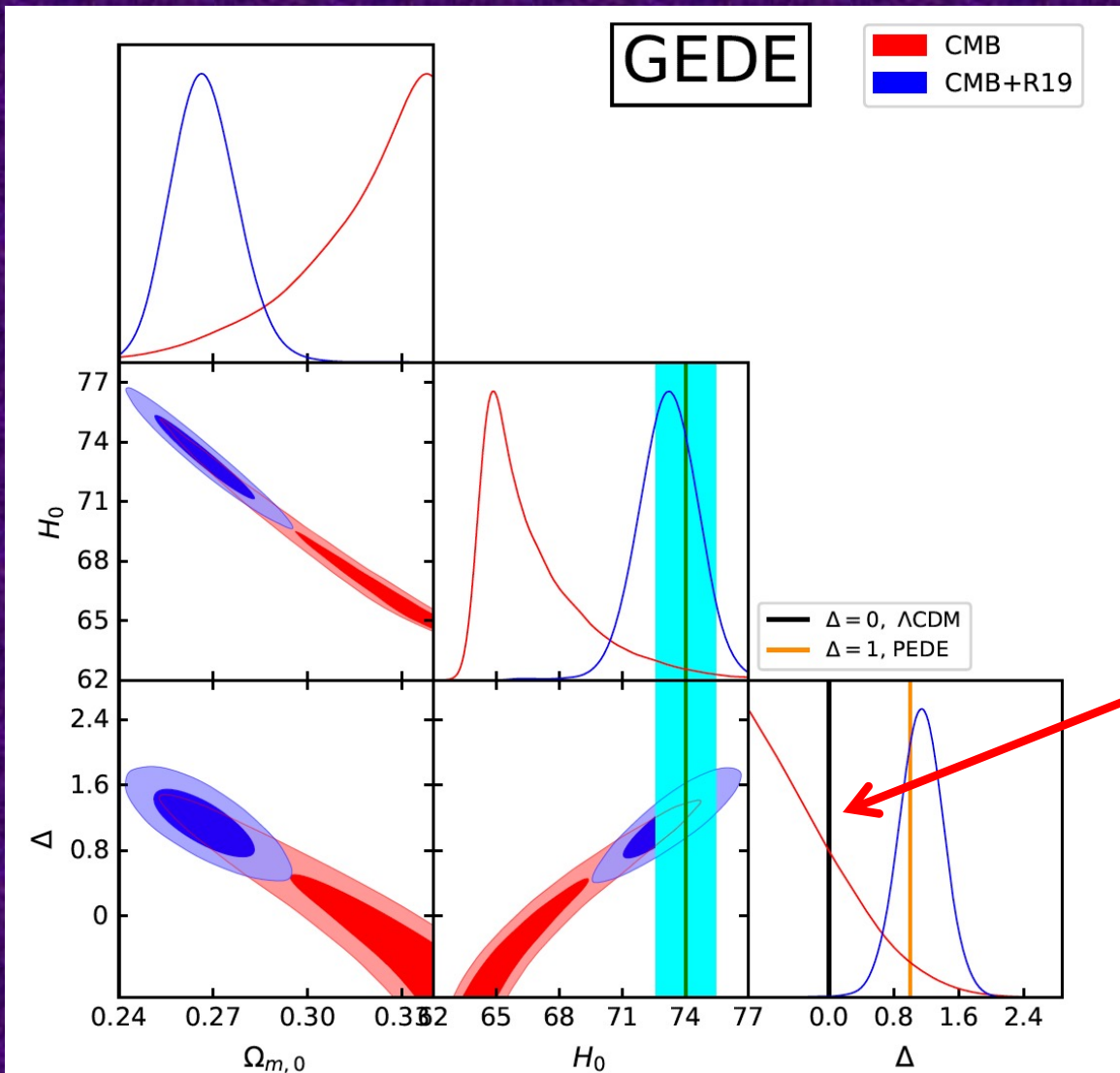
# Generalized Emergent Dark Energy (GEDE)



Lambda outside  
the 4 $\sigma$  CL

Li and Shafieloo, ApJ 2020,  
arXiv:2001.05103

# Generalized Emergent Dark Energy (GEDE)

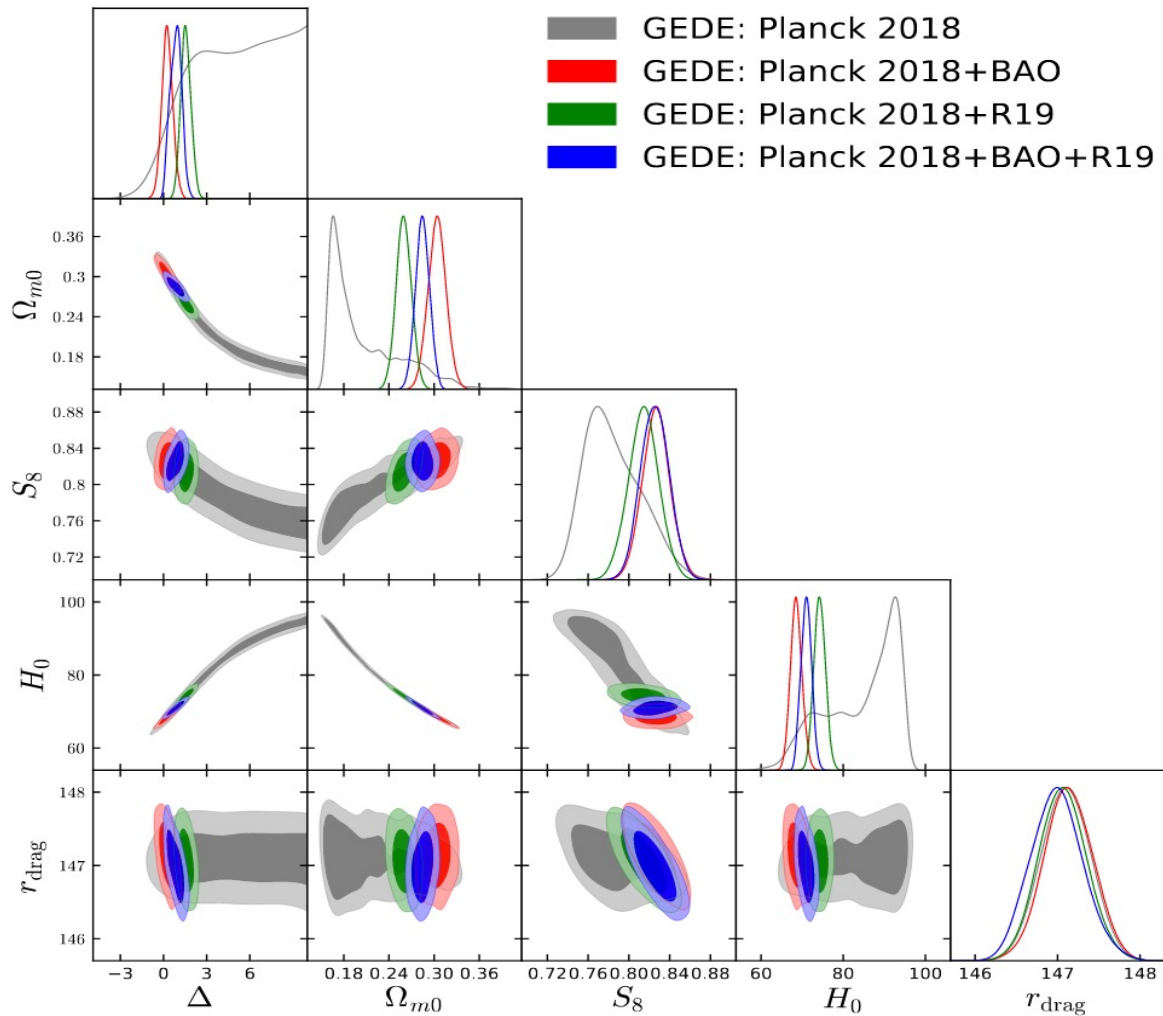


Time will show!

Lambda outside the 4\sigma CL

Li and Shafieloo, ApJ 2020, arXiv:2001.05103

# Generalized Emergent Dark Energy (GEDE)



Full analysis  
using various  
combination of  
the data

W. Yang, E. Di Valentino, S. Pan,  
A. Shafieloo, X. Li,  
arXiv:2103.03815



# Generalized Emergent Dark Energy (GEDE)

Full analysis using  
various combination of  
the data

Parameters	Planck 2018+JLA	Planck 2018+Pantheon	Planck 2018+BAO+JLA+R19	Planck 2018+BAO+Pantheon+R19
$\Omega_c h^2$	0.1202 <sup>+0.0013+0.0025</sup> -0.0013-0.0026	0.1203 <sup>+0.0014+0.0027</sup> -0.0014-0.0026	0.1201 <sup>+0.0012+0.0023</sup> -0.0012-0.0024	0.1199 <sup>+0.0012+0.0023</sup> -0.0012-0.0024
$\Omega_b h^2$	0.02235 <sup>+0.00015+0.00029</sup> -0.00014-0.00029	0.02236 <sup>+0.00015+0.00030</sup> -0.00015-0.00029	0.02238 <sup>+0.00014+0.00030</sup> -0.00016-0.00028	0.02240 <sup>+0.00014+0.00029</sup> -0.00015-0.00029
$100\theta_{MC}$	1.04090 <sup>+0.00031+0.00062</sup> -0.00031-0.00062	1.04092 <sup>+0.00031+0.00061</sup> -0.00031-0.00059	1.04096 <sup>+0.00031+0.00060</sup> -0.00030-0.00060	1.04095 <sup>+0.00031+0.00058</sup> -0.00031-0.00061
$\tau$	0.0544 <sup>+0.0075+0.015</sup> -0.0074-0.014	0.0541 <sup>+0.0074+0.015</sup> -0.0075-0.015	0.0543 <sup>+0.0074+0.015</sup> -0.0078-0.016	0.0550 <sup>+0.0076+0.016</sup> -0.0077-0.015
$n_s$	0.9647 <sup>+0.0043+0.0085</sup> -0.0047-0.0084	0.9647 <sup>+0.0047+0.0086</sup> -0.0043-0.0089	0.9649 <sup>+0.0041+0.0081</sup> -0.0041-0.0079	0.9656 <sup>+0.0041+0.0084</sup> -0.0041-0.0080
$\ln(10^{10} A_s)$	3.045 <sup>+0.015+0.031</sup> -0.016-0.029	3.045 <sup>+0.016+0.031</sup> -0.016-0.031	3.044 <sup>+0.015+0.032</sup> -0.016-0.031	3.046 <sup>+0.016+0.032</sup> -0.016-0.030
$\Delta$	0.30 <sup>+0.36+0.79</sup> -0.40-0.73	0.25 <sup>+0.26+0.51</sup> -0.26-0.52	0.69 <sup>+0.25+0.49</sup> -0.25-0.48	0.55 <sup>+0.20+0.42</sup> -0.21-0.43
$\Omega_{m0}$	0.305 <sup>+0.015+0.029</sup> -0.015-0.029	0.307 <sup>+0.011+0.021</sup> -0.011-0.021	0.289 <sup>+0.0074+0.015</sup> -0.0072-0.014	0.293 <sup>+0.0065+0.015</sup> -0.0067-0.013
$\sigma_8$	0.825 <sup>+0.017+0.037</sup> -0.019-0.034	0.823 <sup>+0.016+0.028</sup> -0.013-0.028	0.841 <sup>+0.014+0.027</sup> -0.014-0.027	0.834 <sup>+0.012+0.025</sup> -0.012-0.025
$H_0$	68.6 <sup>+1.5+3.3</sup> -1.8-3.0	68.3 <sup>+1.1+2.3</sup> -1.1-2.1	70.38 <sup>+0.87+1.8</sup> -0.89-1.7	69.86 <sup>+0.75+1.4</sup> -0.74-1.4
$S_8$	0.831 <sup>+0.015+0.031</sup> -0.015-0.030	0.832 <sup>+0.015+0.030</sup> -0.015-0.029	0.825 <sup>+0.013+0.026</sup> -0.013-0.025	0.824 <sup>+0.014+0.025</sup> -0.013-0.025
$r_{\text{drag}}$	147.05 <sup>+0.28+0.58</sup> -0.31-0.55	147.03 <sup>+0.30+0.58</sup> -0.30-0.57	147.05 <sup>+0.27+0.53</sup> -0.28-0.54	147.10 <sup>+0.27+0.52</sup> -0.27-0.54

# Generalized Emergent Dark Energy (GEDE)

Data	$\ln B_{ij}$
Planck 2018	2.9
Planck 2018+BAO	0.8
Planck 2018+R19	12.1
Planck 2018+BAO+R19	7.9
Planck 2018+JLA	-0.2
Planck 2018+Pantheon	-0.9
Planck 2018+BAO+JLA+R19	6.1
Planck 2018+BAO+Pantheon+R19	5.8

Full analysis using  
various combination of  
the data

Model Comparison:  
Bayesian evidence analysis in strong support of  
emergent dark energy

# Generalized Emergent Dark Energy (GEDE)

Data	$\ln B_{ij}$
Planck 2018	2.9
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Planck 2018+BAO+JLA+R19	6.1
Planck 2018+BAO+Pantheon+R19	5.8

Full analysis using various combination of the data

Current tensions allow us to find models statistically better than LCDM but are all tensions resolved?

