

Physics Beyond the Standard Model?

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Motivation for BSM Physics

Observational

- What is the observed Dark Matter?
- What generates the neutrino masses?
- What generates the Baryon Asymmetry of the Universe (BAU)?

Theoretical

- SM hierarchy problem (Higgs sector): $M_{EW} \ll M_{Pl}$
- SM flavor problem: $m_e \ll m_t$
- Explained by new dynamics?
 - Extra dimensions (Warped (AdS), Flat)
 - Supersymmetry
 - Strong dynamics
 - Little Higgs



Outline (Supersymmetry)

- Supersymmetry (SUSY) Basics
 - SUSY invariant theory
 - SUSY breaking
- Minimal Supersymmetric Standard Model (MSSM)
 - SUSY preserving Lagrangian and soft-breaking terms
 - R-parity
 - Superpartner Mixing
- Implications
 - Dark Matter
 - 125 GeV Higgs



Outline (Extra Dimensions)

- Aspects of Extra Dimensional Theories
 - Large Extra Dimensions (LED) (aka ADD)
 - Universal Extra Dimensions (UED)
 - Warped Extra Dimensions (WED)
- Kaluza-Klein (KK) expansion
- LHC Signatures



Outline (Dark Matter)

- BSM DM Candidates
- DM Detection
 - Direct detection
 - Indirect detection
 - At colliders

SUPERSYMMETRY

Reviews: [Wess & Bagger] [Martin] [Drees]
[Drees, Godbole, Roy] [Baer, Tata]



Supersymmetry (SUSY)

Reviews: [Wess & Bagger]

Symmetry: Fermions \Leftrightarrow Bosons

$Q |\Phi\rangle = |\Psi\rangle$; $Q |\Psi\rangle = |\Phi\rangle$

Q_α is a spinorial charge

SUSY algebra:

$$\{Q_\alpha, \bar{Q}_{\dot{\beta}}\} = 2\sigma_{\alpha\dot{\beta}}^\mu P_\mu$$

$$\{Q_\alpha, Q_\beta\} = \{\bar{Q}_{\dot{\alpha}}, \bar{Q}_{\dot{\beta}}\} = 0$$

$$[P^\mu, Q_\alpha] = [P^\mu, \bar{Q}_{\dot{\alpha}}] = 0$$



SUSY invariant theory

Under a SUSY transformation

$$\delta_\xi \phi = \sqrt{2} \xi \psi$$

$$\delta_\xi \psi = i\sqrt{2} \sigma^m \bar{\xi} \partial_m \phi + \sqrt{2} \xi F$$

$$\delta_\xi F = i\sqrt{2} \bar{\xi} \bar{\sigma}^m \partial_m \psi$$

$$\delta_\xi A_{mn} = i [(\xi \sigma^n \partial_m \bar{\lambda} + \bar{\xi} \bar{\sigma}^n \partial_m \lambda) - (n \leftrightarrow m)]$$

$$\delta_\xi \lambda = i \xi D + \sigma^{mn} \xi A_{mn}$$

$$\delta_\xi D = \bar{\xi} \bar{\sigma}^m \partial_m \lambda - \xi \sigma^m \partial_m \bar{\lambda}$$

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$$\delta_\xi \lambda = i \xi D + \sigma^{mn} \xi A_{mn}$$

$$\delta_\xi D = \bar{\xi} \bar{\sigma}^m \partial_m \lambda - \xi \sigma^m \partial_m \bar{\lambda}$$

A SUSY invariant action: $S = \int d^4x \mathcal{L}$

$$\begin{aligned} \mathcal{L} = & |D_\mu \phi_i|^2 - i \bar{\psi}_i \sigma_\mu D^\mu \psi_i - g \sqrt{2} \left(\phi_i^* T^a \psi_i \lambda^a + \lambda^{a\dagger} \psi^\dagger T^a \phi_i \right) \\ & - \left(\frac{1}{2} \frac{\partial^2 \mathcal{W}(\phi_i)}{\partial \phi_j \partial \phi_k} \psi_j \psi_k + h.c. \right) - \left| \frac{\partial \mathcal{W}(\phi_i)}{\partial \phi_j} \right|^2 \\ & - \frac{1}{4} F_{\mu\nu}^a F_a^{\mu\nu} - \frac{1}{2} \sum_a |g \phi_i^* T_{ij}^a \phi_j|^2 - i \lambda^{a\dagger} \bar{\sigma}_\mu D^\mu \lambda_a \end{aligned}$$

$\mathcal{W}(\phi_i)$: **Superpotential**, a holomorphic function of the fields



Consequences

Solution to gauge hierarchy problem

$$\begin{array}{c}
 \text{---} h \text{---} \bigcirc \text{---} h \text{---} \\
 \text{---} -i \frac{y_t}{\sqrt{2}} \text{---} \\
 t_L, t_R
 \end{array}
 +
 \begin{array}{c}
 \text{---} h \text{---} \bigcirc \text{---} h \text{---} \\
 \text{---} -i \frac{y_{\tilde{t}}}{2} \text{---} \\
 \tilde{t}_L, \tilde{t}_R
 \end{array}
 = 0$$

Λ^2 divergence cancelled

[Romesh Kaul, '81, '82] [Witten]

(Similarly W^\pm, Z divergences cancelled by $\tilde{\lambda}$)

Consequences

Solution to gauge hierarchy problem

$$\begin{array}{c}
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 \circlearrowleft \\
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 \text{---} \text{---} \text{---} \\
 h \text{---} \text{---} h \\
 -i\frac{y_L^2}{2}
 \end{array}
 = 0$$

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[Romesh Kaul, '81, '82] [Witten]

(Similarly W^\pm, Z divergences cancelled by $\tilde{\lambda}$)

- Lightest SUSY Particle (LSP) stable dark matter (if R_p conserved)
- Gauge Coupling Unification - SUSY $SO(10)$ GUT
Includes $\nu_R \Rightarrow$ Neutrino mass via seesaw

SUSY breaking

- Exact SUSY $\implies M_\psi = M_\phi$; $M_A = M_{\tilde{\chi}}$
 - So experiment \implies **SUSY must be broken**
- SUSY broken if and only if $\langle 0|H|0\rangle > 0$
 - Spontaneous SUSY breaking
 - O’Raifeartaigh F -term breaking
 - Fayet-Iliopoulos D -term breaking
 - $STr(M^2) = 0 \implies$ cannot break SUSY spontaneously using SM superfield
 - Hidden sector breaking $\xleftrightarrow{\text{Mediation}}$ Communicated to SM
Spectrum depends on Mediation type + RGE
- In effective low-energy theory
 - Explicit soft-breaking terms, i.e., with dimensionful parameters



The Minimal Supersymmetric Standard Model (**MSSM**)

Reviews: [Martin] [Drees] [Drees,Godbole,Roy] [Baer,Tata]



MSSM fields

To every SM particle, add a *superpartner* (spin differs by 1/2)

Matter fields (Chiral Superfields)

	$(SU(3), SU(2))_{U(1)}$	Components
Q	$(3, 2)_{1/6}$	(\tilde{q}_L, q_L, F_Q) ; $\tilde{q}_L = \begin{pmatrix} \tilde{u}_L \\ \tilde{d}_L \end{pmatrix}$; $q_L = \begin{pmatrix} u_L \\ d_L \end{pmatrix}$
U^c	$(\bar{3}, 1)_{-2/3}$	$(\tilde{u}_R^*, u_R^c, F_U)$
D^c	$(\bar{3}, 1)_{1/3}$	$(\tilde{d}_R^*, d_R^c, F_D)$
L	$(1, 2)_{-1/2}$	$(\tilde{\ell}_L, \ell_L, F_L)$; $\tilde{\ell}_L = \begin{pmatrix} \tilde{\nu}_L \\ \tilde{e}_L \end{pmatrix}$; $\ell_L = \begin{pmatrix} \nu_L \\ e_L \end{pmatrix}$
E^c	$(1, 1)_1$	$(\tilde{e}_R^*, e_R^c, F_E)$
(N^c)	$(1, 1)_0$	$(\tilde{\nu}_R^*, \nu_R^c, F_N)$

Gauge fields

(Vector Superfields)

	Components
$SU(3)$	(g_μ, \tilde{g}, D_3)
$SU(2)$	(W_μ, \tilde{W}, D_2)
$U(1)$	(B_μ, \tilde{B}, D_1)

Higgs fields (Chiral Superfields)

	$(SU(3), SU(2))_{U(1)}$	Components
H_u	$(1, 2)_{1/2}$	$(h_u, \tilde{h}_u, F_{H_u})$; $h_u = \begin{pmatrix} h_u^+ \\ h_u^0 \end{pmatrix}$; $\tilde{h}_u = \begin{pmatrix} \tilde{h}_u^+ \\ \tilde{h}_u^0 \end{pmatrix}$
H_d	$(1, 2)_{-1/2}$	$(h_d, \tilde{h}_d, F_{H_d})$; $h_d = \begin{pmatrix} h_d^0 \\ h_d^- \end{pmatrix}$; $\tilde{h}_d = \begin{pmatrix} \tilde{h}_d^0 \\ \tilde{h}_d^- \end{pmatrix}$



MSSM Superpotential

Write most general \mathcal{W} consistent with $SU(3)_c \otimes SU(2)_L \otimes U(1)_Y$

- $\mathcal{W} = U^c y_u Q H_u - D^c y_d Q H_d - E^c y_e L H_d + \mu H_u H_d + (N^c y_n L H_u)$
- $\mathcal{W}_{\Delta L} = L H_u + L E^c L + Q D^c L$; $\mathcal{W}_{\Delta B} = U^c D^c D^c$
 - $\mathcal{W}_{\Delta L} + \mathcal{W}_{\Delta B}$ induce proton decay : $\tau_p \sim 10^{-10} s$ for $\tilde{m} \sim 1 \text{ TeV}$



MSSM Superpotential

Write most general \mathcal{W} consistent with $SU(3)_c \otimes SU(2)_L \otimes U(1)_Y$

- $\mathcal{W} = U^c y_u QH_u - D^c y_d QH_d - E^c y_e LH_d + \mu H_u H_d + (N^c y_n LH_u)$
- $\mathcal{W}_{\Delta L} = LH_u + LE^c L + QD^c L$; $\mathcal{W}_{\Delta B} = U^c D^c D^c$
 - $\mathcal{W}_{\Delta L} + \mathcal{W}_{\Delta B}$ induce proton decay : $\tau_p \sim 10^{-10} s$ for $\tilde{m} \sim 1$ TeV

So impose Matter Parity $R_M = (-1)^{3(B-L)}$ to forbid ΔL and ΔB terms

For components \implies **R-parity** $R_p = (-1)^{3(B-L)+2s}$

$R_p(\text{particle}) = +1$, $R_p(\text{sparticle}) = -1$

Consequence : The **Lightest SUSY Particle (LSP) is stable**

- Cosmologically stable Dark Matter
- Missing Energy at Colliders



Soft SUSY breaking

Effective parametrization with explicit soft-SUSY-breaking terms

$$\begin{aligned}
 \mathcal{L}_{SUSY Br}^{soft} \supset & -\tilde{Q}^\dagger \tilde{m}_Q^2 \tilde{Q} - \tilde{u}_R^\dagger \tilde{m}_u^2 \tilde{u}_R - \tilde{d}_R^\dagger \tilde{m}_d^2 \tilde{d}_R - \tilde{L}^\dagger \tilde{m}_L^2 \tilde{L} - \tilde{e}_R^\dagger \tilde{m}_e^2 \tilde{e}_R - (\tilde{\nu}_R^\dagger \tilde{m}_\nu^2 \tilde{\nu}_R) \\
 & - \frac{1}{2} M_1 \tilde{B} \tilde{B} - \frac{1}{2} M_2 \tilde{W} \tilde{W} - \frac{1}{2} M_3 \tilde{g} \tilde{g} + h.c. \\
 & - \tilde{u}^c A_u \tilde{Q} H_u + \tilde{d}^c A_d \tilde{Q} H_d + \tilde{e}^c A_e \tilde{L} H_d - (\tilde{\nu}^c A_\nu \tilde{L} H_u) + h.c. \\
 & - m_{H_u}^2 H_u^\dagger H_u - m_{H_d}^2 H_d^\dagger H_d - (B\mu H_u H_d + h.c.)
 \end{aligned}$$



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 & - \frac{1}{2} M_1 \tilde{B} \tilde{B} - \frac{1}{2} M_2 \tilde{W} \tilde{W} - \frac{1}{2} M_3 \tilde{g} \tilde{g} + h.c. \\
 & - \tilde{u}^c A_u \tilde{Q} H_u + \tilde{d}^c A_d \tilde{Q} H_d + \tilde{e}^c A_e \tilde{L} H_d - (\tilde{\nu}^c A_\nu \tilde{L} H_u) + h.c. \\
 & - m_{H_u}^2 H_u^\dagger H_u - m_{H_d}^2 H_d^\dagger H_d - (B\mu H_u H_d + h.c.)
 \end{aligned}$$

UV SUSY breaking and mediation dynamics will set these parameters

- Eg: Gravity Mediation (MSUGRA, CMSSM)
 - Inputs $\tilde{m}_0, M_{1/2}, A_0, \tan\beta, \text{sign}(\mu)$ at GUT scale
 - TeV scale values determined by RGE



Electroweak symmetry breaking (EWSB)

$$\langle H_u \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v_u \end{pmatrix}; \quad \langle H_d \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} v_d \\ 0 \end{pmatrix}; \quad v^2 = v_u^2 + v_d^2; \quad \tan \beta \equiv \frac{v_u}{v_d};$$

Physical Higgses: h^0, H^0, A^0, H^\pm



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Physical Higgses: h^0, H^0, A^0, H^\pm

$$\mathcal{V} = (|\mu|^2 + m_{H_u}^2)|h_u|^2 + (|\mu|^2 + m_{H_d}^2)|h_d|^2 - (b_\mu h_u h_d + h.c.) + \frac{1}{8}(g^2 + g'^2)(|h_u|^2 - |h_d|^2)^2$$

Minimization and EWSB

$$\sin(2\beta) = \frac{2b_\mu}{m_{H_u}^2 + m_{H_d}^2 + 2|\mu|^2} \quad \text{and} \quad m_Z^2 = \frac{|m_{H_d}^2 - m_{H_u}^2|}{\sqrt{1 - \sin^2(2\beta)}} - m_{H_u}^2 - m_{H_d}^2 - 2|\mu|^2$$

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Physical Higgses: h^0, H^0, A^0, H^\pm

$$\mathcal{V} = (|\mu|^2 + m_{H_u}^2)|h_u|^2 + (|\mu|^2 + m_{H_d}^2)|h_d|^2 - (b_\mu h_u h_d + h.c.) + \frac{1}{8}(g^2 + g'^2)(|h_u|^2 - |h_d|^2)^2$$

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$$\sin(2\beta) = \frac{2b_\mu}{m_{H_u}^2 + m_{H_d}^2 + 2|\mu|^2} \quad \text{and} \quad m_Z^2 = \frac{|m_{H_d}^2 - m_{H_u}^2|}{\sqrt{1 - \sin^2(2\beta)}} - m_{H_u}^2 - m_{H_d}^2 - 2|\mu|^2$$

- So we need μ^2 (SUSY preserving param) $\sim m^2$ (SUSY br param)! Why?
 - This is called the **μ -problem**



125 GeV Higgs

At 1-loop

$$m_h^2 \approx m_Z^2 \cos^2(2\beta) + \frac{3g_2^2 m_t^4}{8\pi^2 m_W^2} \left[\ln \left(\frac{m_{\tilde{t}_1} m_{\tilde{t}_2}}{m_t^2} \right) + \frac{X_t^2}{m_{\tilde{t}_1} m_{\tilde{t}_2}} \left(1 - \frac{X_t^2}{12m_{\tilde{t}_1} m_{\tilde{t}_2}} \right) \right]$$

[Haber, Hempfling, Hoang ,1997]

where $X_t = A_t - \mu \cot \beta$

- $m_h = 125$ GeV needs sizable loop contribution

- Hard! Needs large $m_{\tilde{t}_1} m_{\tilde{t}_2}$ or large X_t^2

- But $\delta m_{H_u}^2 \approx \frac{3g_2^2 m_t^4}{8\pi^2 m_W^2} \left[\ln \left(\frac{m_{\tilde{t}_1} m_{\tilde{t}_2}}{m_t^2} \right) + \frac{X_t^2}{2m_{\tilde{t}_1} m_{\tilde{t}_2}} \left(1 - \frac{X_t^2}{6m_{\tilde{t}_1} m_{\tilde{t}_2}} \right) \right]$

So fine-tuning necessary to keep m_Z^2 correct (cf previous EWSB relation)
 “Little hierarchy problem”



Neutralino mixing

Neutralino: Neutral EW gauginos (\tilde{B} , \tilde{W}^3 , \tilde{H}_u^0 , \tilde{H}_d^0) : Majorana states

$$\mathcal{L} \supset -\frac{1}{2} (\tilde{B} \ \tilde{W}^3 \ \tilde{H}_u^0 \ \tilde{H}_d^0) \begin{pmatrix} M_1 & 0 & -c_\beta s_W m_Z & s_\beta s_W m_Z \\ 0 & M_2 & c_\beta c_W m_Z & -s_\beta c_W m_Z \\ -c_\beta s_W m_Z & c_\beta c_W m_Z & 0 & -\mu \\ s_\beta s_W m_Z & -s_\beta c_W m_Z & -\mu & 0 \end{pmatrix} \begin{pmatrix} \tilde{B} \\ \tilde{W}^3 \\ \tilde{H}_u^0 \\ \tilde{H}_d^0 \end{pmatrix}$$

Diagonalizing this $\begin{pmatrix} \tilde{B} \\ \tilde{W}^3 \\ \tilde{H}_u^0 \\ \tilde{H}_d^0 \end{pmatrix} \rightarrow \begin{pmatrix} \tilde{\chi}_1^0 \\ \tilde{\chi}_2^0 \\ \tilde{\chi}_3^0 \\ \tilde{\chi}_4^0 \end{pmatrix}$: the mass eigenstates

Chargino mixing

Chargino: Charged EW gauginos ($\tilde{W}^\pm, \tilde{H}^\pm$), $\tilde{W}^\pm = \tilde{W}_1 \pm i\tilde{W}_2$

Form Dirac states $\tilde{W}^+ = \begin{pmatrix} \tilde{W}_\alpha^+ \\ \tilde{W}^{-\dot{\alpha}} \end{pmatrix}$; $\tilde{H}^+ = \begin{pmatrix} \tilde{H}_u^+ \\ \tilde{H}_d^{-\dot{\alpha}} \end{pmatrix}$

$\mathcal{L} \supset -(\overline{\tilde{W}^+} \overline{\tilde{H}^+}) (M_\chi P_L + M_\chi^\dagger P_R) \begin{pmatrix} \tilde{W}^+ \\ \tilde{H}^+ \end{pmatrix} + h.c.$

$$\text{where } M_\chi = \begin{pmatrix} M_2 & \sqrt{2} \sin \beta m_W \\ \sqrt{2} \cos \beta m_W & \mu \end{pmatrix}$$

Diagonalizing this $\begin{pmatrix} \tilde{W}^+ \\ \tilde{H}^+ \end{pmatrix} \rightarrow \begin{pmatrix} \tilde{\chi}_1^+ \\ \tilde{\chi}_2^+ \end{pmatrix}$: the mass eigenstates

Scalar mixing

Eg. stop sector $(\tilde{t}_L, \tilde{t}_R)$

$$\mathcal{L} \supset - (\tilde{t}_L^* \tilde{t}_R^*) \begin{pmatrix} \tilde{m}_{LL}^2 + m_t^2 + \Delta_L & (v_u A_t - \mu^* \cot \beta m_t)^* \\ (v_u A_t - \mu^* \cot \beta m_t) & \tilde{m}_{RR}^2 + m_t^2 + \Delta_R \end{pmatrix} \begin{pmatrix} \tilde{t}_L \\ \tilde{t}_R \end{pmatrix}$$

$$\text{where } \Delta = (T_3 - Q_S^2) \cos(2\beta) m_Z^2$$

Diagonalizing this $\begin{pmatrix} \tilde{t}_L \\ \tilde{t}_R \end{pmatrix} \rightarrow \begin{pmatrix} \tilde{t}_1 \\ \tilde{t}_2 \end{pmatrix}$: the mass eigenstates



Flavor Probes

FCNC (Mixing, Rare decays) and Precision probes

- Kaon observable, B-factories (BaBar, Belle)
- $(g - 2)_\mu$, EDM, ...

Flavor Problem

- In general \tilde{m}_{ij} can have arbitrary flavor structure and phases (MSSM has 9 new phases + 1 CKM phase)
 - FCNC & EDM experiments severely constrain these
 - some deeper reason (in SUSY br mediation)?
 - Minimal Flavor Violation (MFV)
 - Only CKM phase
 - *Need experimental guidance*



EXTRA DIMENSION(S)



Large Extra Dimensions (LED, ADD)

[Arkani-Hamed, Dimopoulos, Dvali (ADD), 1998]

n (compact) space extra dims with Radius R
(in addition to the usual 3+1 dims)

- Only fundamental scale $M_* \sim 1 \text{ TeV}$

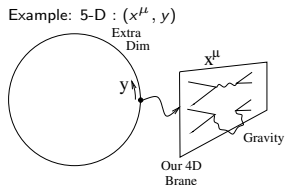
$$M_{pl}^2 = M_*^{2+n} V_n \quad V_n \sim R^n$$

- Gravity in bulk, SM on brane

$$S = \int d^4x d^n y \left[\mathcal{L}_{\text{Bulk}} + \delta(\underline{y}) \mathcal{L}_{\text{Brane}} \right]$$

- Gravitational potential modified to

$$V(r) \sim 1/r^{n+1}$$



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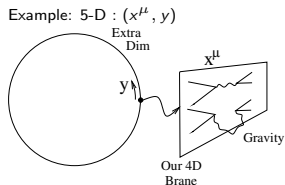
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Some implications

- for $n = 1$, $R = 10^{11} m$
 - excluded by solar system tests!
- for $n = 2$, $R \sim 100 \mu m$
 - Cavendish type experiments limit $M_* > 4 \text{ TeV}$



Universal Extra Dimensions (UED)

[Appelquist, Cheng, Dobrescu] [Cheng, Matchev, Schmaltz] [Datta, Kong, Matchev]

All SM fields propagate in Extra Dimension(s)

- No solution to the hierarchy problem
- KK parity conserved
 - Relaxed constraints since no tree level contribution to EW precision obs
 - $M_{KK} \gtrsim 400 \text{ GeV}$
 - LKP stable!
 - Dark Matter
 - Missing energy at Colliders

[Servant, Tait]



Warped Extra Dimensions (WED, RS)

SM in background 5D warped AdS space

[Randall, Sundrum 99]

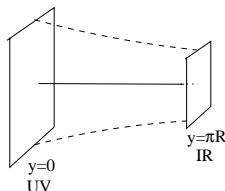
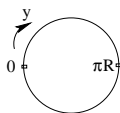
$$ds^2 = e^{-2k|y|}(\eta_{\mu\nu} dx^\mu dx^\nu) + dy^2$$

Z_2 orbifold fixed points:

- Planck (UV) Brane
- TeV (IR) Brane

R : radius of Ex. Dim.

k : AdS curvature scale ($k \lesssim M_{pl}$)



Hierarchy prob soln:

- IR localized Higgs : $M_{EW} \sim ke^{-k\pi R}$: Choose $k\pi R \sim 34$
 - CFT dual is a composite Higgs model

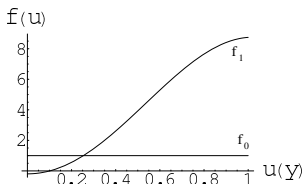
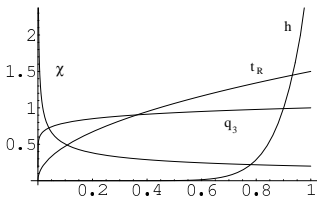
Explaining SM (gauge & mass) hierarchies (WED)