**No!**

Model Comparison:  
Bayesian evidence analysis in strong support of emergent dark energy



(Present)

## ***Standard Model of Cosmology***

Universe is Flat

Universe is Isotropic

Universe is Homogeneous

Dark Energy is Lambda ( $w=-1$ )

Power-Law primordial spectrum ( $n_s=\text{const}$ )

Dark Matter is cold

All within framework of FLRW

# Model Independent Estimation of Primordial Spectrum

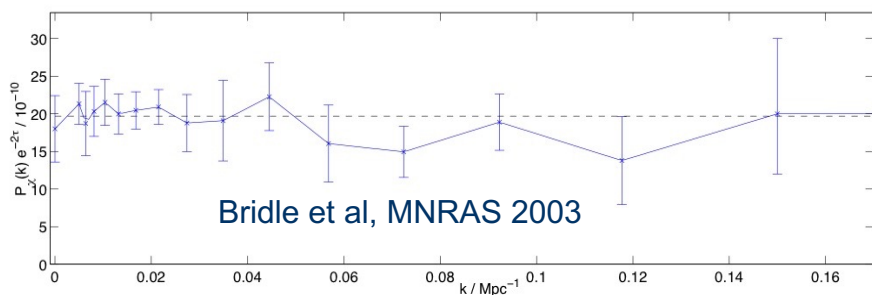
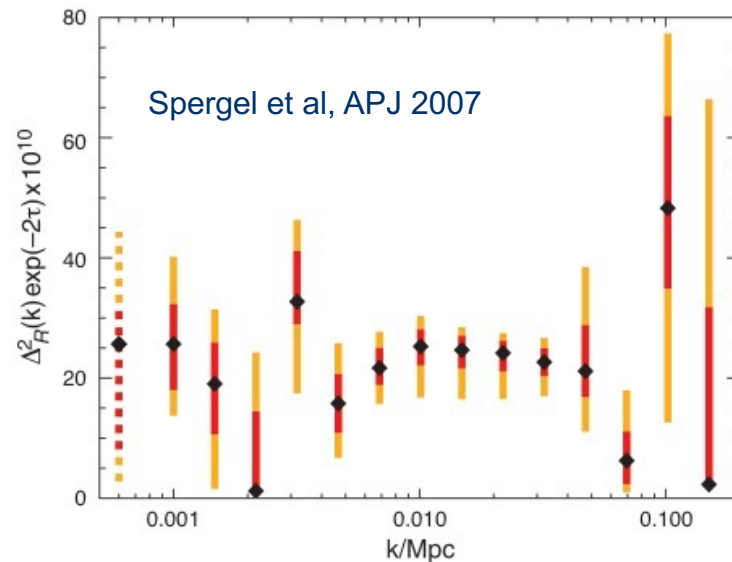
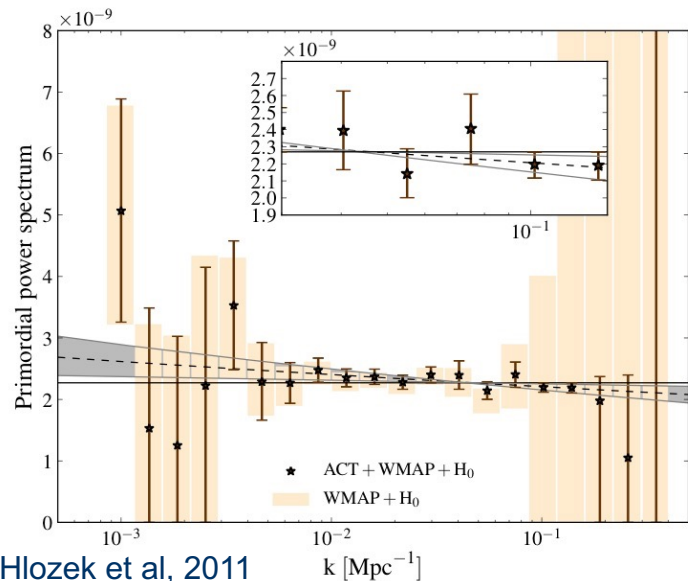
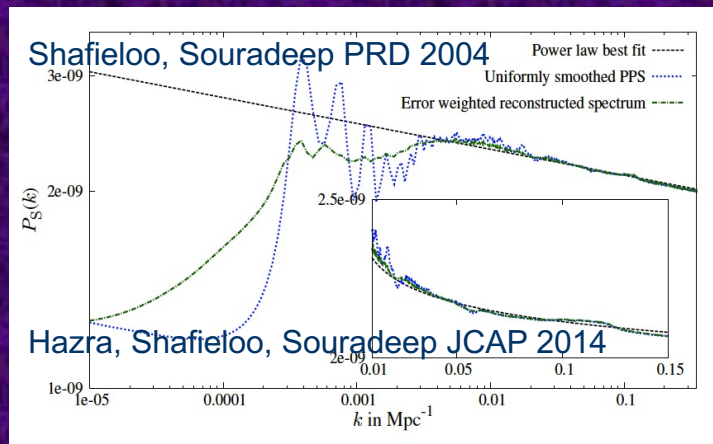
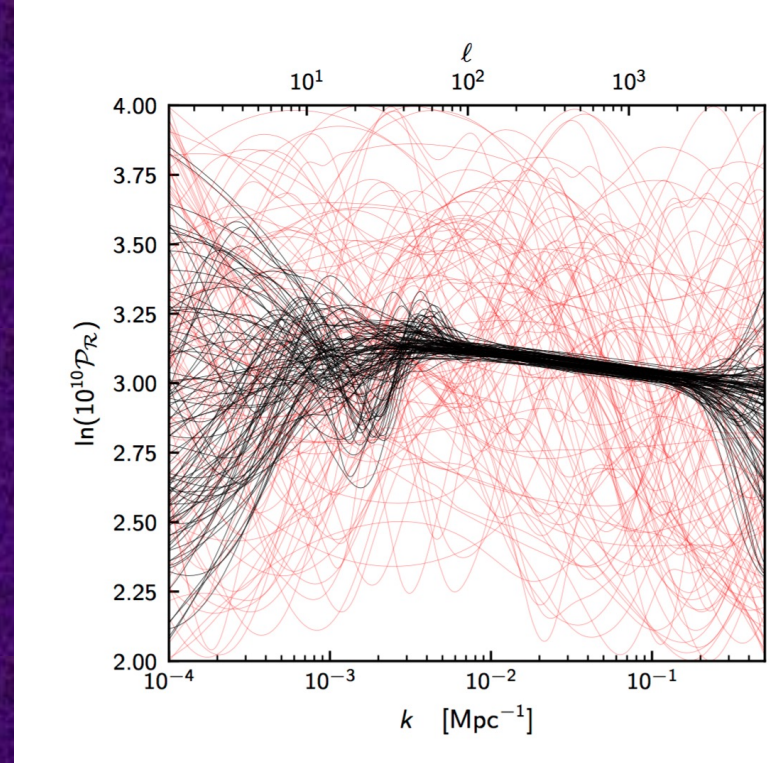
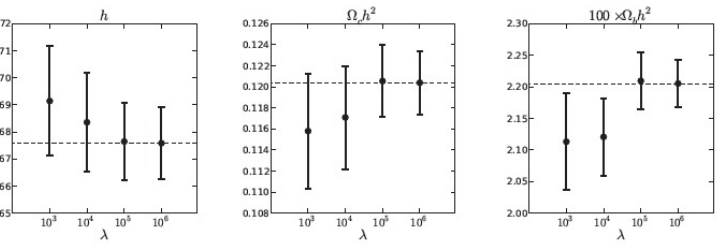
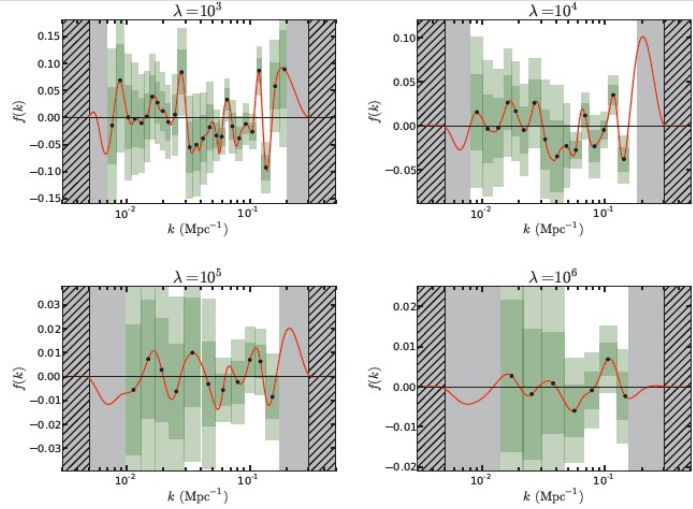


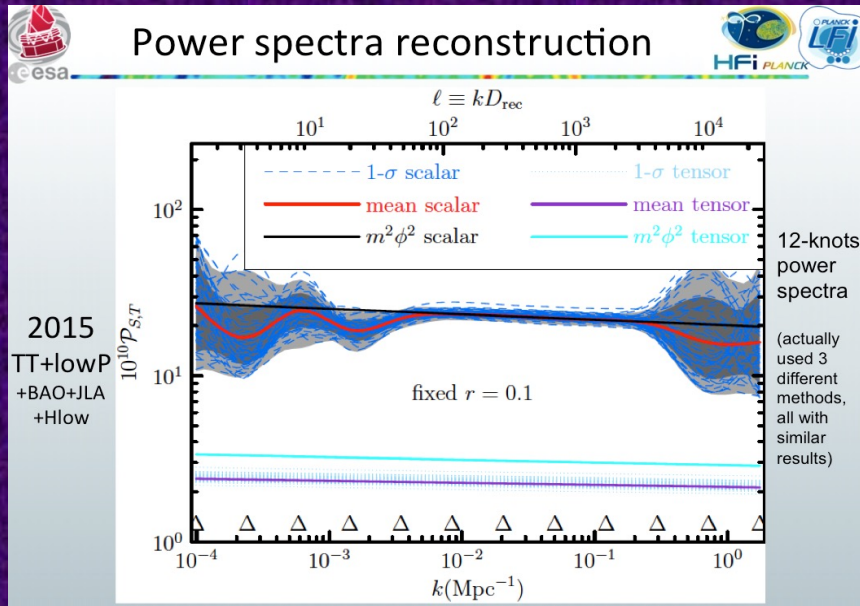
Figure 4. Reconstruction of the shape of the primordial power spectrum in 16 bands after marginalising over the Hubble constant, baryon and dark matter densities, and the redshift of reionization.





Planck 2013

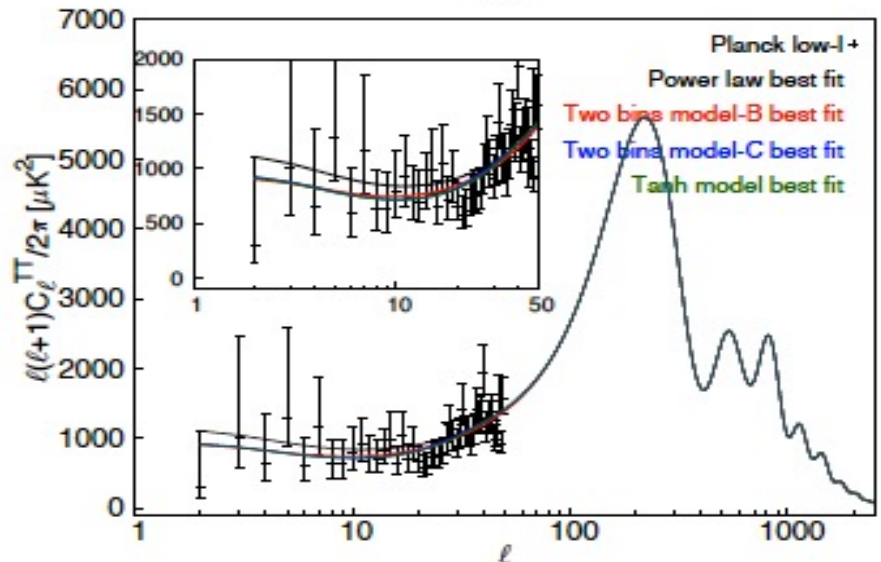
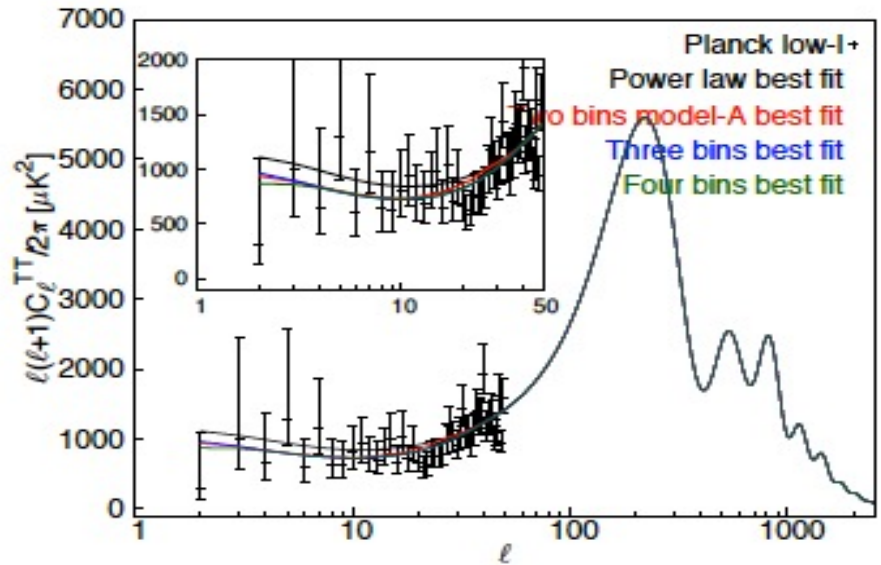
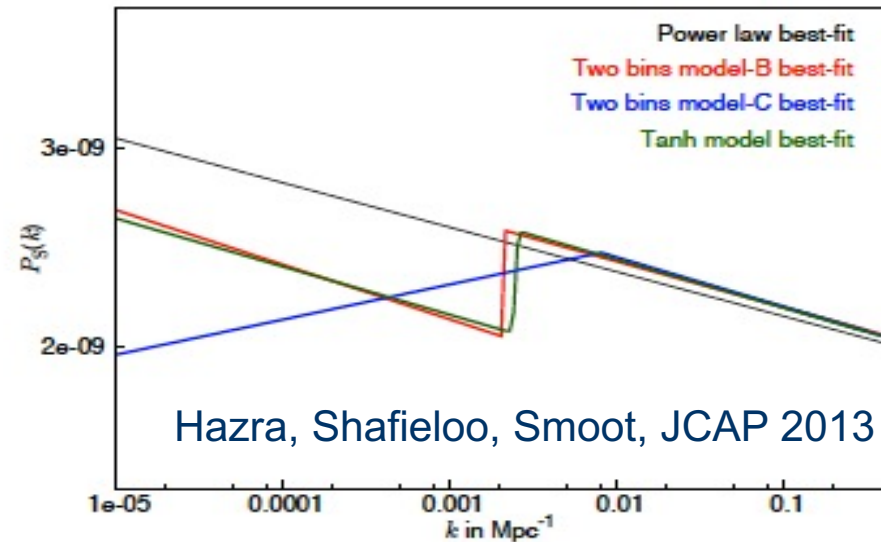
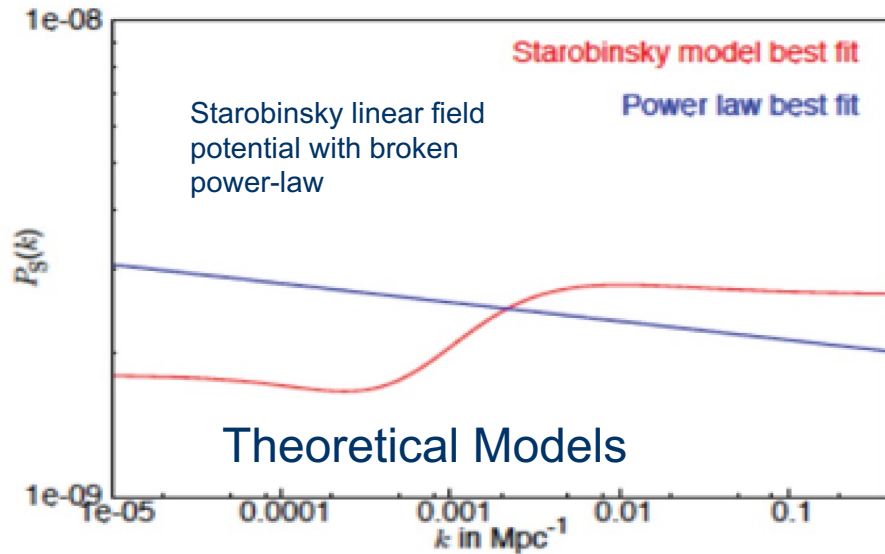
Planck 2015