Bulk Fermions explain SM mass hierarchy

[Gherghetta, Pomarol 00][Grossman, Neubert 00]

$$S^{(5)} \supset \int d^4x dy \left\{ c_\psi k \bar{\Psi}(x, y) \Psi(x, y) \right\}$$

Fermion bulk mass (c_ψ parameter) controls $f^\psi(y)$ localization



RS-GIM keeps FCNC under control

For details, see our review: [Davoudiasl, SG, Ponton, Santiago, New
J.Phys.12:075011,2010. arXiv:0908.1968 [hep-ph]]

AdS/CFT Correspondence

AdS/CFT Correspondence

[Maldacena, 1997]

- A classical supergravity theory in $AdS_5 \times S_5$ at weak coupling is **dual** to a 4D large-N CFT at strong coupling
- The CFT is at the boundary of AdS [Witten 1998; Gubser, Klebanov, Polyakov 1998]

$$Z_{CFT}[\phi_0] = e^{-\Gamma_{AdS}[\phi_0]}$$

$S \supset \int d^4x \mathcal{O}_{CFT}(x) \phi_0(x)$ Eg: $\langle \mathcal{O}(x_1) \mathcal{O}(x_2) \rangle = \frac{\delta^2 Z_{CFT}[\phi_0]}{\delta \phi_0(x_1) \delta(x_2)}$ with Z_{CFT} given by the RHS	$\Gamma_{AdS}[\phi]$ supergravity eff. action $\phi(y, x)$ is a solution of the EOM ($\delta\Gamma = 0$) for given bndry value $\phi_0(x) = \phi(y = y_0, x)$
--	---



4D Duals of Warped Models

[Arkani-Hamed, Porrati, Randall, 2000; Rattazzi, Zaffaroni, 2001]

- Dual of Randall-Sundrum model **RS1 (SM on IR Brane)**
 - Planck brane \implies UV Cutoff; Dynamical gravity in the 4D CFT
 - TeV (IR) brane \implies IR Cutoff; Conformal invariance broken below a TeV
 - All SM fields are composites of the CFT

- Dual of Warped Models with **Bulk SM**
 - UV localized fields are elementary
 - IR localized fields (Higgs) are composite
 - 4D dual is Composite Higgs model
 - Shares many features with Walking Extended Technicolor

- Partial Compositeness
 - AdS dual is weakly coupled and hence calculable!

- KK states are dual to composite resonances

[Georgi, Kaplan 1984]



Kaluza-Klein (KK) expansion

Eg: 5-Dimensional theory : Bulk fields : $\Phi(x, y) = \{A_M, \phi, \Psi, \dots\}$

$$\mathcal{S} = \int d^4x dy \mathcal{L}^{(5)} \quad ; \quad \mathcal{L}_\phi^{(5)} \supset \partial^M \phi^\dagger \partial_M \phi - m_\phi^2 \phi^\dagger \phi$$

$$\delta S^{(5)} = 0 \quad \implies \quad \text{Euler-Lagrange Equations of Motion (EOM)} : \quad \frac{\delta \mathcal{L}^{(5)}}{\delta \Phi} = \partial_M \frac{\delta \mathcal{L}^{(5)}}{\delta \partial_M \Phi}$$



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KK expansion: expand in a complete set of states $f_n(y)$

$$\Phi(x, y) = \sum_{n=0}^{\infty} \phi^{(n)}(x) f^{(n)}(y) \quad \text{with} \quad \int dy f^{(n)}(y) f^{(m)}(y) = \delta_{nm}$$



Kaluza-Klein (KK) expansion

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Plug into EOM, y dependent piece is $\left[-\partial_y^2 + \hat{M}_\phi^2 \right] f_{(n)}(y) = m_n^2 f_n(y)$

$$\text{The solution is } f_{(n)}(y) = \frac{1}{N_n} e^{im_n y} \quad ; \quad m_n = \frac{n}{R}$$

Plug in the KK expansion into 5D action and integrate over y

$$\mathcal{S} = \int d^4x \left[\sum_{n=-\infty}^{\infty} \left(\partial^\mu \phi^{(n)*} \partial_\mu \phi^{(n)} - m_n^2 \phi^{(n)*} \phi^{(n)} \right) \right]$$

Is the **equivalent 4D theory**
with an *infinite* tower of states (the **KK states**)



Equivalent 4D theory (with interactions)

Similar procedure for interactions also

$$\mathcal{S}^{(4)} \supset \sum \int d^4x \, m_n^2 \phi^{(n)} \phi^{(n)} + g_{4D}^{(nm)} \psi^{(n)} \psi^{(m)} A^{(l)} + \lambda_{4D}^{(nm)} \psi_L^{(n)} \psi_R^{(m)} H$$

$\phi^{(n)} \rightarrow$ KK tower with mass m_n ; Denote $\phi^{(1)} \equiv \phi'$; $m_1 \equiv m_{KK} \sim \text{TeV}$
(for WED)

Some 4D couplings

- Yukawas: $\lambda_{4D}^{(00)} = \lambda_{5D} \int dy \, f_0^{\psi L} f_0^{\psi R} f^H$
- Gauge couplings: $g_{4D}^{(001)} = g_{5D} \int dy \, f_0^{\psi} f_0^{\psi} f_1^A$



Equivalent 4D theory (with interactions)

Similar procedure for interactions also

$$S^{(4)} \supset \sum \int d^4x \, m_n^2 \phi^{(n)} \phi^{(n)} + g_{4D}^{(nml)} \psi^{(n)} \psi^{(m)} A^{(l)} + \lambda_{4D}^{(nm)} \psi_L^{(n)} \psi_R^{(m)} H$$

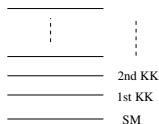
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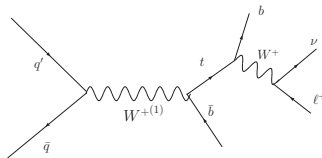
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- Gauge couplings: $g_{4D}^{(001)} = g_{5D} \int dy \, f_0^{\psi} f_0^{\psi} f_1^A$

In summary

- 5D (compact) field \leftrightarrow "Infinite" tower of 4D fields
- Look for this tower at the LHC

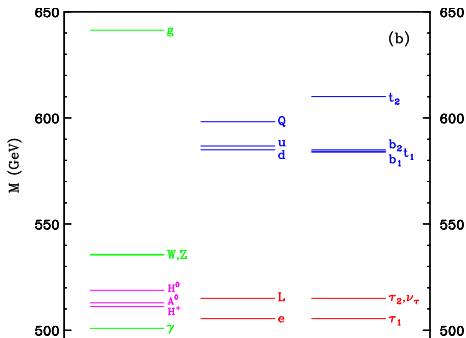


Example:



UED Spectrum

- All KK states degenerate at leading order
 - Loop corrections split this



[Cheng, Matchev, Schmaltz]

LHC SUSY ↔ UED confusion!

[Cheng, Matchev, Schmaltz: 2002]



4-D KK couplings in WED

$$\xi \equiv \sqrt{k\pi R} \approx 5$$

Compare to SM couplings:

- ξ enhanced: $t_R t_R A', hhA', \phi\phi A'$
- $1/\xi$ suppressed: $\psi_{light} \psi_{light} A'_{++}$
- SM strength: $t_L t_L A'$

(Equivalence Theorem $\Rightarrow \phi \leftrightarrow A_L$)

Note: $\psi_{light} \psi_{light} A'_{-+} = 0$



4-D KK couplings in WED

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- $1/\xi$ suppressed: $\psi_{light} \psi_{light} A'_{++}$ Note: $\psi_{light} \psi_{light} A'_{-+} = 0$
- SM strength: $t_L t_L A'$

Effective coupling (Eg: Z'):

$$\mathcal{L}^{4D} \supset \bar{\psi}_{L,R} \gamma^\mu \left[eQ \mathcal{I} A_{1\mu} + g_Z \left(T_L^3 - s_W^2 T_Q \right) \mathcal{I} Z_{1\mu} + g_{Z'} \left(T_R^3 - s'^2 T_Y \right) \mathcal{I} Z_{X1\mu} \right] \psi_{L,R}$$



Challenge I : Precision EW Constraints in WED



Precision Electroweak Constraints (S, T, $Zb\bar{b}$)

- Bulk gauge symm - $SU(2)_L \times U(1)$ (SM ψ , H on TeV Brane)
 - T parameter $\sim (\frac{v}{M_{KK}})^2 (k\pi R)$ [Csaki, Erlich, Terning 02]
 - S parameter also $(k\pi R)$ enhanced

- AdS bulk gauge symm $SU(2)_R \Leftrightarrow$ CFT Custodial Symm [Agashe, Delgado, May, Sundrum 03]
 - T parameter - Protected
 - S parameter - $\frac{1}{k\pi R}$ for light bulk fermions
 - Problem: $Zb\bar{b}$ shifted

- 3rd gen quarks (2,2) [Agashe, Contino, DaRold, Pomarol 06]
 - $Zb\bar{b}$ coupling - Protected
 - Precision EW constraints $\Rightarrow M_{KK} \gtrsim 2 - 3$ TeV

[Carena, Ponton, Santiago, Wagner 06,07] [Bouchart, Moreau-08] [Djouadi, Moreau, Richard 06]



WED Bulk Gauge Group

[Agashe, Delgado, May, Sundrum 03]

Bulk gauge group : $SU(3)_{QCD} \otimes SU(2)_L \otimes SU(2)_R \otimes U(1)_X$

- 8 gluons
- 3 neutral EW (W_L^3, W_R^3, X)
- 2 charged EW (W_L^\pm, W_R^\pm)



WED Bulk Gauge Group

[Agashe, Delgado, May, Sundrum 03]

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- 8 gluons
- 3 neutral EW (W_L^3, W_R^3, X)
- 2 charged EW (W_L^\pm, W_R^\pm)

Gauge Symmetry breaking:

- By Boundary Condition (BC):
 - $SU(2)_R \times U(1)_X \rightarrow U(1)_Y$
- By VEV of TeV brane Higgs
 - $SU(2)_L \times U(1)_Y \rightarrow U(1)_{EM}$

$$A_{-+}(x, y) \text{ BC: } A|_{y=0} = 0; \quad \partial_y A|_{y=\pi R} = 0$$

$$\text{Higgs } \Sigma = (2, 2)$$



Fermion representation : $Zb\bar{b}$ not protected

[Agashe, Delgado, May, Sundrum '03]

- Complete $SU(2)_R$ multiplet : Doublet t_R (DT) model
 - $Q_L \equiv (\mathbf{2}, \mathbf{1})_{1/6} = (t_L, b_L)$
 - $\psi_{t_R} \equiv (\mathbf{1}, \mathbf{2})_{1/6} = (t_R, b')$
 - $\psi_{b_R} \equiv (\mathbf{1}, \mathbf{2})_{1/6} = (t', b_R)$
 - "Project-out" b' , t' zero-modes by $(-, +)$ B.C.
 - New $\psi_{VL} : b', t'$
- $b \leftrightarrow b'$ mixing
 - $Zb\bar{b}$ coupling shifted
 - So LEP constraint quite severe



Fermion representation : $Zb\bar{b}$ protected

- $Q_L = (2, 2)_{2/3} = \begin{pmatrix} t_L & \chi \\ b_L & t' \end{pmatrix}$ [Agashe, Contino, DaRold, Pomarol '06]
- $Zb_L\bar{b}_L$ protected by custodial $SU(2)_{L+R} \otimes P_{LR}$ invariance
 $Wt_L b_L, Zt_L t_L$ not protected, so shifts



Fermion representation : $Zb\bar{b}$ protected

- $Q_L = (2, 2)_{2/3} = \begin{pmatrix} t_L & \chi \\ b_L & t' \end{pmatrix}$ [Agashe, Contino, DaRold, Pomarol '06]
 - $Zb_L\bar{b}_L$ protected by custodial $SU(2)_{L+R} \otimes P_{LR}$ invariance
 $Wt_L b_L, Zt_L t_L$ not protected, so shifts

Two t_R possibilities:

① Singlet t_R (ST) : $(1, 1)_{2/3} = t_R$ New $\psi_{VL} : \chi, t'$

② Triplet t_R (TT) :

$$(1, 3)_{2/3} \oplus (3, 1)_{2/3} = \psi'_{t_R} \oplus \psi''_{t_R} = \begin{pmatrix} \frac{t_R}{\sqrt{2}} & \chi' \\ b' & -\frac{t_R}{\sqrt{2}} \end{pmatrix} \oplus \begin{pmatrix} \frac{t''}{\sqrt{2}} & \chi'' \\ b'' & -\frac{t''}{\sqrt{2}} \end{pmatrix}$$

New $\psi_{VL} : \chi, t', \chi', b', \chi'', t'', b''$



Flavor structure

[Agashe, Perez, Soni, 04]

$$\mathcal{L} \supset \bar{\Psi}^i i \Gamma^\mu D_\mu \Psi^i + M_{ij} \bar{\Psi}^i \Psi^j + y_{ij}^{5D} H \bar{\Psi}^i \Psi^j + h.c.$$

- Basis choice: M_{ij} diagonal $\equiv M_i$
 - All flavor violation from y_{ij}^{5D}
 - KK decompose and go to mass basis
 - $\implies g \bar{\Psi}_{(n)}^i W_\mu^{(k)} \Psi_{(m)}^j$ off-diagonal in flavor
(due to non-degenerate f^i i.e. M^i)
- 5D fermion Ψ is vector-like
 - M_{ij} is independent of $\langle H \rangle = v$
 - But zero-mode made chiral (SM)



FCNC couplings

- $h_{(0)}^{\mu\nu} \psi_{(0)} \psi_{(0)}$: diagonal
- $\{A_{(0)}, g_{(0)}\} \psi_{(0)} \psi_{(0)}$: diagonal (unbroken gauge symmetry)
- $\{Z_{(0)}, Z_{X(0)}\} \psi_{(0)} \psi_{(0)}$: almost diagonal (non-diagonal due to EWSB effect)
- $h \psi_{(0)} \psi_{(0)}$: diagonal (only source of mass is $\langle h \rangle = v$)

- $h_{(1)}^{\mu\nu} \psi_{(0)} \psi_{(0)}$: off-diagonal
- $\{A_{(1)}, g_{(1)}\} \psi_{(0)} \psi_{(0)}$: off-diagonal (i=1,2 almost diagonal)
- $\{Z_{(1)}, Z_{X(1)}\} \psi_{(0)} \psi_{(0)}$: off-diagonal

- $h_{(0)}^{\mu\nu} \psi_{(0)} \psi_{(1)}$: 0
- $\{A_{(0)}, g_{(0)}\} \psi_{(0)} \psi_{(1)}$: 0 (unbroken gauge symmetry)
- $\{Z_{(0)}, Z_{X(0)}\} \psi_{(0)} \psi_{(1)}$: off-diagonal (EWSB effect)
- $h \psi_{(0)} \psi_{(1)}$: off-diagonal (since M_ψ is extra source of mass)

$\psi_{(0)} \leftrightarrow \psi_{(1)}$ mixing due to EWSB



FCCC couplings

- $W_{L(0)}^{\pm} \psi_{(0)}^i \psi_{(0)}^j : g V_{CKM}^{ij}$
- $\{W_{L(1)}^{\pm}, W_{R(1)}^{\pm}\} \psi_{(0)} \psi_{(0)} : g V_{100} [f_{W(1)} f_{\psi} f_{\psi}]$
 - [...] suppressed for $i = 1, 2$; (Not suppr for b_L, t_L, t_R)
- $W_{L(0)}^{\pm} \psi_{(0)} \psi_{(1)} : g V_{001} [f_{W(1)} f_{\psi} f_{\psi(1)}]$



Challenge II : Flavor Constraints in WED

- $K^0 \bar{K}^0$ mixing:

- Tree-level FCNC vertex $g_{(1)} d s \propto V_L^{d\dagger} \begin{pmatrix} [g_{(1)} d d] & 0 \\ 0 & [g_{(1)} s s] \end{pmatrix} V_L^d$

- $b \rightarrow s \gamma$:

- No tree-level contribution to helicity flip dipole operator
 - So 1-loop with $g_{(1)} b s_{(1)}$ OR $\phi^\pm b s_{(1)}$

- $b \rightarrow s \ell^+ \ell^-$, $b \rightarrow s s \bar{s}$, $K \rightarrow \pi \nu \bar{\nu}$:

- Tree level FCNC vertex $Z s d$

Bound : $m_{KK} \gtrsim \text{few TeV}$

[Agashe et al][Buras et al][Neubert et al][Csaki et al]

Relaxed with flavor alignment : MFV, NMFV, flavor symmetries, ...

[Fitzpatrick et al][Agashe et al]

[SG, A.Iyer, S.Vempati Ongoing]



LHC Phenomenology



LED KK Graviton @ LHC

[Giudice, Rattazzi, Wells 1998][Hewett 1998] [Han, Lykken, Zhang 1998]

Look for KK Gravitons ($h_{\mu\nu}^{(n)}$) : Missing energy (MET)

- Small KK spacing : sum over huge number of states
 - Cutoff dependence
- Final state Gravitons : $pp \rightarrow \gamma h^{(n)}, j h^{(n)}$
- Virtual Gravitons : $pp \rightarrow h^{(n)} \rightarrow \ell^+ \ell^-, \dots$



LED LHC Limit $pp \rightarrow h_{\mu\nu}^{(n)} \rightarrow \ell^+ \ell^-$

TABLE VIII. Observed 95% C.L. lower limits on M_S (in units of TeV), including systematic uncertainties, for ADD signal in the GRW, Hewett and HLZ formalisms with K factors of 1.6 and 1.7 applied to the signal for the dilepton and diphoton channels, respectively. Separate results are provided for the different choices of flat priors: $1/M_S^4$ and $1/M_S^8$.

Channel	Prior	GRW	Hewett	HLZ				
				$n=3$	$n=4$	$n=5$	$n=6$	$n=7$
ee	$1/M_S^4$	2.95	2.63	3.51	2.95	2.66	2.48	2.34
	$1/M_S^8$	2.82	2.67	3.08	2.82	2.68	2.59	2.52
$\mu\mu$	$1/M_S^4$	3.07	2.74	3.65	3.07	2.77	2.58	2.44
	$1/M_S^8$	2.82	2.67	3.08	2.82	2.68	2.59	2.52
$ee + \mu\mu$	$1/M_S^4$	3.27	2.92	3.88	3.27	2.95	2.75	2.60
	$1/M_S^8$	3.09	2.92	3.37	3.09	2.94	2.84	2.76
$ee + \mu\mu + \gamma\gamma$	$1/M_S^4$	3.51	3.14	4.18	3.51	3.17	2.95	2.79
	$1/M_S^8$	3.39	3.20	3.69	3.39	3.22	3.11	3.02

ATLAS : 1211.1150 : 7TeV, 5 fb^{-1}

WED KK Graviton

[Agashe et al, 07] [Fitzpatrick et al, 07]

$$m_n = x_n k e^{-k\pi r} \quad x_n = 3.83, 7.02, \dots$$

$$\mathcal{L} \supset -\frac{C^{ffG}}{\Lambda} T^{\alpha\beta} h_{\alpha\beta}^{(n)} \quad \Lambda = \bar{M}_P e^{-k\pi r}$$

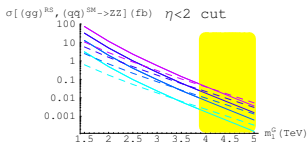
- SM on IR brane

- CDF & D0 bounds : $m_1 > 300 - 900$ GeV for $\frac{k}{M_p} = 0.01-0.1$
- ATLAS & CMS reach : 3.5 TeV with $100 fb^{-1}$

$$gg \rightarrow h^{(1)} \rightarrow ZZ \rightarrow 4\ell$$

- SM in Bulk (flavor)

- light fermion couplings highly suppressed
- gauge field couplings $\frac{1}{k\pi r}$ suppressed
- Decays dominantly to t, h, V_{Long}

various $\frac{k}{M_p}$; SM dashed

[Agashe, Davoudiasl, Perez, Soni, 2007]



KK Gluon

[Agashe et al, 06] [Lillie et al, 07]

$$m_n = x_n k e^{-k\pi r} \quad x_n \approx 2.45, 5.57, \dots \quad \text{Width } \Gamma \approx \frac{M}{6}$$

 $g^{(1)} t\bar{t}$: parity violating couplings!

$$\text{LHC: } q\bar{q} \rightarrow g^{(1)} \rightarrow t\bar{t}$$



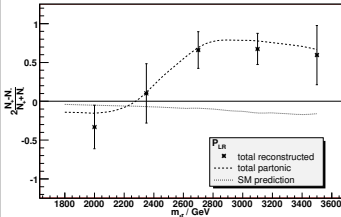
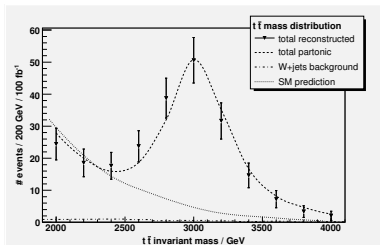
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$$P_{LR} = 2 \frac{N_+ - N_-}{N_+ + N_-} \quad N_+ \text{ forward going } \ell \text{ wrt } k_t$$

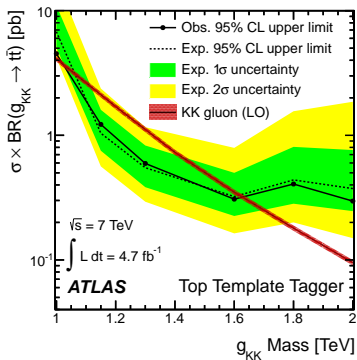
LHC reach: About 4 TeV with 100 fb⁻¹

W'^{\pm} Channels summary

[Agashe, SG, Han, Huang, Soni, 08: arXiv:0810.1497]
(\mathcal{L}_2 TeV; \mathcal{L}_3 TeV) in fb^{-1}

- $W'^{\pm} \rightarrow t b$:
 - Leptonic $\mathcal{L} : (100; 1000) fb^{-1}$
 - $t \bar{t}$ becomes (reducible) bkgnd since collimated t can fake a b-jet
Jet-mass cut : cone size 1.0 and $0 < j_M < 75 \Rightarrow 0.4\%$ of $tops$ fake b
- $W'^{\pm} \rightarrow Z W$:
 - Fully leptonic $\mathcal{L} : (100; 1000) fb^{-1}$
 - Semi leptonic $\mathcal{L} : (300; -) fb^{-1}$
- $W'^{\pm} \rightarrow W h$: $\mathcal{L} : (100; 300) fb^{-1}$
 - $m_h \approx 120 : h \rightarrow b b$
 - What is b-tagging eff at large p_{T_b} ?
 - $m_h \approx 150 : h \rightarrow W W$
 - Use W jet-mass to reject light jet

LHC KK-gluon search



ATLAS JHEP01(2013) 116 : Limit (7 TeV, 4.7 fb^{-1}): $M_{KK} > 1.6 \text{ TeV} @ 95\% \text{ CL}$

WED KK Fermions @ LHC

- SM fermions : $(+, +)$ BC \rightarrow zero-mode
- “Exotic” fermions : $(-, +)$ BC \rightarrow No zero-mode
 - 1^{st} KK vectorlike fermion

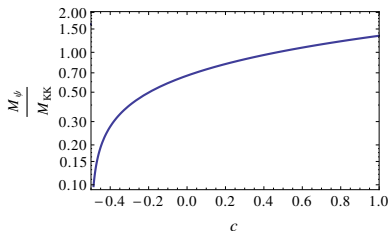
- Typical c_{tR}, c_{tL} : $(-, +)$ top-partners “light”

c : Fermion bulk mass parameter

[Choi, Kim, 2002] [Agashe, Delgado, May, Sundrum, 03]

[Agashe, Perez, Soni, 04] [Agashe, Servant 04]

- Look for it at the LHC



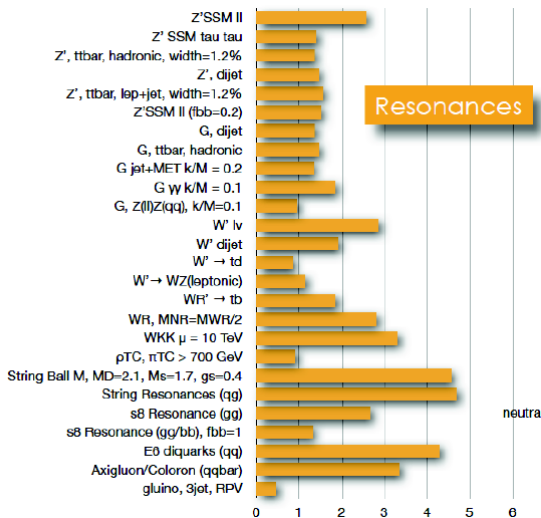
[Dennis et al, '07] [Carena et al, '07] [Contino, Servant, '08]

[Atre et al, '09, '11] [Aguilar-Saavedra, '09] [Mrazek, Wulzer, '09]

[SG, Moreau, Singh, '10] [SG, Mandal, Mitra, Tibrewala, '11] [SG, Mandal, Mitra, Moreau : '13]



CMS Resonances Limits (Moriond 2013)



ATLAS Extra Dimensions Limits (Moriond 2013)

ATLAS Exotics Searches* - 95% CL Lower Limits (Status: HCP 2012)

Large ED (ADD) : microjet + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}$, 7 TeV [1210.4491]	4.37 TeV	$M_D (\delta=2)$
Large ED (ADD) : monophoton + $E_{T,miss}$	$L=4.6 \text{ fb}^{-1}$, 7 TeV [1209.4525]	1.93 TeV	$M_D (\delta=2)$
Large ED (ADD) : diphoton & dilepton, $m_{\gamma\gamma}$	$L=4.7 \text{ fb}^{-1}$, 7 TeV [1211.1190]	4.10 TeV	M_S (HLZ $\delta=3$, NLO)
UED : diphoton + $E_{T,miss}$	$L=4.8 \text{ fb}^{-1}$, 7 TeV [ATLAS-CONF-2012-072]	1.41 TeV	Compact scale R^{-1}
S^1/Z_2 ED : dilepton, m_{ll}	$L=4.9-5.3 \text{ fb}^{-1}$, 7 TeV [1209.2535]	4.71 TeV	$M_{KK} \sim R^{-1}$
RS1 : diphoton & dilepton, $m_{\gamma\gamma}$	$L=4.7-5.3 \text{ fb}^{-1}$, 7 TeV [1210.5359]	2.23 TeV	Graviton mass ($k/M_{Pl} = 0.1$)
RS1 : ZZ resonance, m_{ll}	$L=1.0 \text{ fb}^{-1}$, 7 TeV [1203.0718]	145 GeV	Graviton mass ($k/M_{Pl} = 0.1$)
RS1 : WW resonance, $m_{\gamma\gamma}$	$L=4.7 \text{ fb}^{-1}$, 7 TeV [1208.2383]	1.23 TeV	Graviton mass ($k/M_{Pl} = 0.1$)
$S g_{KK} \rightarrow tt$ (BR=0.925) : $tt \rightarrow l+jets$, m_{jj}	$L=4.7 \text{ fb}^{-1}$, 7 TeV [ATLAS-CONF-2012-136]	1.9 TeV	g_{KK} mass
ADD BH ($M_{BH}/M_D=3$) : SS dimuon, $N_{col,part}$	$L=1.3 \text{ fb}^{-1}$, 7 TeV [1111.0686]	1.25 TeV	$M_D (\delta=6)$
ADD BH ($M_{BH}/M_D=3$) : leptons + jets, $2p_T$	$L=1.0 \text{ fb}^{-1}$, 7 TeV [1204.4545]	1.5 TeV	$M_D (\delta=6)$
Quantum black hole : dijet, $F(m_{jj})$	$L=4.7 \text{ fb}^{-1}$, 7 TeV [1210.1715]	4.11 TeV	$M_D (\delta=6)$

ATLAS
Preliminary

$$\int L dt = (1.0 - 13.0) \text{ fb}^{-1}$$

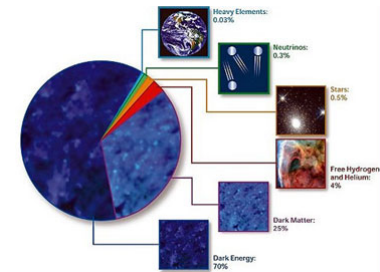
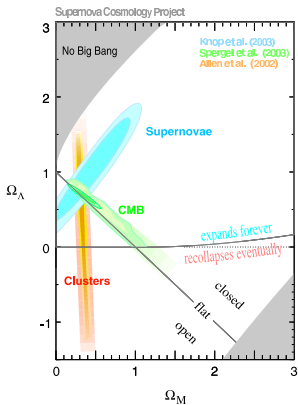
$$\sqrt{s} = 7, 8 \text{ TeV}$$



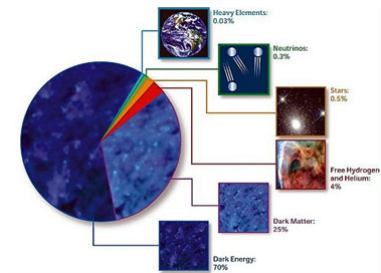
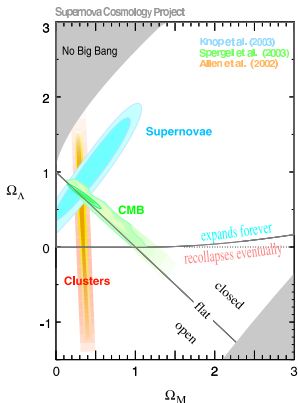
Dark Matter Candidates from BSM



Observations tell us

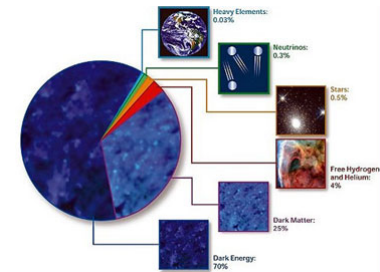
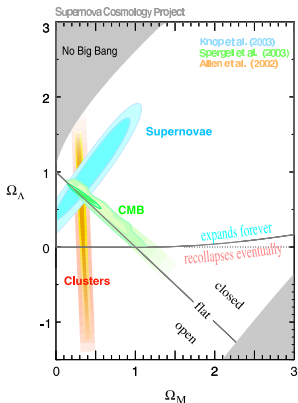


Observations tell us



- **Flat** on large scales
- Expansion is **Accelerating**
- **95%** is unknown **dark matter + dark energy**
 - **What is it??**

Observations tell us



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The DARK SIDE rules!



What is the dark sector?

- Dark Matter
 - Astrophysical objects? (Disfavoured)
 - MAssive Compact Halo Objects (MACHO) or Black Holes or ...
 - Particle dark matter? More on this...
 - Hot or Warm or **Cold Dark Matter (CDM)**



What is the dark sector?

- Dark Matter
 - Astrophysical objects? (Disfavoured)
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 - Particle dark matter? More on this...
 - Hot or Warm or **Cold Dark Matter (CDM)**
- Dark energy



Particle DM Requirements

- Should be around for a long long long time ...
 - Absolutely stable : Conserved quantum number
 - e, p are stable, but not “dark”! So not possible
 - Active ν_L , disfavored. Sterile ν_R , possible
 - BSM particle with Z_2 symmetry
 - Decays, but with very very very long life-time
 - Very very very tiny coupling to other SM states



Particle Dark Matter

- Thermal Relic
 - In thermal equilibrium in early universe
 - Details of its origin do NOT matter
 - So most studied
- Nonthermal Relic
 - Never in thermal equilibrium
 - Details of its origin do matter



Particle DM Possibilities

- LSP - Lightest Supersymmetric Particle
 - $\tilde{\chi}_1^0$ Neutralino (SUSY partner of neutral gauge boson)
 - $\tilde{\nu}$ Sneutrino (SUSY partner of neutrino)
- SuperWIMP - Gravitino (SUSY partner of graviton)
- E-WIMP - Right-handed sneutrino (partner of neutrino)
- WIMPzilla - Extremely massive particle
- LKP - Lightest Kaluza-Klein Particle - Extra space dimensions
- LTP - Lightest T-odd Particle - Little-higgs theory with Z_2
- Hidden sector DM



Particle DM Possibilities

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- Your candidate here



Thermal Relic

Thermal history of the Universe

Big Bang → Inflation → DM freeze-out → BBN → γ decouples → Today

Hubble rate:

$$H \equiv \frac{\dot{a}}{a} ; \quad H^2 = \frac{8\pi G}{3} \rho$$

$$H = 1.66 \sqrt{g_*} \frac{T^2}{M_{Pl}} \quad (\text{Rad Dom})$$



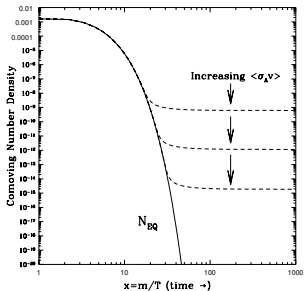
Boltzmann Equation

$$\frac{d}{dt} n = -3Hn - \langle \sigma v \rangle_{SI} (n^2 - n_{eq}^2) - \langle \sigma v \rangle_{CI} (nn_\phi - n_{eq} n_{\phi eq}) + C_\Gamma$$

Thermal equilibrium if

$$\langle \sigma v \rangle_{SI} n_{\tilde{\nu}_0} > 3H ; \quad \langle \sigma v \rangle_{CI} n_\phi > 3H$$

Freeze-out



[Kolb & Turner, Early Universe]



Weakly Interacting Massive Particle (WIMP)

WIMP Cold dark matter - New BSM particle

- Mass: $M \sim 100 \text{ GeV}$
- Interaction strength: $g \sim g_{EW}$

$$\Omega_0 \equiv \frac{n_0 M}{\rho_c} \approx 4 \times 10^{-10} \left(\frac{\text{GeV}^{-2}}{\langle \sigma v \rangle} \right)$$

Example: SUSY WIMP: If conserved R_p , Lightest Supersymmetric Particle (LSP) stable

- LSP (Eg: Neutralino) can be WIMP DM



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Example: SUSY WIMP: If conserved R_p , Lightest Supersymmetric Particle (LSP) stable

- LSP (Eg: Neutralino) can be WIMP DM
- Precisely the scale being explored at colliders!
 - DM at present colliders? (LHC connection)



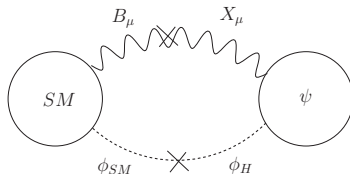
Hidden sector DM

Extend the SM to: $SM \times U(1)_X$

- $U(1)_X$ sector : GaugeBoson(X_μ), Scalar(Φ_H), Fermion(ψ)
 - If stable, can be DM

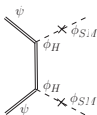
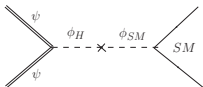
$SM \leftrightarrow U(1)_X$ communication

$$\mathcal{L} \supset -\alpha |\Phi_{SM}|^2 |\Phi_H|^2 + \frac{\eta}{2} X_{\mu\nu} B^{\mu\nu}$$



Hidden Sector Relic Density

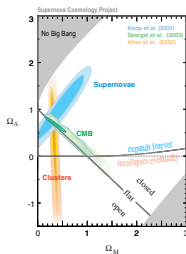
Self-annihilation



$$\Omega_0 h^2 = 10^{-29} x_f \left(\frac{eV^{-2}}{\langle \sigma v \rangle} \right)$$

$$\sigma v_{rel} = a + b v_{rel}^2 + O(v_{rel}^4)$$

$$\langle \sigma v \rangle = a + b/x_f \quad x_f \equiv M_\psi / T_f \approx 25$$



Observations : $\Omega_0 = 0.222 \pm 0.02$ [PDG '08]

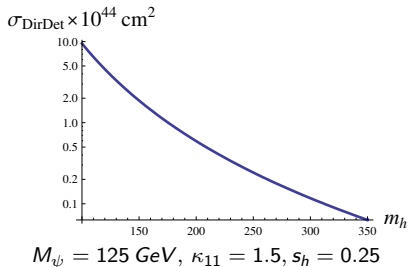
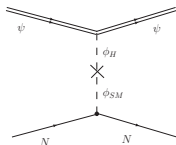
Channels $\psi\psi \rightarrow b\bar{b}, W^+W^-, ZZ, hh, t\bar{t}$