Planck 2018



# Beyond Power-Law: there are some other models consistent to the data.



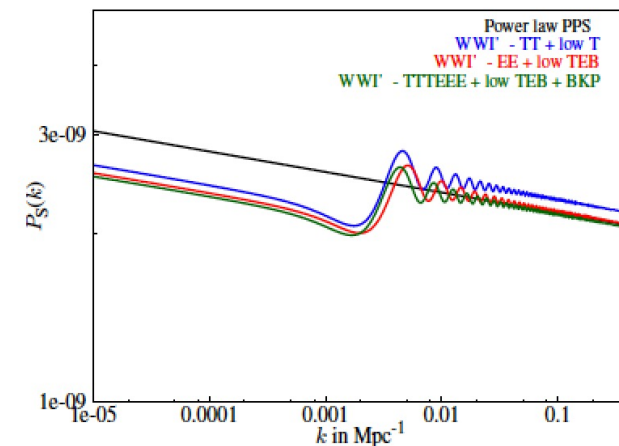
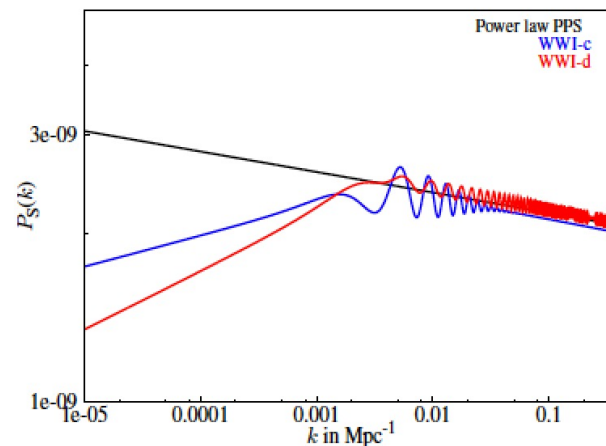
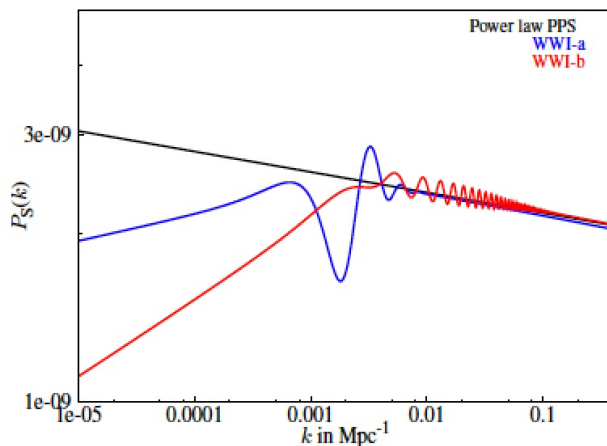
Individual likelihoods comparison

Individual likelihood	Baseline	WWI-a $\Delta_{\text{DOF}} = 4$	WWI-b $\Delta_{\text{DOF}} = 4$	WWI-c $\Delta_{\text{DOF}} = 4$	WWI-d $\Delta_{\text{DOF}} = 4$	WWI' $\Delta_{\text{DOF}} = 2$
TT	761.1	762	761.9	762.8	762.8	762.4
lowT	15.4	8.2	13.4	12.1	13	10.2
Total	778.1	772.1 (-6)	777 (-1.1)	777 (-1.1)	778.4 (0.3)	775 (-3.1)
EE	751.2	748.8	747.2	748.6	750.2	746.8
lowTEB	10493.6	10490	10495.6	10492.4	10495.7	10492.2
Total	11248.8	11241.8 (-7)	11246.2 (-2.6)	11244.5 (-4.3)	11249.3 (0.5)	11242.3 (-6.5)
TTTEEE	2431.7	2432.7	2422.6	2427.8	2421.7	2426.5
lowTEB	10497	10490.8	10495.1	10493.4	10495.3	10492.7
Total	12935.6	12929.5 (-6.1)	12924.2 (-11.4)	12927.6 (-8)	12923.4 (-12.2)	12925.2 (-10.4)
TT	764.5	763.6	762.2	764.4	762.9	762.8
EE	753.9	754.8	750.5	750.8	750.8	751
TE	932	933.4	928.7	929.2	927	928.8
lowTEB	10498.4	10490.4	10495.8	10493.7	10495.6	10492.4
BKP	41.6	42	42	42.6	41.8	42.9
Total	12997	12991 (-6)	12985.9 (-11.1)	12987.2 (-9.8)	12985 (-12)	12985.1 (-11.9)
TTTEEE	2431.7	2432.8	2421.4	2426.7	2421	2425.7
lowTEB	10498.5	10490.5	10495.5	10493.6	10495.8	10492.6
BKP	41.6	42	42.7	42	41.9	42.5
Total	12978.3	12971.3 (-7)	12967.3 (-11)	12968.6 (-9.7)	12965 (-13.3)	12968.6 (-9.7)
TT (bin1)	8402.1	8404.1	8403.9	8405.2	8402.1	8401.9
lowT	15.4	8.3	13.3	11.9	13.2	10.3
Total	8419.6	8414.7 (-4.9)	8419.5 (-0.1)	8419.8 (0.2)	8418.1 (-1.5)	8414.4 (-5.2)
TTTEEE (bin1)	24158.2	24158.6	24149	24155	24148.4	24151.5
lowTEB	10497.6	10490.3	10493.4	10493.6	10495.3	10492.7
Total	34661.9	34655.3 (-6.6)	34650.5 (-11.4)	34654.4 (-7.5)	34649.5 (-12.4)	34650.6 (-11.3)

Beyond Power-Law:  
*there are some other models consistent to the data.*

## Whipped Inflation

- Hazra, Shafieloo, Smoot, JCAP 2013
- Hazra, Shafieloo, Smoot, Starobinsky, JCAP 2014a
- Hazra, Shafieloo, Smoot, Starobinsky, JCAP 2014b
- Hazra, Shafieloo, Smoot, Starobinsky, Phys. Rev. Lett 2014
- Hazra, Shafieloo, Smoot, Starobinsky, JCAP 2016
- Hazra et al, JCAP 2018
- Debono, Hazra, Shafieloo, Smoot, Starobinsky, MNRAS 2020
- Hazra, Paoletti, Debono, Shafieloo, Smoot, Starobinsky, JCAP 2021





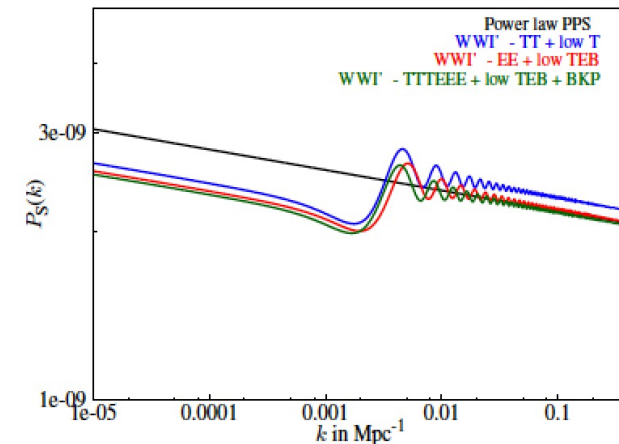
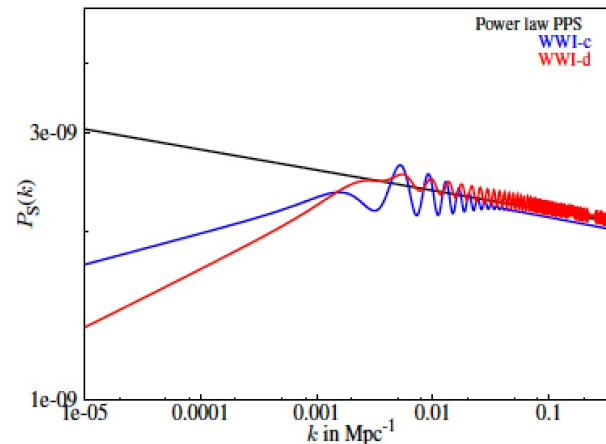
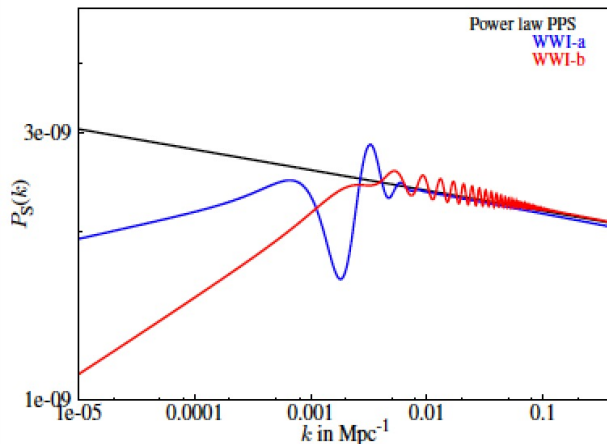
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Individual likelihood	Baseline	WWI-a $\Delta_{\text{DOF}} = 4$	WWI-b $\Delta_{\text{DOF}} = 4$	WWI-c $\Delta_{\text{DOF}} = 4$	WWI-d $\Delta_{\text{DOF}} = 4$	WWI' $\Delta_{\text{DOF}} = 2$
TT	761.1	762	761.9	762.8	762.8	762.4
lowT	15.4	8.2	13.4	12.1	13	10.2
Total	778.1	772.1 (-6)	777 (-1.1)	777 (-1.1)	778.4 (0.3)	775 (-3.1)
EE	751.2	748.8	747.2	748.6	750.2	746.8
lowTEB	10493.6	10490	10495.6	10492.4	10495.7	10492.2
Total	11248.8	11241.8 (-7)	11246.2 (-2.6)	11244.5 (-4.3)	11249.3 (0.5)	11242.3 (-6.5)
TTTEEE	2431.7	2432.7	2422.6	2427.8	2421.7	2426.5
lowTEB	10497	10490.8	10495.1	10493.4	10495.3	10492.7
Total	12935.6	12929.5 (-6.1)	12924.2 (-11.4)	12927.6 (-8)	12923.4 (-12.2)	12925.2 (-10.4)
TT	764.5	763.6	762.2	764.4	762.9	762.8
EE	753.9	754.8	750.5	750.8	750.8	751
TE	932	933.4	928.7	929.2	927	928.8
lowTEB	10498.4	10490.4	10495.8	10493.7	10495.6	10492.4
BKP	41.6	42	42	42.6	41.8	42.9
Total	12997	12991 (-6)	12985.9 (-11.1)	12987.2 (-9.8)	12985 (-12)	12985.1 (-11.9)
TTTEEE	2431.7	2432.8	2421.4	2426.7	2421	2425.7
lowTEB	10498.5	10490.5	10495.5	10493.6	10495.8	10492.6
BKP	41.6	42	42.7	42	41.9	42.5
Total	12978.3	12971.3 (-7)	12967.3 (-11)	12968.6 (-9.7)	12965 (-13.3)	12968.6 (-9.7)
TT (bin1)	8402.1	8404.1	8403.9	8405.2	8402.1	8401.9
lowT	15.4	8.3	13.3	11.9	13.2	10.3
Total	8419.6	8414.7 (-4.9)	8419.5 (-0.1)	8419.8 (0.2)	8418.1 (-1.5)	8414.4 (-5.2)
TTTEEE (bin1)	24158.2	24158.6	24149	24155	24148.4	24151.5
lowTEB	10497.6	10490.3	10493.4	10493.6	10495.3	10492.7
Total	34661.9	34655.3 (-6.6)	34650.5 (-11.4)	34654.4 (-7.5)	34649.5 (-12.4)	34650.6 (-11.3)

Beyond Power-Law:  
*there are some other models consistent to the data.*

*Whipped Inflation*

- Hazra, Shafieloo, Smoot, JCAP 2013
- Hazra, Shafieloo, Smoot, Starobinsky, JCAP 2014A
- Hazra, Shafieloo, Smoot, Starobinsky, JCAP 2014B
- Hazra, Shafieloo, Smoot, Starobinsky, Phys. Rev. Lett 2014
- Hazra, Shafieloo, Smoot, Starobinsky, JCAP 2016
- Hazra et al, JCAP 2018
- Debono, Hazra, Shafieloo, Smoot, Starobinsky, MNRAS 2020
- Hazra, Paoletti, Debono, Shafieloo, Smoot, Starobinsky, JCAP 2021





# Forms of PPS and Effects on the Background Cosmology

- Flat Lambda Cold Dark Matter Universe (LCDM) with power-law form of the primordial spectrum
- It has 6 main parameters.