Dark Matter Detection

- Direct Detection
 - DM directly interacts with a detector
- Indirect Detection
 - Look for indirect emissions from DM
- Collider Detection
 - DM escapes as missing momentum at colliders



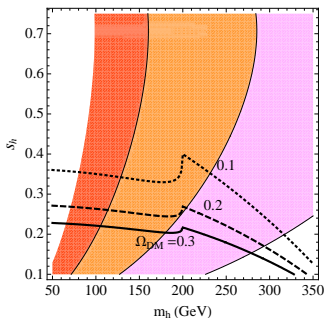
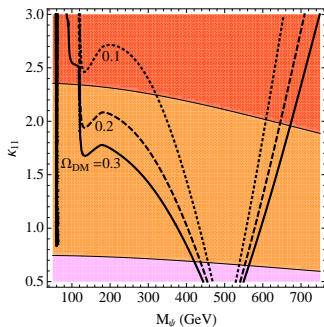
Direct Detection of Hidden sector



Effective $h\bar{N}N$ coupling $\approx 2 \times 10^{-3}$ [Shifman, Vainshtein, Zakharov (1973)]

ψ - Nucleon c.s. :

$$\sigma(\psi N \rightarrow \psi N) \approx \frac{\kappa_{11}^2 s_h^2 c_h^2 \lambda_N^2}{8\pi v_{\text{rel}}} \frac{(|\mathbf{p}_\psi|^2 + m_N^2)}{(t - m_h^2)^2}$$

ψ Relic Density + Direct Detection

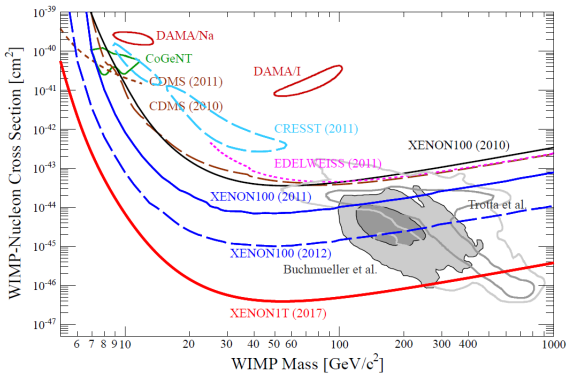
[SG, S.Lee, J.Wells 2009]

 $M_\psi = 250\text{GeV}, m_h = 120\text{GeV}, \kappa_{11} = 2.0, s_h = 0.25, \kappa_{3\phi} = 1, m_H = 1\text{TeV}$

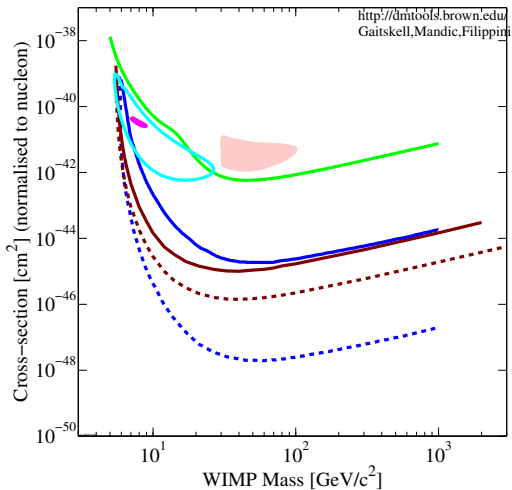
Shaded:

 $\sigma_{Dir} \gtrsim 10^{-43} \text{ cm}^2$ (dark); $\gtrsim 10^{-44} \text{ cm}^2$ (medium); $\gtrsim 10^{-45} \text{ cm}^2$ (light)


Direct Detection Experimental Limits (Old)



Direct Detection Experimental Limits



DATA listed top to bottom on plot

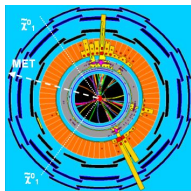
- CoGeNT, 2013, WIMP region of interest, SI
- DAMA, 2000, NaI-0 to 4 combined, 58,000kg-days, 3sig
- CDMSII-Si (Silicon), c58 95% CL, SI (2013)
- CRESST II commissioning run (2009) extended to low mass
- XENON100, 2012, 225 live days (7650 kg-days), SI
- LUX (2013) 85d 118kg (SI, 95% CL)
- - - LUX (2014/15) 300d projection (SI, 90% CL median expect)
- - - Xenon10T, G3 expected sensitivity (2013)

● DAMA vs. XENON/LUX puzzle

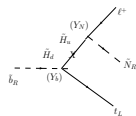
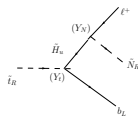
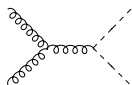
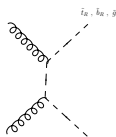
- What's going on?



DM at Colliders II



- Example: Supersymmetry

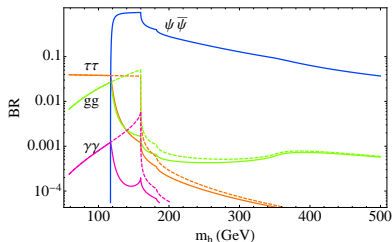
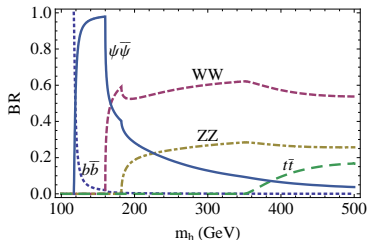


- LSP leads to “missing momentum”

Higgs decay to DM

- Higgs decay and BR

- If $m_h > 2M_\psi$: $h \rightarrow \psi\bar{\psi}$ Invisible Decay!
 - Decay channels: $h \rightarrow \psi\bar{\psi}, b\bar{b}, WW, ZZ, t\bar{t}$



$$M_\psi \approx 59 \text{ GeV}, s_h = 0.25, \kappa_{11} = 2.0, \kappa_{3\phi} = 1.0, m_H = 1 \text{ TeV}$$

NB: Relic density not enforced

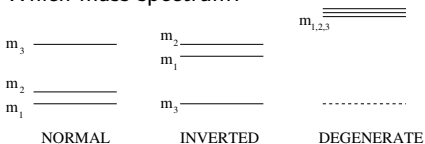


Neutrino Mass Generation

Questions

- What is the scale of m_ν
- Is the ν a DIRAC or MAJORANA particle? (Is $L_\#$ good?)

- Which mass spectrum?

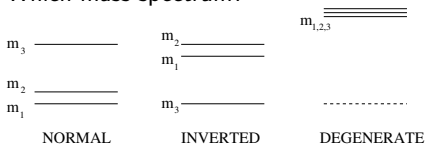


- Is there CP violation in the lepton sector?

Neutrino Mass Generation

Questions

- What is the scale of m_ν
- Is the ν a DIRAC or MAJORANA particle? (Is $L_\#$ good?)
- Which mass spectrum?



- Is there CP violation in the lepton sector?

Possible Answers

- Dirac ν : Add ν_R with TINY (10^{-12}) Yukawa coupling
- Type I seesaw: Add ν_R and a BIG (10^{11} GeV) mass
- Type II seesaw: Add SU(2) triplet scalar ξ with TINY (0.1 eV) VEV
- Type III seesaw: Add SU(2) triplet fermion Ξ
- Extra dimensions: Add BULK ν_R with BRANE coupling to ν_L



Conclusions

- Standard Model has shortcomings
 - Theoretical: Gauge (& flavor) hierarchy problem
 - Observational: DM, BAU
- Beyond the Standard Model physics can resolve these
 - Supersymmetry, Extra dimension(s), Strong dynamics, Little Higgs, ...
- Are any of these ideas realized in Nature?
 - *Desperately seeking experimental guidance*
 - Experiments poised for discovery?
 - LHC7,8 constraints already nontrivial.
LHC14 high luminosity run crucial
 - DM Direct, Indirect detection
 - Flavor and precision probes



BACKUP SLIDES

BACKUP SLIDES



Yukawa Couplings

Yukawa Couplings

- No $Zb\bar{b}$ protection

- DT $\mathcal{L}_{\text{Yuk}} \supset \lambda_t \bar{Q}_L \Sigma \psi_{t_R} + \lambda_b \bar{Q}_L \Sigma \psi_{b_R} + h.c.$

- With $Zb\bar{b}$ protection

- ST $\mathcal{L}_{\text{Yuk}} \supset \lambda_t \text{Tr}[\bar{Q}_L \Sigma] t_R + h.c.$

- TT $\mathcal{L}_{\text{Yuk}} \supset \lambda_t \text{Tr}[\bar{Q}_L \Sigma \psi'_{t_R}] + \lambda'_t \text{Tr}[\bar{Q}_L \Sigma \psi''_{t_R}] + h.c.$

- b Yukawa requires triplet b_R

$$(1, 3)_{2/3} \oplus (3, 1)_{2/3} = \psi'_{b_R} \oplus \psi''_{b_R} = \begin{pmatrix} \frac{t'_b}{\sqrt{2}} & \chi'_b \\ b_R & -\frac{t'_b}{\sqrt{2}} \end{pmatrix} \oplus \begin{pmatrix} \frac{t''_b}{\sqrt{2}} & \chi''_b \\ b''_b & -\frac{t''_b}{\sqrt{2}} \end{pmatrix}$$

$$\mathcal{L}_{\text{Yuk}} \supset \lambda_b \text{Tr}[\bar{Q}_L \Sigma \psi'_{b_R}] + \lambda'_b \text{Tr}[\bar{Q}_L \Sigma \psi''_{b_R}] + h.c.$$

c_{b_R} such that new $\psi'_b, \psi''_b \gtrsim 3 \text{ TeV}$, so ignore them



WED $pp \rightarrow g^{(1)} \rightarrow t\bar{t}$ (semi-leptonic)

!!!Warning!!! Very rough estimates!

- $\sigma(M_{g^{(1)}} = 2\text{TeV}, \sqrt{S} = 14\text{TeV}, k\pi R = 35) \approx 600\text{fb}$
 - $\mathcal{L}^{5\sigma}(M_{g^{(1)}} = 2\text{TeV}, \sqrt{S} = 14\text{TeV}, k\pi R = 35) = 1.2\text{fb}^{-1}$
- $14\text{TeV} \rightarrow 7\text{TeV}$: $\sigma(g^{(1)} = 2\text{TeV})$ falls by a factor of 25
 - $\mathcal{L}^{5\sigma}(M_{g^{(1)}} = 2\text{TeV}, \sqrt{S} = 7\text{TeV}, k\pi R = 35) = 30\text{fb}^{-1}$
(Assumed : Bkgnd falls with same factor)
- $\mathcal{L}^{5\sigma}(M_{g^{(1)}} = 2\text{TeV}, \sqrt{S} = 7\text{TeV}, k\pi R = 7) = 1\text{fb}^{-1}$



Bulk EW Gauge Sector

Bulk EW Gauge group : $SU(2)_L \times SU(2)_R \times U(1)_X$

- Three neutral gauge bosons: (W_L^3, W_R^3, X)
- Two charged gauge bosons: (W_L^\pm, W_R^\pm)

Symmetry Breaking:

- By Boundary Condition (BC):

$$Z_X(-, +) \text{ means } Z_X|_{y=0} = 0; \partial_y Z_X|_{y=\pi R} = 0$$

- $SU(2)_R \times U(1)_X \rightarrow U(1)_Y$: $(W_R^3, W_L^3, X) \rightarrow (W_L^3, B, Z_X)$
 $A \rightarrow (+, +); Z \rightarrow (+, +); Z_X \rightarrow (-, +)$
- $Z_X \equiv \frac{1}{\sqrt{g_X^2 + g_R^2}} (g_R W_R^3 - g_X X) \rightarrow (-, +)$; $W_R^\pm \rightarrow (-, +)$
- $B \equiv \frac{1}{\sqrt{g_X^2 + g_R^2}} (g_X W_R^3 + g_R X) \rightarrow (+, +)$; $W_L^\pm \rightarrow (+, +)$



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- $B \equiv \frac{1}{\sqrt{g_X^2 + g_R^2}}(g_X W_R^3 + g_R X) \rightarrow (+, +)$; $W_L^\pm \rightarrow (+, +)$

- By VEV of TeV brane Higgs

- $SU(2)_L \times U(1)_Y \rightarrow U(1)_{EM}$: $(W_L^3, B, Z_X) \rightarrow (A, Z, Z_X)$



Gauge EW KK States

Gauge Boson

- “Zero” modes: $A^{(0)}, Z^{(0)}$; $W_L^{(0)}$
- First KK modes: $A^{(1)}, Z^{(1)}, Z_X^{(1)} \rightarrow Z'$; $W_L^{(1)}, W_R^{(1)}$

EWSB mixes : $Z^{(0)} \leftrightarrow Z^{(1)}$; $Z^{(0)} \leftrightarrow Z_X^{(1)}$; $Z^{(1)} \leftrightarrow Z_X^{(1)}$
 $W_L^{(0)} \leftrightarrow W_L^{(1)}$; $W_L^{(0)} \leftrightarrow W_R^{(1)}$; $W_L^{(1)} \leftrightarrow W_R^{(1)}$

Mass eigenstates :

- “Zero” modes: A, Z ; W^\pm
- First KK modes: $A_1, \tilde{Z}_1, \tilde{Z}_{X_1} \rightarrow Z'$; $\tilde{W}_{L_1}, \tilde{W}_{R_1} \rightarrow W'^\pm$



Z' Overlap Integrals

Define: $\xi \equiv \sqrt{k\pi R} = 5.83$

Z' overlap with Higgs $\rightarrow \xi$

Z' overlap with fermions:

	Q_L^3	t_R	other fermions
\mathcal{I}^+	$-\frac{1.13}{\xi} + 0.2\xi \approx 1$	$-\frac{1.13}{\xi} + 0.7\xi \approx 3.9$	$-\frac{1.13}{\xi} \approx -0.2$
\mathcal{I}^-	$0.2\xi \approx 1.2$	$0.7\xi \approx 4.1$	0

Compared to SM

- Z' couplings to h enhanced (also V_L - Equivalence Theorem!)
- Z' couplings to t_R enhanced
- Z' couplings to χ suppressed

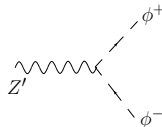
$$\bar{\psi}_{L,R} \gamma^\mu \left[eQI A_{1\mu} + g_Z (T_L^3 - s_W^2 T_Q) IZ_{1\mu} + g_{Z'} (T_R^3 - s'^2 T_Y) IZ_{X1\mu} \right] \psi_{L,R}$$



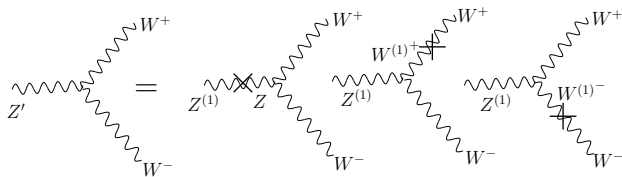
EWSB induced $Z'W^+W^-$ coupling

$Z^{(1)}V^{(0)}V^{(0)}$ is zero by orthogonality ...
 ... but induced after EWSB

Using Goldstone equivalence:



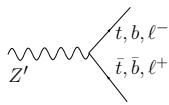
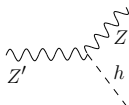
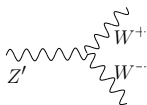
In Unitary Gauge:



Even though $\xi \cdot \left(\frac{v}{M_{KK}}\right)^2$ suppressed ...

Z' decays

[Agashe, Davoudiasl, SG, Han, Huang, Perez, Si, Soni - arXiv:0709.0007 [hep-ph]]



$$\Gamma(A_1 \rightarrow W_L W_L) = \frac{e^2 \kappa^2 M_{Z'}^5}{192\pi m_W^4}; \quad \kappa \propto \sqrt{k\pi r_c} \left(\frac{m_W}{M_{W_1^\pm}} \right)^2,$$

$$\Gamma(\tilde{Z}_1, \tilde{Z}_{X1} \rightarrow W_L W_L) = \frac{g_L^2 c_W^2 \kappa^2 M_{Z'}^5}{192\pi m_W^4}; \quad \kappa \propto \sqrt{k\pi r_c} \left(\frac{m_Z}{(M_{Z_1}, M_{Z_{X1}})} \right)^2,$$

$$\Gamma(\tilde{Z}_1, \tilde{Z}_{X1} \rightarrow Z_L h) = \frac{g_Z^2 \kappa^2}{192\pi} M_{Z'}; \quad \kappa \propto \sqrt{k\pi r_c},$$

$$\Gamma(Z' \rightarrow f\bar{f}) = \frac{(e^2, g_Z^2)}{12\pi} (\kappa_V^2 + \kappa_A^2) M_{Z'}.$$

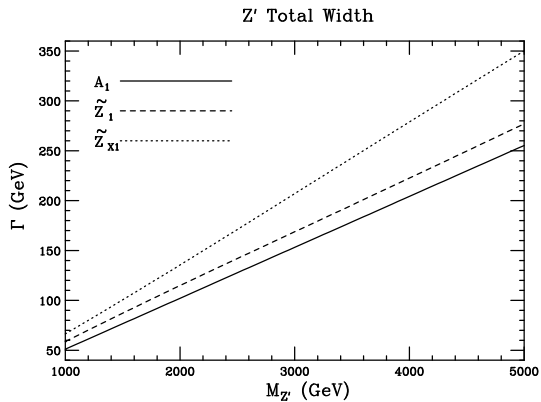


Widths & BR's (For $M_{Z'} = 2\text{TeV}$)

	A_1		\tilde{Z}_1		\tilde{Z}_{X1}	
	$\Gamma(\text{GeV})$	BR	$\Gamma(\text{GeV})$	BR	$\Gamma(\text{GeV})$	BR
$\bar{t}t$	55.8	0.54	18.3	0.16	55.6	0.41
$\bar{b}b$	0.9	8.7×10^{-3}	0.12	10^{-3}	28.5	0.21
$\bar{u}u$	0.28	2.7×10^{-3}	0.2	1.7×10^{-3}	0.05	4×10^{-4}
$\bar{d}d$	0.07	6.7×10^{-4}	0.25	2.2×10^{-3}	0.07	5.2×10^{-4}
$\ell^+\ell^-$	0.21	2×10^{-3}	0.06	5×10^{-4}	0.02	1.2×10^{-4}
$W_L^+ W_L^-$	45.5	0.44	0.88	7.7×10^{-3}	50.2	0.37
$Z_L h$	-	-	94	0.82	2.7	0.02
Total	103.3		114.6		135.6	



Total Widths

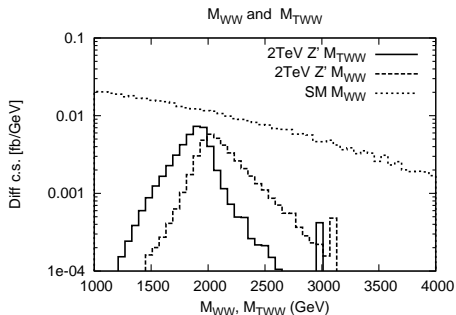


$M_{Z'} = 2\text{TeV}$	A_1	Z_1	Z_{X1}
Γ (GeV)	103.3	114.6	135.6

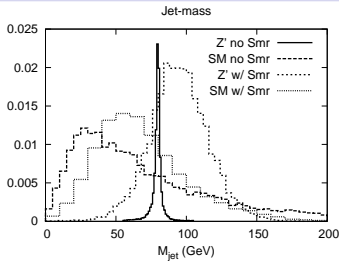
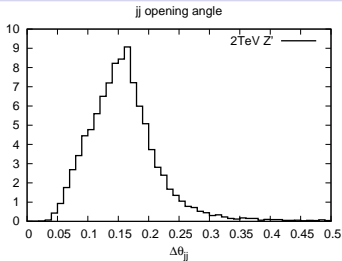


$pp \rightarrow Z' \rightarrow W^+W^- \rightarrow \ell \nu jj$

$$M_{eff} \equiv p_{T_{jj}} + p_{T_\ell} + \cancel{p}_T \quad M_{T_{WW}} \equiv 2\sqrt{p_{T_{jj}}^2 + m_W^2}$$



$pp \rightarrow Z' \rightarrow W^+W^- \rightarrow \ell \nu jj$ (Boosted $W \rightarrow (jj)$)



jj Collimation implies forming m_W nontrivial : use jet-mass

In our study: Jet-mass after Parton shower in Pythia

[Thanks to Frank Paige for discussions]

To account for (HCal) expt. uncert.

Smearing by $\delta E = 80\%/\sqrt{E}$; $\delta\eta, \delta\phi = 0.05$

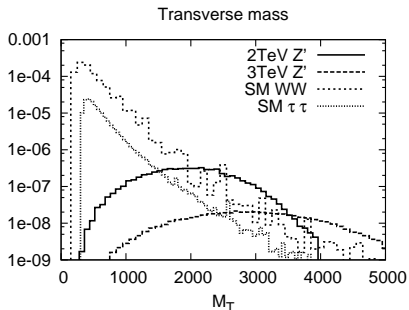
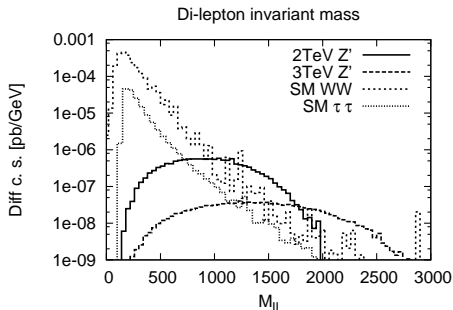
Tracker + ECal (2 cores?) have better resolutions

[F. Paige; M. Strassler]



$pp \rightarrow Z' \rightarrow W^+W^- \rightarrow \ell\nu\ell\nu$

2 ν 's \Rightarrow cannot reconstruct event



$$M_{eff} \equiv p_{T_{\ell_1}} + p_{T_{\ell_2}} + \cancel{p}_T \quad M_{T_{WW}} \equiv 2\sqrt{p_{T_{\ell\ell}}^2 + M_{\ell\ell}^2}$$

\mathcal{L} needed: 100 fb^{-1} (2 TeV) ; 1000 fb^{-1} (3 TeV)



$$pp \rightarrow Z' \rightarrow W^+W^- \rightarrow \ell\nu\ell\nu$$

Cross-section (in fb) after cuts:

2 TeV	Basic cuts	$ \eta_\ell < 2$	$M_{eff} > 1 \text{ TeV}$	$M_T > 1.75 \text{ TeV}$	# Evts	S/B	S/\sqrt{B}
Signal	0.48	0.44	0.31	0.26	26	0.9	4.9
WW	82	52	0.4	0.26	26		
$\tau\tau$	7.7	5.6	0.045	0.026	2.6		
3 TeV	Basic cuts	$ \eta_\ell < 2$	$1.5 < M_{eff} < 2.75$	$2.5 < M_T < 5$	# Evts	S/B	S/\sqrt{B}
Signal	0.05	0.05	0.03	0.025	25		
WW	82	52	0.08	0.04	40	0.6	3.8
$\tau\tau$	7.7	5.6	0.015	0.003	3		

events above is for

- 2 TeV : 100 fb^{-1}
- 3 TeV : 1000 fb^{-1}



$$pp \rightarrow Z' \rightarrow W^+W^- \rightarrow \ell \nu jj$$

Cross-section (in fb) after cuts:

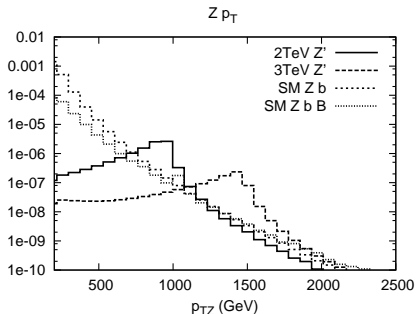
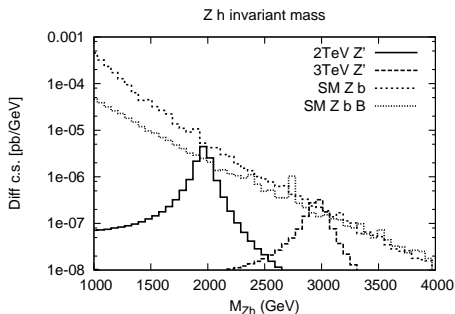
$M_{Z'} = 2 \text{ TeV}$	p_T	$\eta_{\ell,j}$	M_{eff}	$M_{T_{WW}}$	M_{jet}	# Evts	S/B	S/\sqrt{B}
Signal	4.5	2.40	2.37	1.6	1.25	125	0.39	6.9
W+1j	1.5×10^5	3.1×10^4	223.6	10.5	3.15	315		
WW	1.2×10^3	226	2.9	0.13	0.1	10		
$M_{Z'} = 3 \text{ TeV}$								
Signal	0.37	0.24	0.24	0.12	-	120	0.17	4.6
W+1j	1.5×10^5	3.1×10^4	88.5	0.68	-	680		
WW	1.2×10^3	226	1.3	0.01	-	10		

events above is for

- 2 TeV : 100 fb^{-1}
- 3 TeV : 1000 fb^{-1}



$pp \rightarrow Z' \rightarrow Zh \rightarrow \ell^+ \ell^- b \bar{b}$ ($m_h = 120$ GeV)



How well can we tag high p_T b's ?