$$C_l = \sum G(l, k) P(k)$$

↕ 3

$$C_l^{obs}$$

2 ←  $G(l, k)$  ← 1

2 ←

$$P(k) = A_s \left[ \frac{k}{k_*} \right]^{n_s - 1}$$

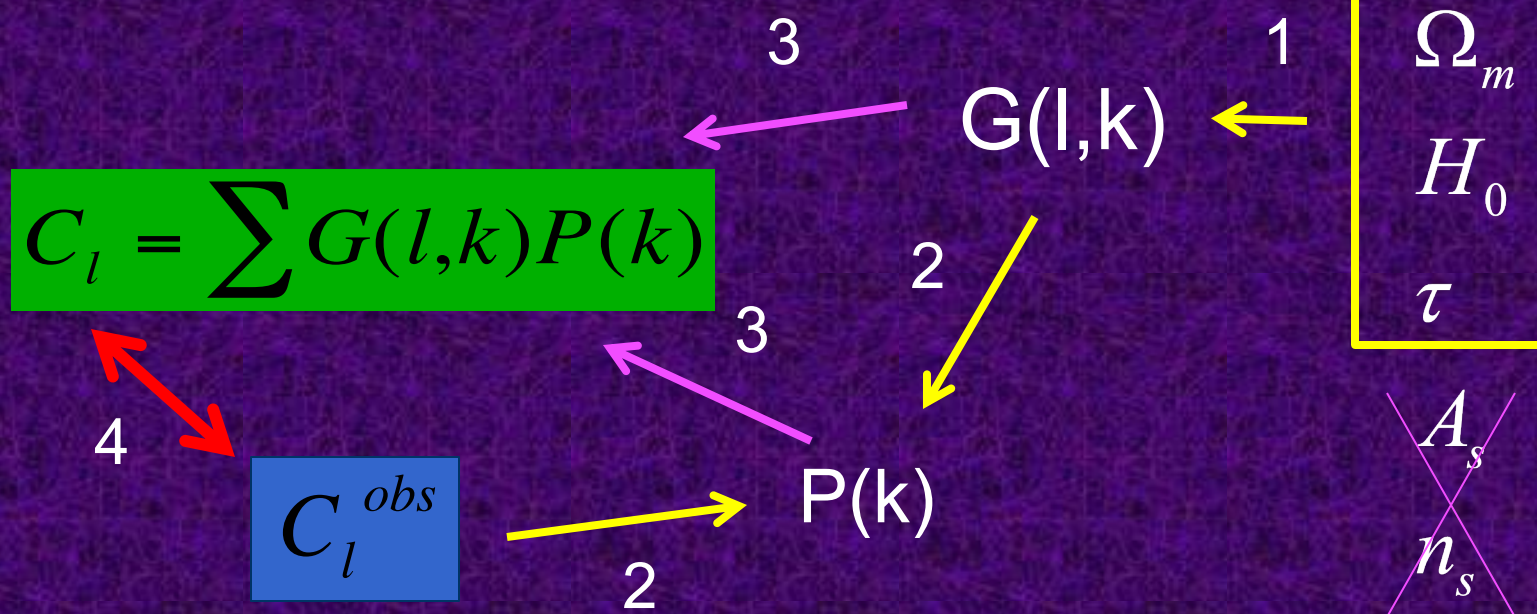
1 ←

$$\begin{matrix} \Omega_b \\ \Omega_m \\ H_0 \\ \tau \end{matrix}$$

$$\begin{matrix} A_s \\ n_s \end{matrix}$$

# Forms of PPS and Effects on the Background Cosmology

- Cosmological parameter estimation with free form primordial power spectrum



# Modified Richardson-Lucy Deconvolution

- Iterative algorithm
- Not sensitive to the initial guess.
- Enforce positivity of  $P(k)$ .

$$C_\ell = \sum_i G_{\ell k_i} P_{k_i}$$

[  $G(l, k)$  is positive definite and  $C_l$  is positive ]

$$P_k^{(i+1)} - P_k^{(i)} = P_k^{(i)} \times \left[ \sum_{\ell=2}^{\ell=900} \tilde{G}_{\ell k}^{\text{un-binned}} \left\{ \left( \frac{C_\ell^D - C_\ell^{\text{T}(i)}}{C_\ell^{\text{T}(i)}} \right) \tanh^2 \left[ Q_\ell (C_\ell^D - C_\ell^{\text{T}(i)}) \right] \right\}_{\text{un-binned}} + \sum_{\ell_{\text{binned}} > 900} \tilde{G}_{\ell k}^{\text{binned}} \left\{ \left( \frac{C_\ell^D - C_\ell^{\text{T}(i)}}{C_\ell^{\text{T}(i)}} \right) \tanh^2 \left[ \frac{C_\ell^D - C_\ell^{\text{T}(i)}}{\sigma_\ell^D} \right]^2 \right\}_{\text{binned}} \right], \quad (1)$$

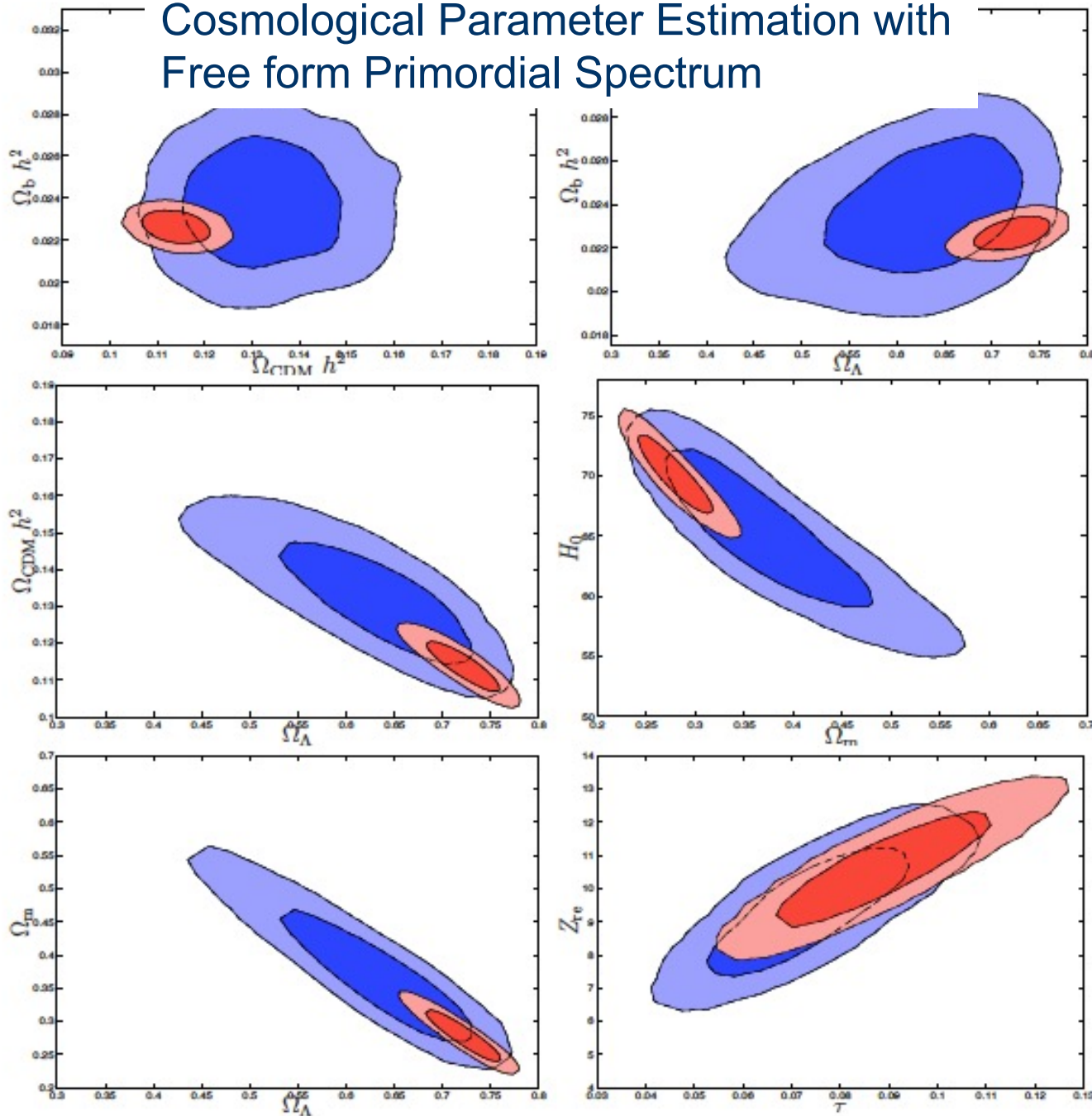
Shafieloo & Souradeep PRD 2004 ;  
 Shafieloo et al, PRD 2007;  
 Shafieloo & Souradeep, PRD 2008;  
 Nicholson & Contaldi JCAP 2009  
 Hamann, Shafieloo & Souradeep JCAP 2010  
 Hazra, Shafieloo & Souradeep PRD 2013  
 Hazra, Shafieloo & Souradeep JCAP 2013  
 Hazra, Shafieloo & Souradeep JCAP 2014  
 Hazra, Shafieloo & Souradeep JCAP 2015

$$Q_\ell = \sum_{\ell'} (C_{\ell'}^D - C_{\ell'}^{\text{T}(i)}) \text{COV}^{-1}(\ell, \ell'),$$

Hazra, Shafieloo, Souradeep, JCAP 2019  
 Keeley, Shafieloo, Hazra, Souradeep, JCAP 2020  
 Hazra, Antony, Shafieloo, arXiv:2201.12000



# Cosmological Parameter Estimation with Free form Primordial Spectrum



WMAP9 Data

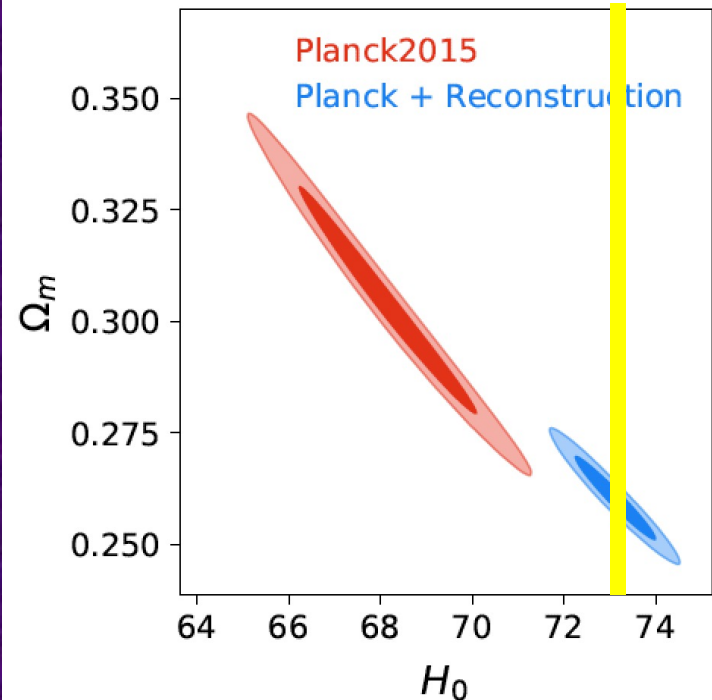
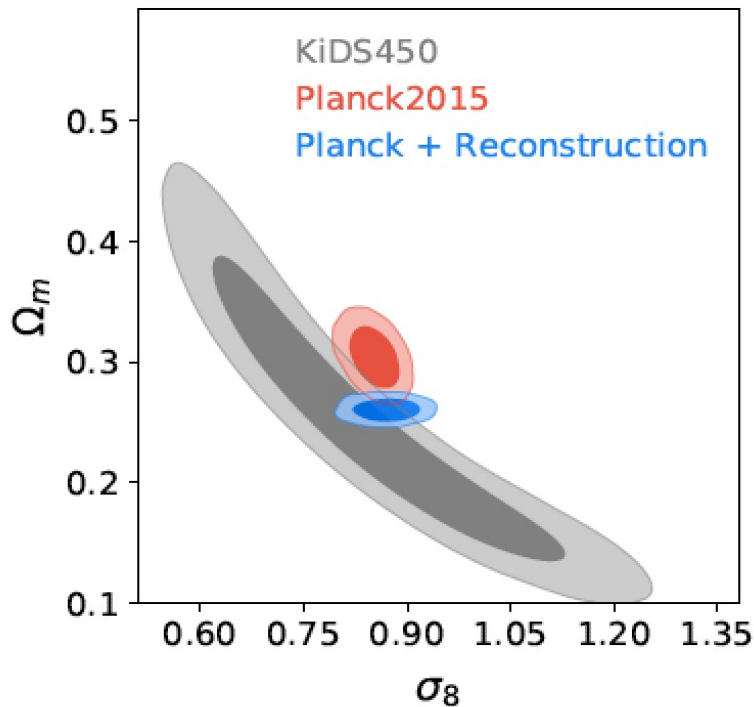
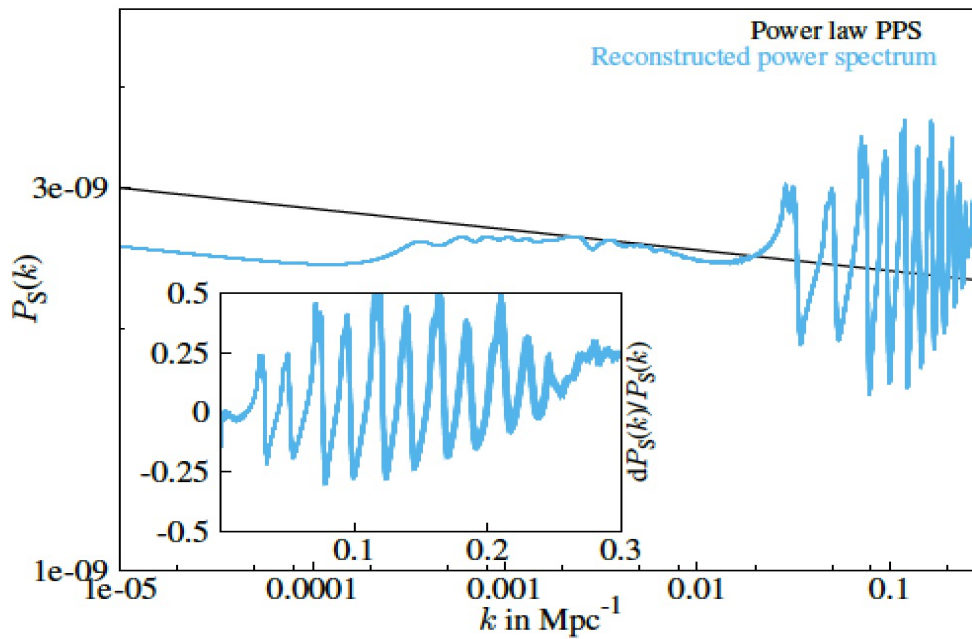
Red Contours:  
Power Law PPS

Blue Contours:  
Free Form PPS

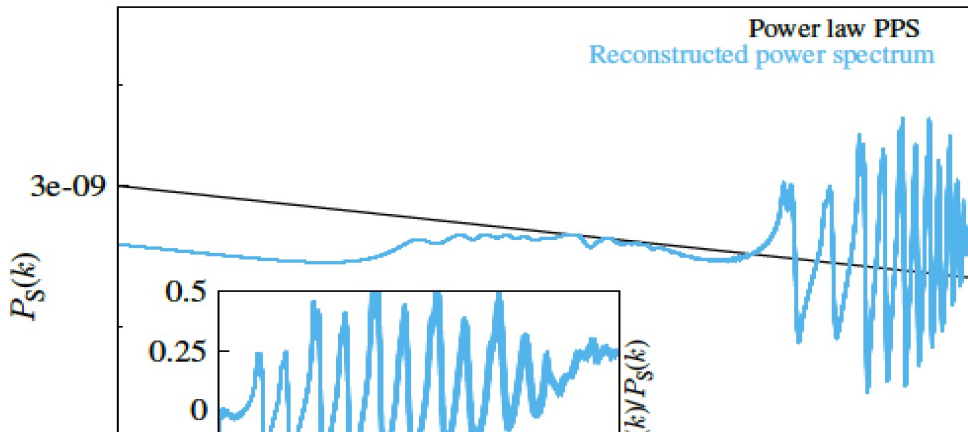
Hazra, Shafieloo, Souradeep,  
PRD 2013

# Background Cosmological Parameters and PPS

We use the reconstructed PPS for parameter estimation, similar to what we do with PL.

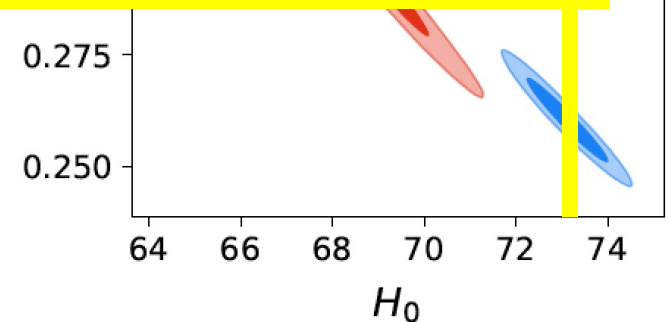
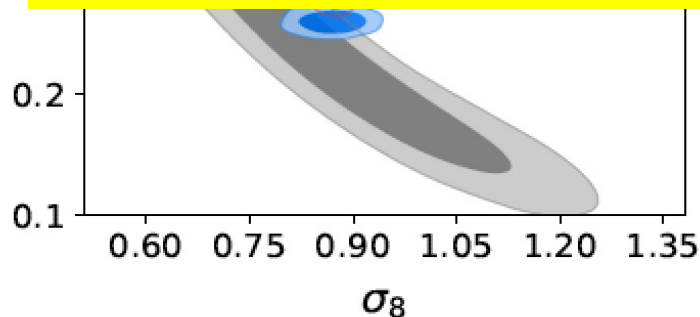


# Background Cosmological Parameters and PPS

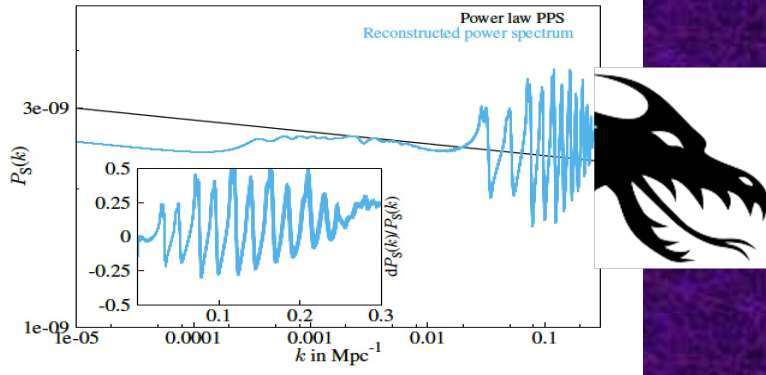


NOTE: Similar attempts by other groups to find a form of PPS for a different set of background parameters (to resolve Hubble tension) has failed so far.

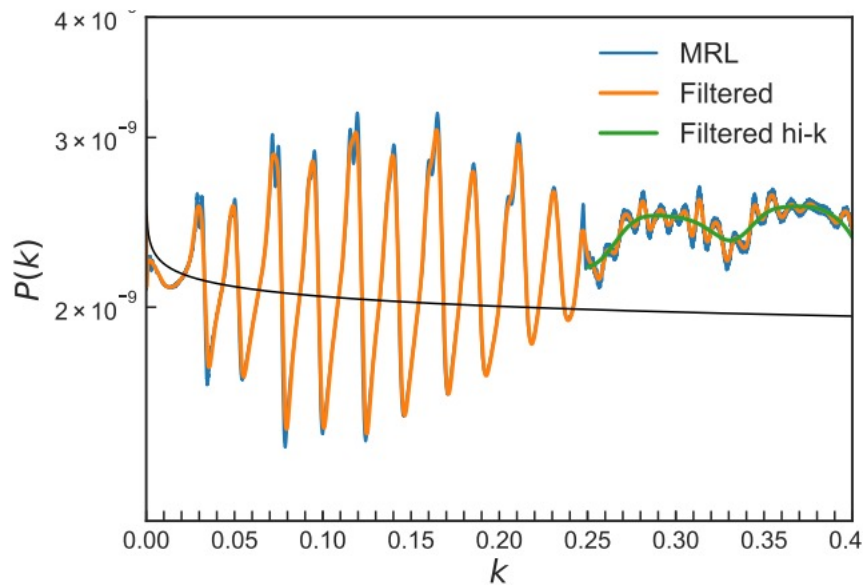
The great advantage of the MRL deconvolution to other methods is in its ability to generate *various features with different amplitudes and frequencies at different wave numbers.*



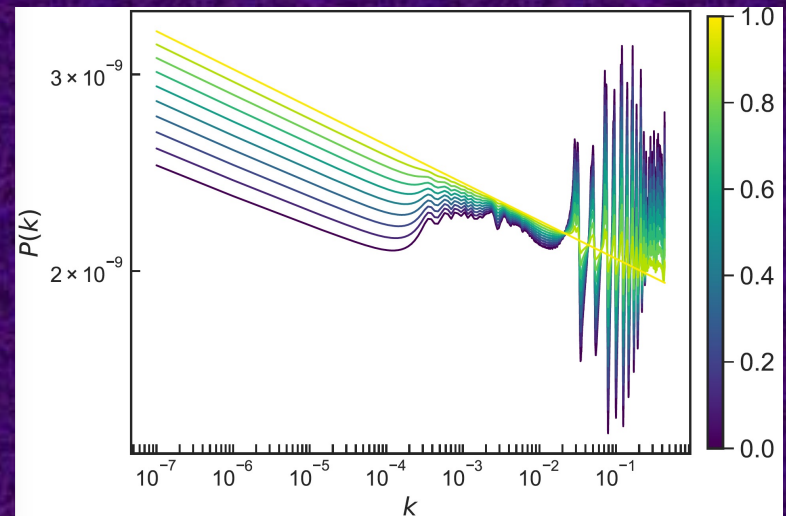




Do we need the high-k features?



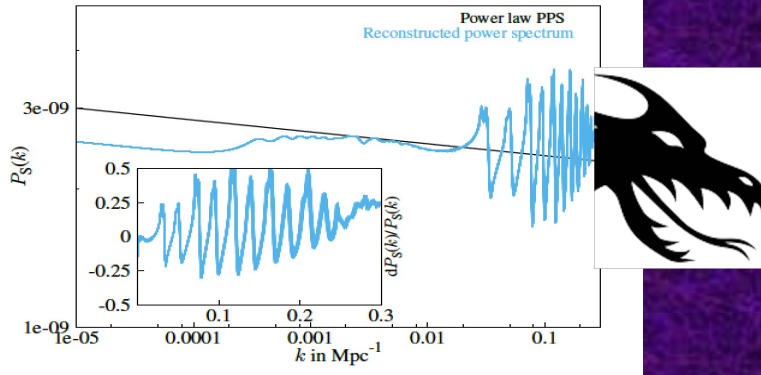
No, a featured decorated HZ should be fine ;)



$H_0 = 71.8 \pm 0.9$  km/s/Mpc.  
 Bayes factor of  $\log K = 5.7$  in favor of the deformation model.

$$P(k, f) = P_{\text{MRL}}(k) + f(P_{\text{PL}}(k) - P_{\text{MRL}}(k)).$$

# Issues:

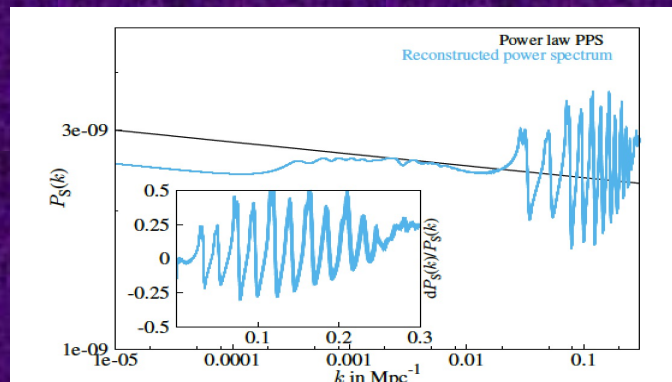


1. Is it **natural** to generate a complex form of the reconstructed PPS within an **inflationary scenario** without extreme fine tuning? However, we do not provide any conclusive reason to close the possibility of a physical early Universe explanation. We are currently searching for such scenarios!
2. Using **polarization data** it should be possible to validate further the possibility of the reconstructed form of the PPS. Likewise, using polarization data we might be able to look for a more optimized form of the PPS to remove tensions from different observations.
3. A wider exploration of the **underlying parameter space** of the cosmological model would be essential to reveal potential routes to ameliorate the disagreements in cosmological parameters inferred.
4. **Need for a comprehensive iterative approach** to derive observational constraints and confront vs theoretical/phenomenological models.
5. **Lensing templates and A\_Lens issue!**

# Issues:

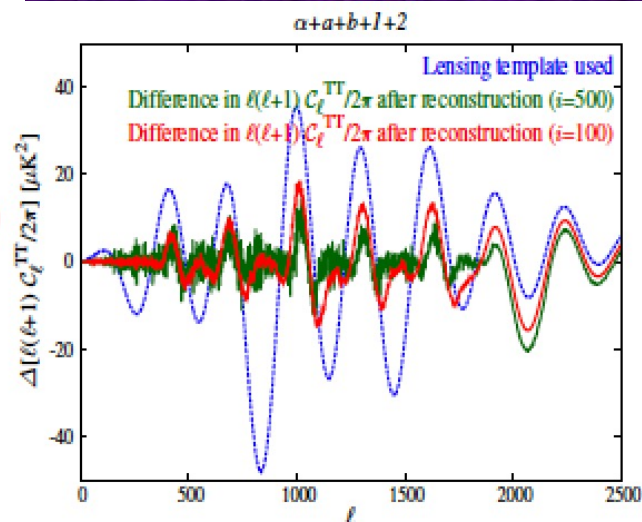
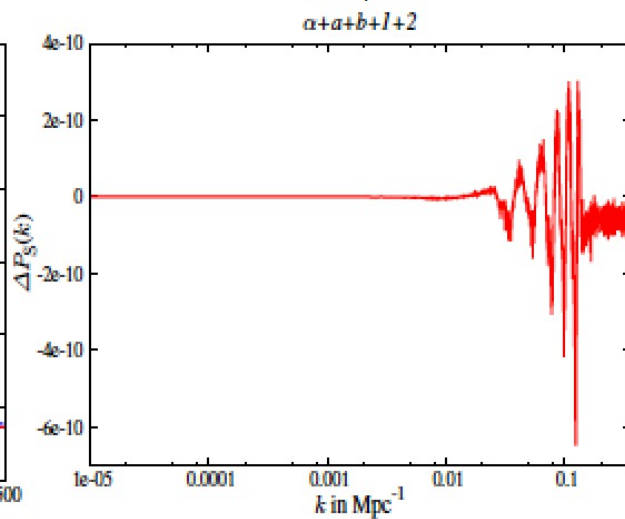
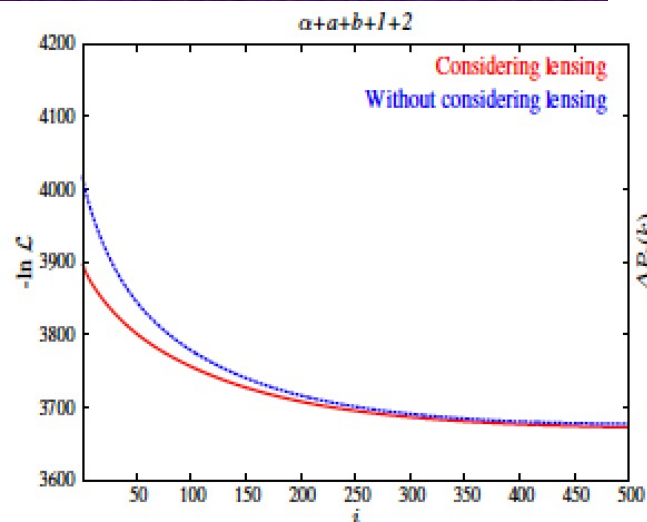
- The features at high  $k$  values are very similar to the features we reconstructed previously when we did not consider CMB lensing (trying to project the effect on the form of the PPS). Can CMB lensing and  $A_{\text{Lens}}$  problem play a key role?