For $\epsilon_b = 0.4$, expect $R_j \approx 20 - 50$; $R_c = 5$

Two b's close : $\Delta R_{bb} \sim 0.16$

\mathcal{L} needed: 200 fb^{-1} (2 TeV) ; 1000 fb^{-1} (3 TeV)



$pp \rightarrow Z' \rightarrow Zh \rightarrow \ell^+ \ell^- b \bar{b}$ ($m_h = 120$ GeV)

Cross-section (in fb) after cuts:

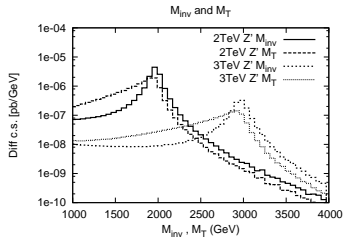
$M_{Z'} = 2$ TeV	Basic	$p_{T, \eta}$	$\cos \theta_{Zh}$	M_{inv}	b-tag	# Evts	S/B	S/ \sqrt{B}
$Z' \rightarrow hZ \rightarrow b\bar{b} \ell\ell$	0.81	0.73	0.43	0.34	0.14	27	1.1	5.3
SM $Z + b$	157	1.6	0.9	0.04	0.016	3		
SM $Z + b\bar{b}$	13.5	0.15	0.05	0.01	0.004	0.8		
SM $Z + q_l$	2720	48	22.4	1.5	0.08	15		
SM $Z + g$	505.4	11.2	5.8	0.5	0.025	5		
SM $Z + c$	184	1.9	1.1	0.05	0.01	2		
$M_{Z'} = 3$ TeV								
$Z' \rightarrow hZ \rightarrow b\bar{b} \ell\ell$	0.81	0.12	0.05	0.04	0.016	16	2	5.7
SM $Z + b$	157	0.002	0.001	3×10^{-4}	1.2×10^{-4}	0.12		
SM $Z + b\bar{b}$	13.5	0.018	0.014	0.002	0.001	1		
SM $Z + q_l$	2720	1.1	0.7	0.1	0.005	5		
SM $Z + g$	505.4	0.3	0.2	0.03	0.0015	1.5		
SM $Z + c$	183.5	0.03	0.02	0.002	4×10^{-4}	0.4		

events above is for

- 2 TeV : 200 fb⁻¹
- 3 TeV : 1000 fb⁻¹



$pp \rightarrow Z' \rightarrow Z h : Z \rightarrow jj ; h \rightarrow W^+W^- \rightarrow jj \ell \nu$
 ($m_h = 150$ GeV)



$$M_{T_{Zh}} \equiv \sqrt{p_{T_Z}^2 + m_Z^2} + \sqrt{p_{T_h}^2 + m_h^2}$$

$M_{Z'} = 2$ TeV $m_h = 150$ GeV	Basic	p_T, η	$\cos \theta$	M_T	M_{jet}	# Evts	S/B	S/\sqrt{B}
$Z' \rightarrow hZ \rightarrow \ell \cancel{E}_T (jj) (jj)$	2.4	1.6	0.88	0.7	0.54	54	2.5	11.5
SM Wjj	3×10^4	35.5	12.7	0.62	0.19	19		
SM WZj	184	0.45	0.15	0.02	0.02	2		
SM WWj	712	0.54	0.2	0.02	0.01	1		
$M_{Z'} = 3$ TeV $m_h = 150$ GeV								
$Z' \rightarrow hZ \rightarrow \ell \cancel{E}_T (jj) (jj)$	0.26	0.2	0.14	0.06	—	18	1.2	4.7
SM Wjj	3×10^4	4.1	0.05	—	—	15		

events above is for

- 2 TeV : 100 fb⁻¹
- 3 TeV : 300 fb⁻¹



$$pp \rightarrow Z' \rightarrow \ell^+ \ell^-$$

$M_{Z'} = 2 \text{ TeV}$	Basic	$p_{T\ell}$	$M_{\ell\ell}$	# Evts	S/B	S/\sqrt{B}
Signal	0.1	0.09	0.06	60	0.3	4.2
SM $\ell\ell$	3×10^4	5.4	0.2	200		
SM WW	295	0.03	0.002	2		

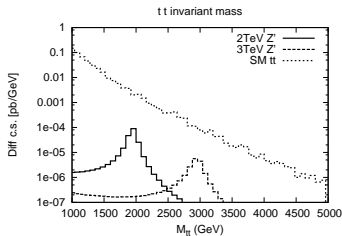
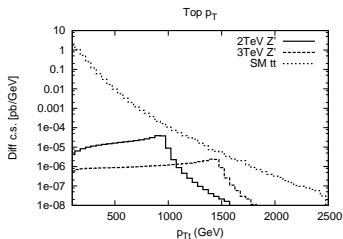
events above is for

- 2 TeV : 1000 fb⁻¹

Experimentally clean, but needs a LOT of luminosity



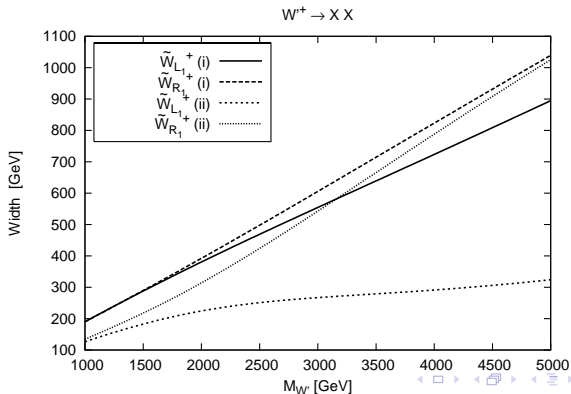
$pp \rightarrow Z' \rightarrow t\bar{t}$



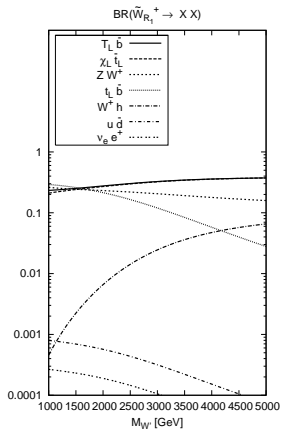
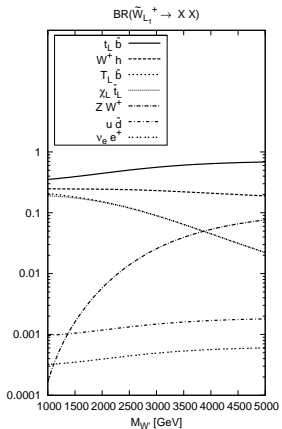
$M_{Z'} = 2 \text{ TeV}$	Basic	$p_T > 800$	$1900 < M_{t\bar{t}} < 2100$
Signal	17	7.2	5.6
SM $t\bar{t}$	1.9×10^5	31.1	19.1
$M_{Z'} = 3 \text{ TeV}$	Basic	$p_T > 1250$	$2850 < M_{t\bar{t}} < 3100$
Signal	1.7	0.56	0.45
SM $t\bar{t}$	1.9×10^5	4.1	1.1



W'^{\pm} width



$W'^{\pm} BR$

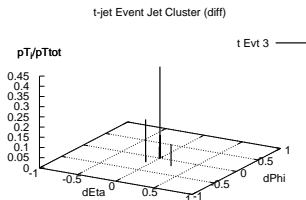
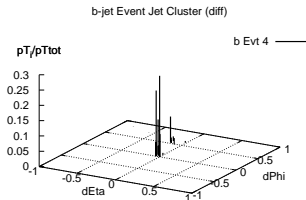
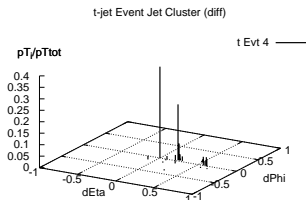
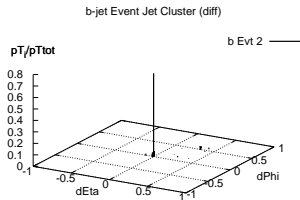


$W'^{\pm} \rightarrow t b \rightarrow l \nu b b$

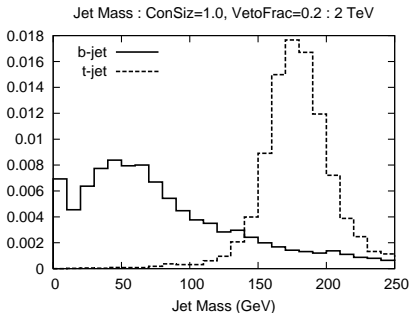
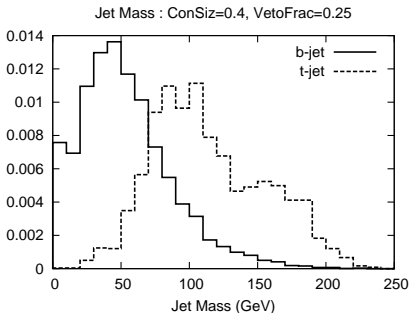
Signal c.s. $\sim 1fb$

Bkgnd is single top + QCD W b b AND ...

$t\bar{t}$: hadronically decaying top can fake a b



$W'^{\pm} \rightarrow t b \rightarrow \ell \nu b b$



Jet-mass cut: cone size 1.0 and $0 < j_M < 75 \Rightarrow 0.4\%$ of *top fakes* b
 \mathcal{L} needed: 100 fb^{-1} (2 TeV)



$W'^{\pm} \rightarrow Z W$ and $W h$

$W'^{\pm} \rightarrow Z W$:

- Fully leptonic $\rightarrow \mathcal{L} : 100 \text{ fb}^{-1}$ (2 TeV) ; 1000 fb^{-1} (3 TeV)
- Semi leptonic $\rightarrow \mathcal{L} : 300 \text{ fb}^{-1}$ (2 TeV) (SM $W/Z + 1j$ large)



$W'^{\pm} \rightarrow Z W$ and $W h$

$W'^{\pm} \rightarrow Z W$:

- Fully leptonic $\rightarrow \mathcal{L} : 100 \text{ fb}^{-1}$ (2 TeV) ; 1000 fb^{-1} (3 TeV)
- Semi leptonic $\rightarrow \mathcal{L} : 300 \text{ fb}^{-1}$ (2 TeV) (SM $W/Z + 1j$ large)

$W'^{\pm} \rightarrow W h$:

- $m_h \approx 120 : h \rightarrow b b$
 - What is b-tagging eff?
- $m_h \approx 150 : h \rightarrow W W$
 - Use W jet-mass to reject light jet

\mathcal{L} needed: 100 fb^{-1} (2TeV) ; 300 fb^{-1} (3TeV)



Warped States

- Warped (RS) model
- Heavy EW gauge bosons : 3 neutral (Z') & 2 charged (W'^{\pm})
 - Precision electroweak observables require $M_{Z'}$, $M_{W_1^{\pm}} \gtrsim 2$ TeV
 - Makes discovery challenging at the LHC