Also see: Kable, Addison, Bennett, arXiv:1809.03983



Hazra, Shafieloo, Souradeep, JCAP 2019

Hazra, Shafieloo, Souradeep, JCAP 2014





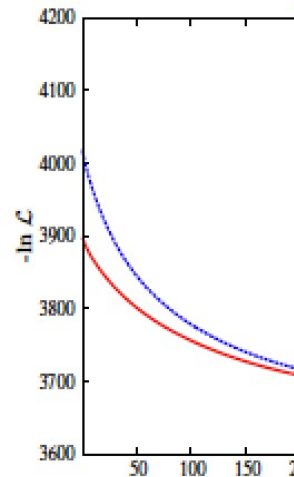
# Issues:

5. The features in the primordial spectrum, CMB lensing, Hubble tension, can there be any connection?

Also see: Kable, *et al.*,  
arXiv:1809.03983

Features in the primordial spectrum, CMB lensing, Hubble tension, can there be any connection?

See talk by Akhil in the afternoon!

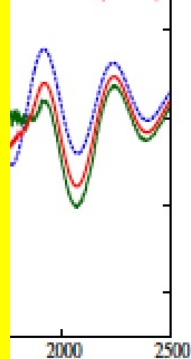


sted  
ect  
/

AP 2019

AP 2014

ing template used  
struction ( $i=500$ )  
struction ( $i=100$ )



# Current Status

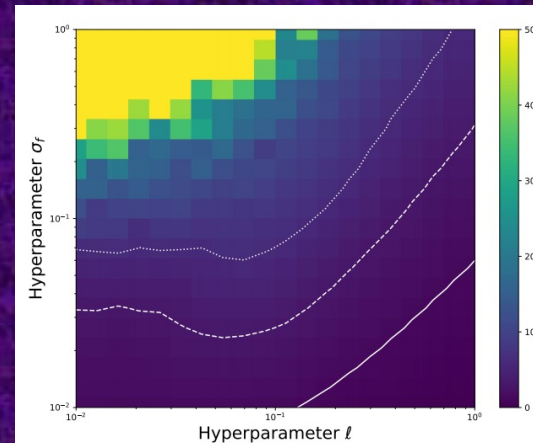
Open problem. Many tensions and hints for various systematics

Many theoretical/phenomenological models are proposed to ease the tensions. None is convincing so far.

Not possible to resolve all problems with minimal modification of the standard model. This has helped the standard model to survive so far.

Model independent consistency test between various data is essential to rule out systematics.

Consistency of SDSS BAO and Pantheon SN Ia data  
Keeley, Shafieloo, Zhao et al, arXiv:2010.03234 [SDSS IV paper]



# Future Perspective

High possibilities for systematics in different data

Need for independent measurements

Two key questions:

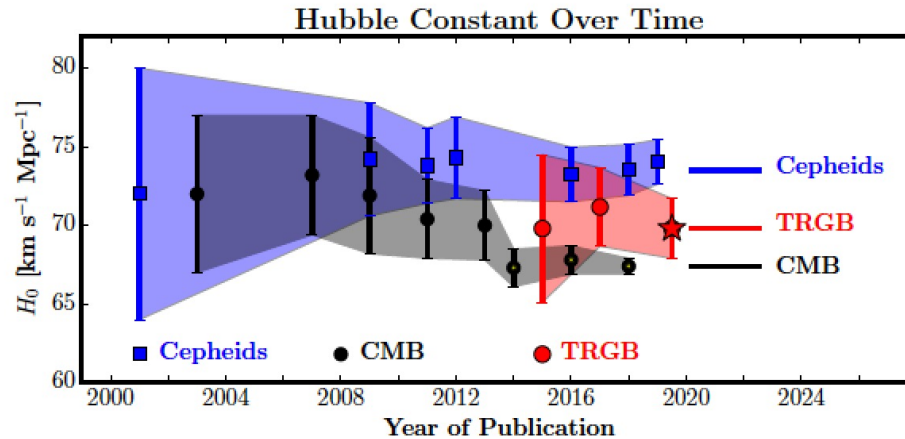
Power-Law Primordial Power Spectrum?

Lambda Dark Energy?



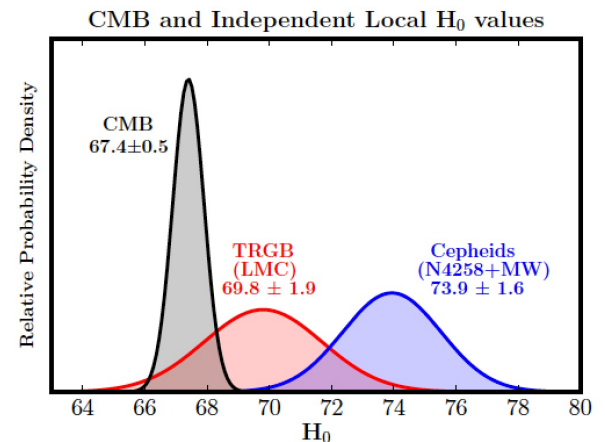
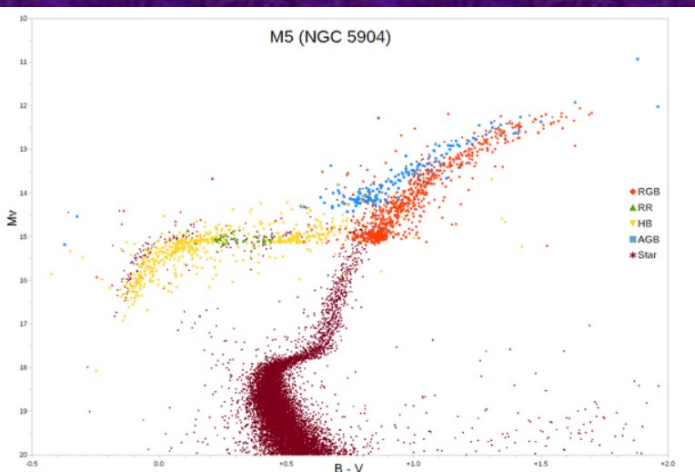
# Tip of the Red Giant Branch

Future  
Perspective



**Figure 17.** A plot of  $H_0$  values as a function of time. The points and shaded region in black are those determined from measurements of the CMB; those in blue are Cepheid calibrations of the local value of  $H_0$ ; and the red points are TRGB calibrations. The red star is the best-fit value obtained in this paper. Error bars are  $1\sigma$ .

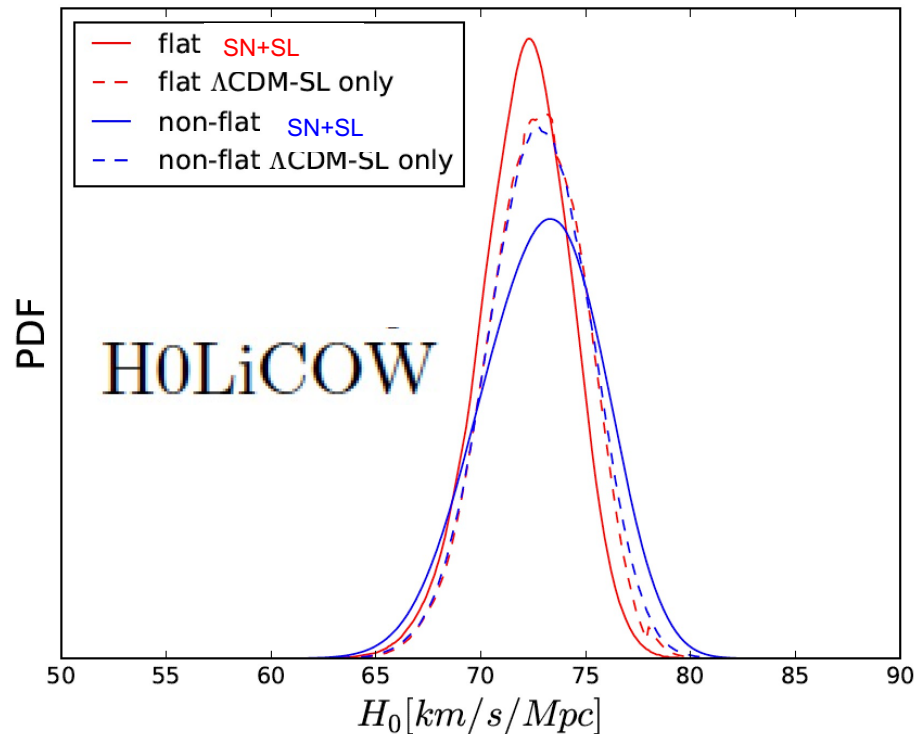
Freedman et al,  
arXiv:1907.05922



**Figure 18.** Completely independent calibrations of  $H_0$ . Shown in red is the probability density function based on our LMC CCHP TRGB calibration of CSP-I SNe Ia; in blue is the Cepheid calibration of  $H_0$  (Riess et al. 2016), using the Milky Way parallaxes and the maser distance to NGC 4258 as anchors (excluding the LMC). The Planck value of  $H_0$  is shown in black.

# H0 from Strongly Lensed systems

Kai, Shafieloo, Keeley, Linder, ApJ Letters 2019  
 Kai, Shafieloo, Keeley, Linder, ApJ Letters 2020  
 Bag, Kim, Linder, Shafieloo, ApJ 2021



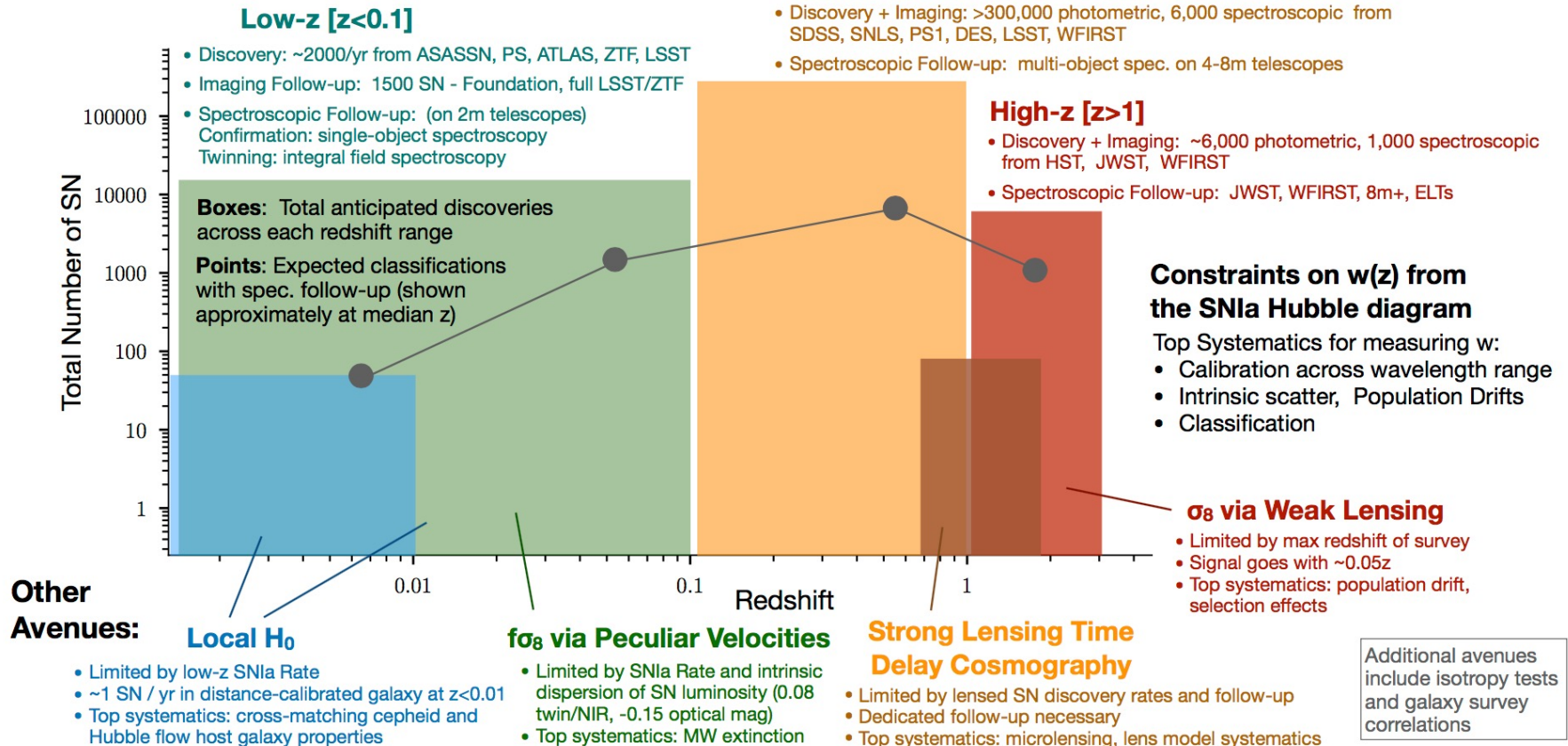
## H0LiCOW I. H0 Lenses in COSMOGRAIL's Wellspring

Suyu et al. MNRAS 2017

Order	Name	$z_L$	$z_S$
1	RXJ1131-1231	0.295	0.654
2	HE 0435-1223	0.4546	1.693
3	B1608+656	0.6304	1.394
4	SDSS 1206+4332	0.745	1.789

# Future perspective (late universe, SN Ia)

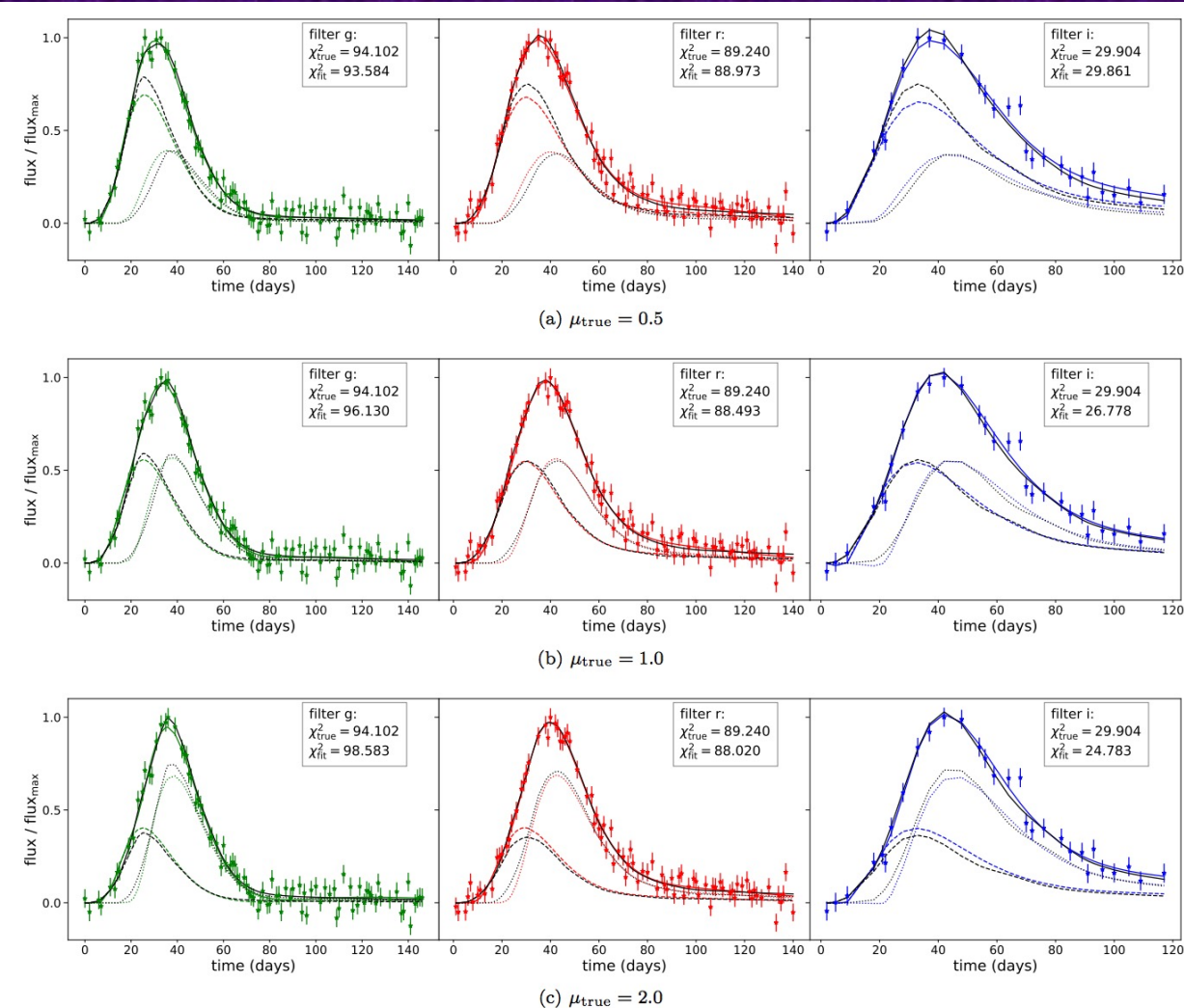
## The Future of SN Ia Cosmology at a Glance



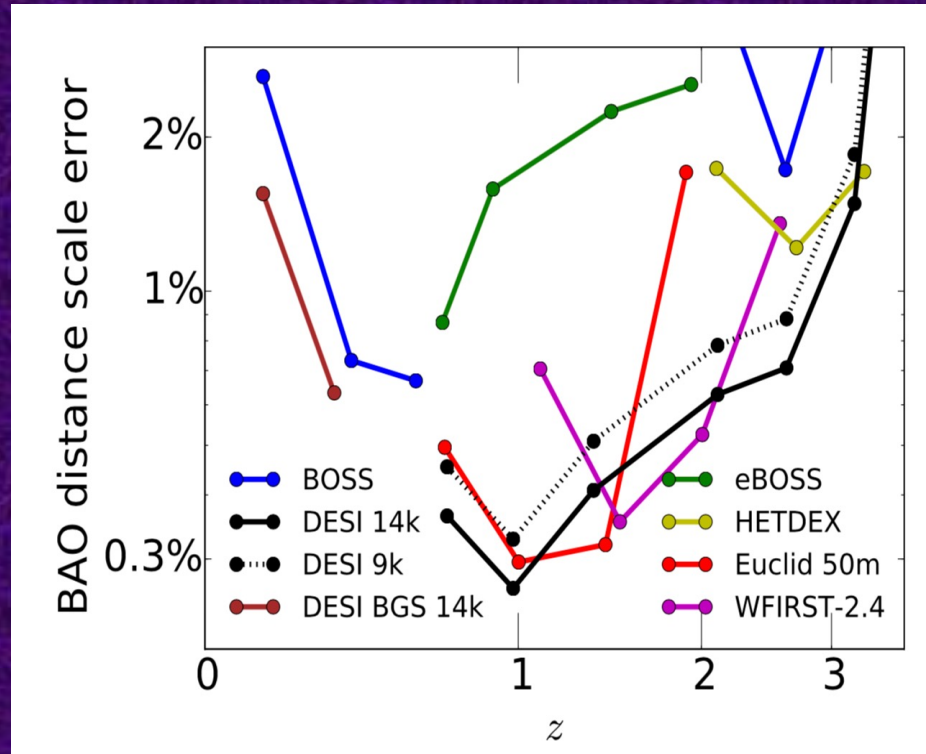
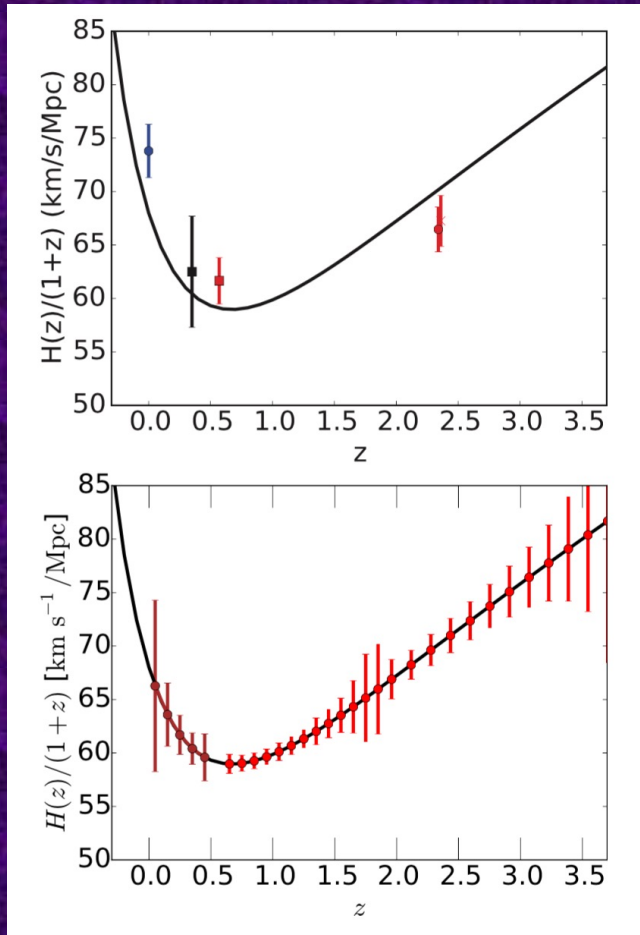


# Future Perspective (late universe, SN Ia SL)

Resolving  
Unresolved  
Lensed  
Systems!

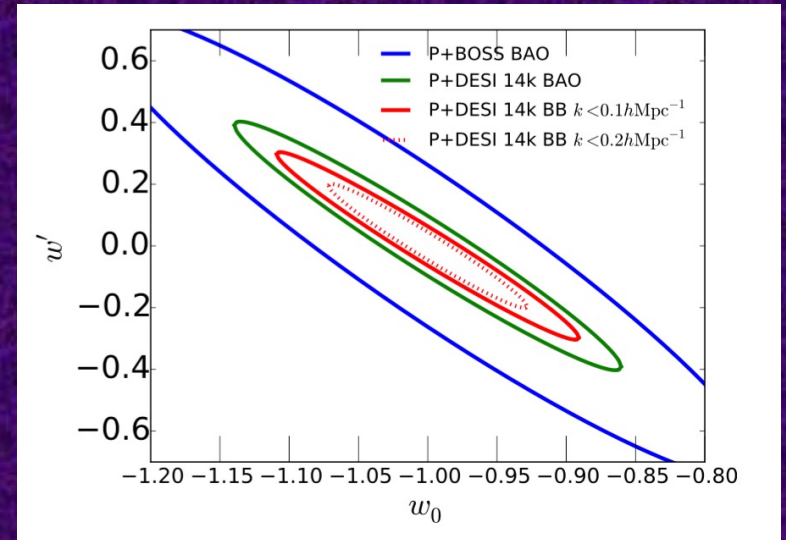
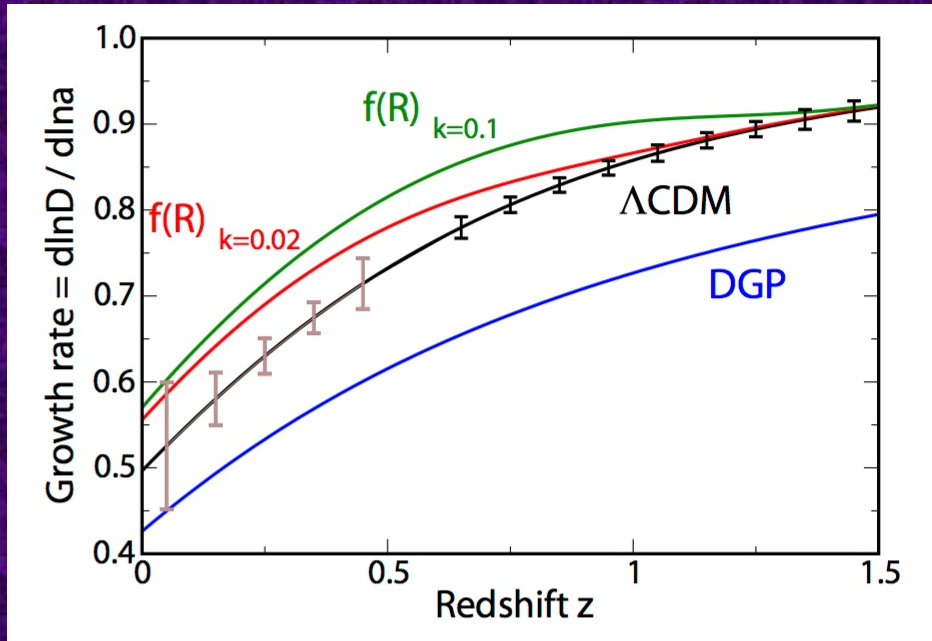


# Future perspective (late universe; BAO)



Aghamousa et al, [arXiv:1611.00036]  
DESI Collaboration

# Future perspective (late universe, RSD)





# Future perspective [G-Waves and Standard Sirens]

## Astro2020

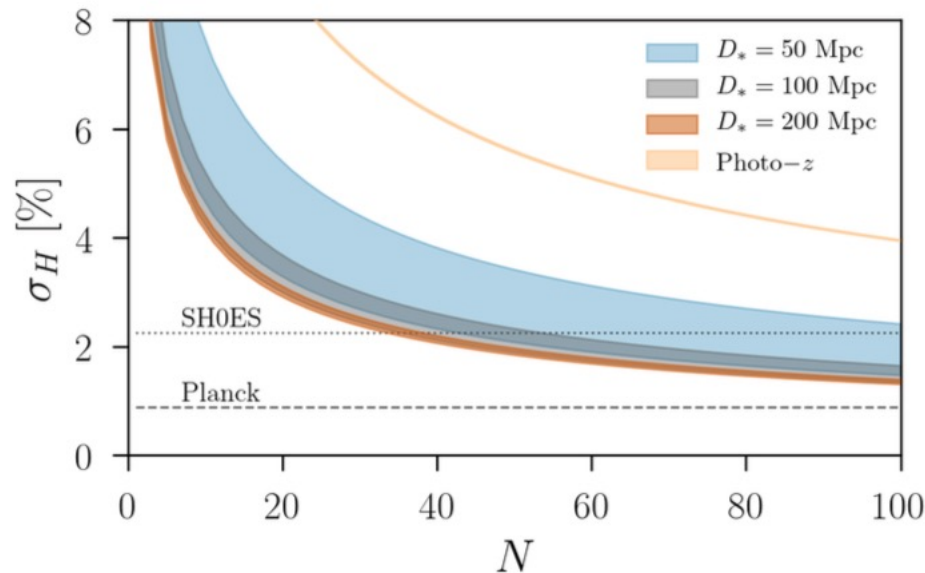


Figure 1: Hubble constant uncertainty ( $1\sigma$ ) as a function of combined GW events with associated EM counterpart. The shaded regions show the impact of the peculiar velocity uncertainty between 100 and 400  $\text{km s}^{-1}$  for different distance reaches  $D_*$ . The latest results from standard candles (SH0ES, [13]) and CMB (Planck, [14]) are also shown.

# Future Perspective (primordial)

## Full picture

Complete reconstruction analysis  
with polarization data

$$C_{\ell}^{TT} = \int \frac{dk}{k} P(k) G_{\ell}^{TT}(k)$$

$$C_{\ell}^{EE} = \int \frac{dk}{k} P(k) G_{\ell}^{EE}(k)$$

$$C_{\ell}^{BB} = \int \frac{dk}{k} P_{\dagger}(k) G_{\ell}^{BB}(k)$$

$$C_{\ell}^{TE} = \int \frac{dk}{k} P(k) G_{\ell}^{TE}(k)$$

Searching for  
correlations!

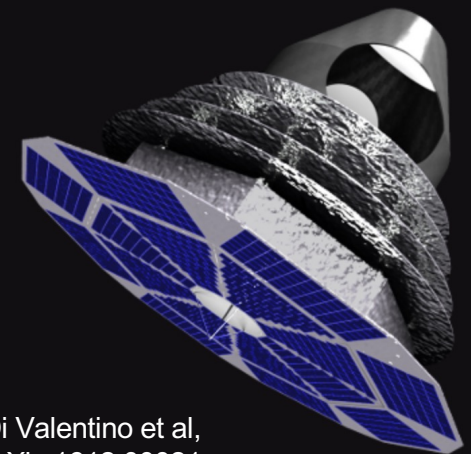
$$P_S(k), P_T(k), P_{iso}(k)$$

Primordial power spectra  
from Early universe

$$G_{\ell}^{TT}(k), G_{\ell}^{EE}(k), G_{\ell}^{BB}(k), G_{\ell}^{TE}(k)$$

Post recombination Radiative  
transport kernels in a given  
cosmology

# Features with Future of CMB (S4)



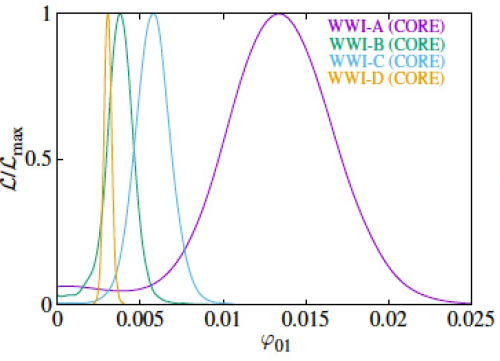
Di Valentino et al, arXiv:1612.00021

## Wiggly Whipped Inflation

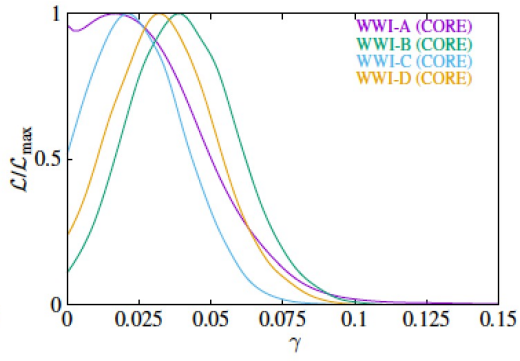
Hazra et al, JCAP 2018  
Debono et al, MNRAS 2020

With Cosmic Origins Explorer (CORE)-like survey specification

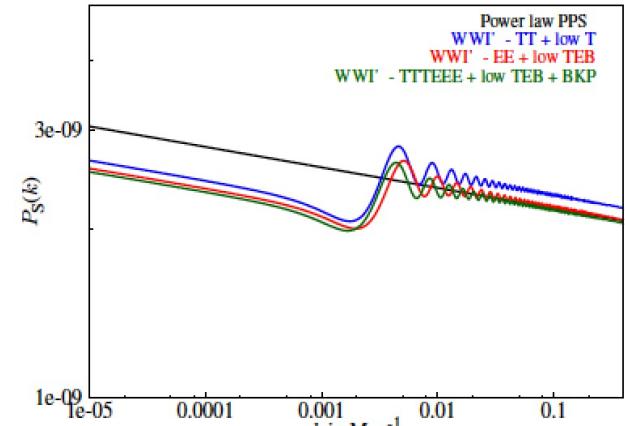
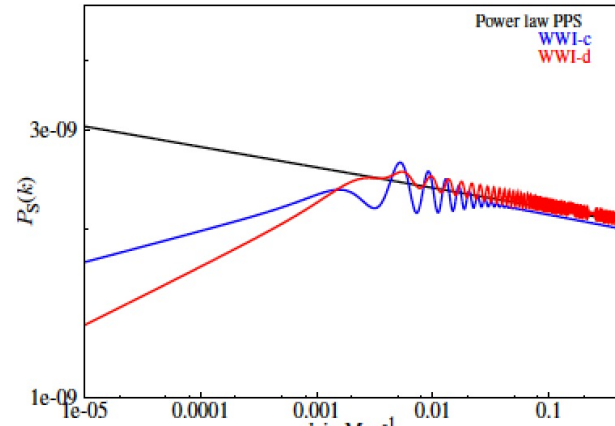
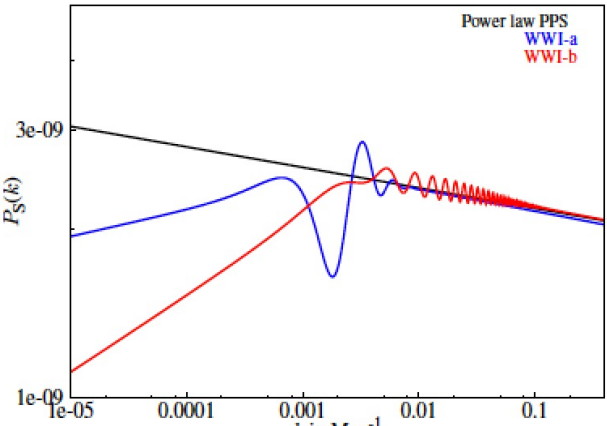
Wiggles



Suppression



- Large scale suppressions can not be detected with high significance
- Some of the intermediate and small scale oscillations can be detected, if present





# Future

# Perspective

# From 2D to 3D

## ***Using LSS data to test early universe scenarios***

1. We need to estimate matter power spectrum but we observe galaxies. Hence we have to model linear clustering bias and estimate its parameters accurately and precisely to connect the observables to theory. Bias modeling would be different for different surveys and susceptible to systematics.
1. Does power spectrum (or bi-spectrum, etc) necessarily contains all the information in 3D data of LSS? Can't reducing dimensionality of the data wash out some information?

# From 2D to 3D

## N-Body Simulation (DESI/Euclid like)

L'Huillier, Shafieloo, Hazra, Starobinsky, MNRAS 2018  
 Hassani, L'Huillier, Shafieloo, Kunz, Adamek, JCAP 2020

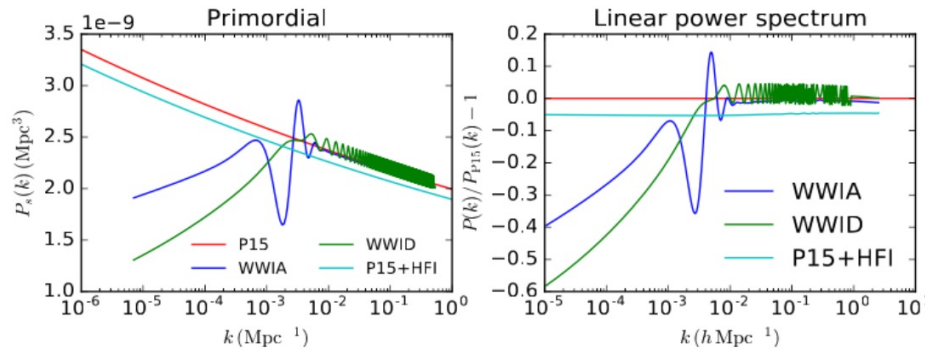
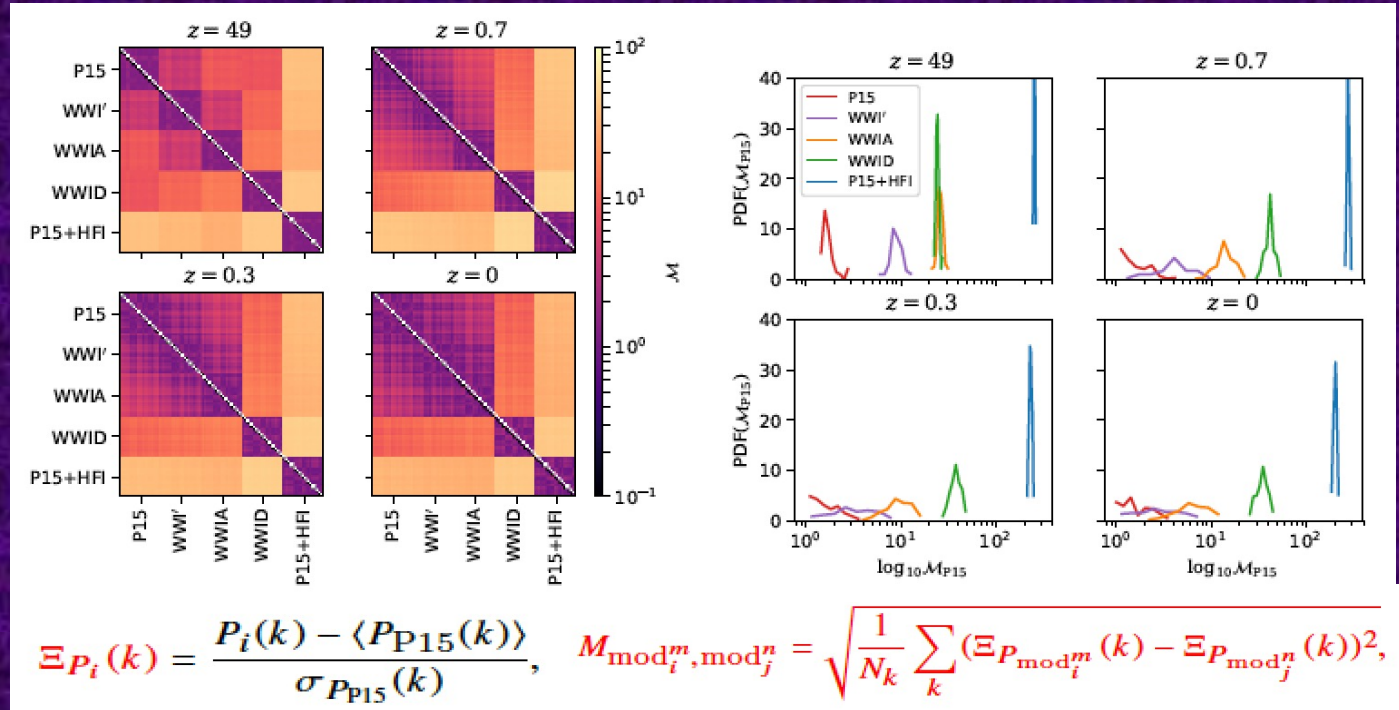


Table 2: Cosmological parameters of models

Model	$\Omega_m$	$H_0$ ( $\text{km s}^{-1} \text{Mpc}^{-1}$ )	$\sigma_8$	$n_s$
P15	0.319	66.93	0.8156	0.9625
WWIA	0.320	66.86	0.8340	NA
WWID	0.318	67.01	0.8419	NA
P15+HFI	0.319	66.93	0.8156	0.9619

*2 point correlation functions and power spectrum unable to distinguish between the models*



$$\Xi_{P_i}(k) = \frac{P_i(k) - \langle P_{P15}(k) \rangle}{\sigma_{P_{P15}}(k)}, \quad M_{\text{mod}_i^m, \text{mod}_j^n} = \sqrt{\frac{1}{N_k} \sum_k (\Xi_{P_{\text{mod}_i^m}}(k) - \Xi_{P_{\text{mod}_j^n}}(k))^2}$$

# From 2D to 3D

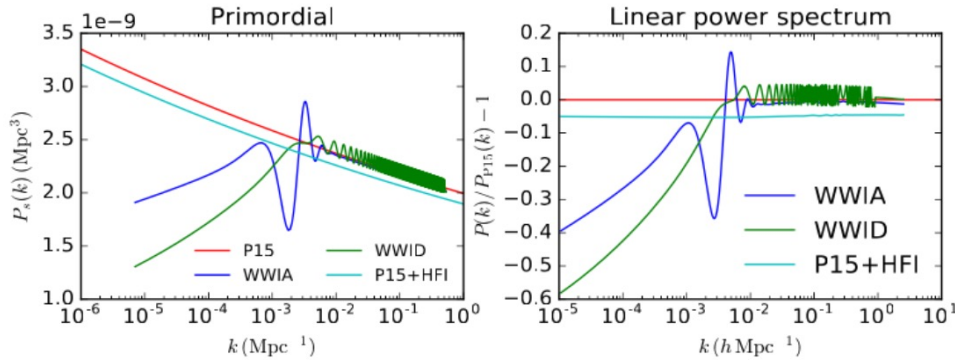
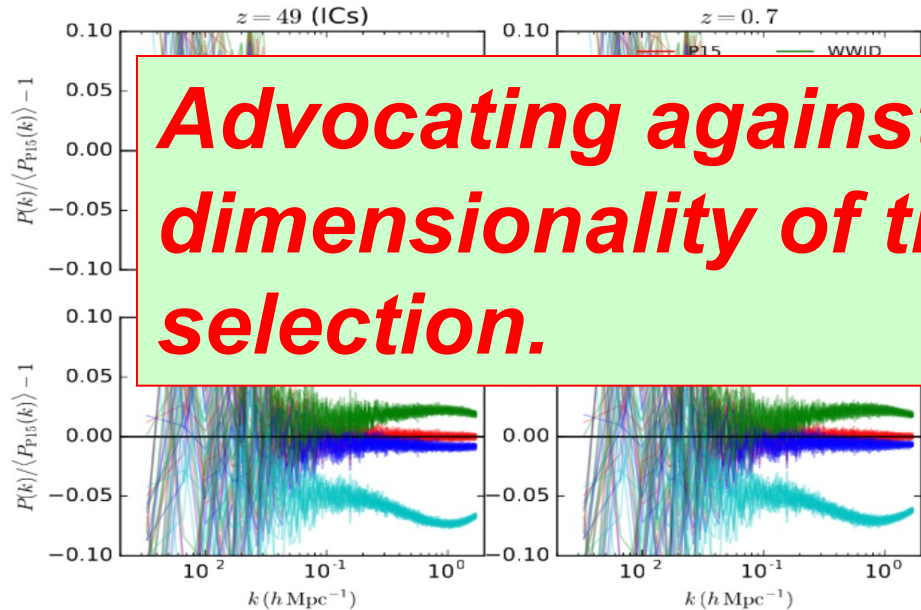


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WWID	0.318	67.01	0.8419	NA
P15+HFI	0.319	66.93	0.8156	0.9619

N-Body Simulation (DESI like)



**Advocating against reducing the dimensionality of the data for model selection.**

(c)  $N_{\text{Mesh}} = 512$  ( $R = 3.69 h^{-1} \text{Mpc}$ )

(d)  $N_{\text{Mesh}} = 1024$  ( $R = 1.85 h^{-1} \text{Mpc}$ )



# Cosmology vs Systematics vs Assumptions

- With higher quality of the data the role of systematics will become more and more prominent.
- Higher precision may cost us uncontrollable bias if we make wrong assumptions.

***What we Should be worried about!***

# Conclusion

- Standard Model of Cosmology fits different data pretty well *individually* but there are tensions fitting different combinations of the data.
- $H_0$  tension (and some others) seems remaining persistent in the context of the  $\Lambda$ CDM model. This can open ways for **competitive alternatives (GEDE?)**.
- ***Tensions are not resolved with minimal extensions of the standard model.*** It is highly possible that there are **systematics** in some of the data and we might need **new physics** too. ***It can be a combination of both!*** New independent measurements and observations can help to clear things up.
- ***First target*** can be testing different aspects of the standard model. If it is not **' $\Lambda$ ' dark energy or 'power-law' primordial spectrum** then we can look further. It is possible to focus the power of the data for the purpose of the falsification. ***Next generation of astronomical observations***, (DESI, Euclid, LSST, WFIRST, SKA(?), etc) will make it much more clear about the status of the concordance model in 2020s.