

Inflation and the early universe

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Prospects for frontier CMB space experiments from India

ISRO, Bengaluru

January 8–9, 2018

Plan of the talk

- 1 The inflationary paradigm
- 2 The power spectra generated during inflation
- 3 Constraints on the primordial power spectra from Planck
- 4 Constraints on non-Gaussianities
- 5 Search for the B-modes
- 6 'Anomalies'
- 7 Expertise in India
- 8 Summary

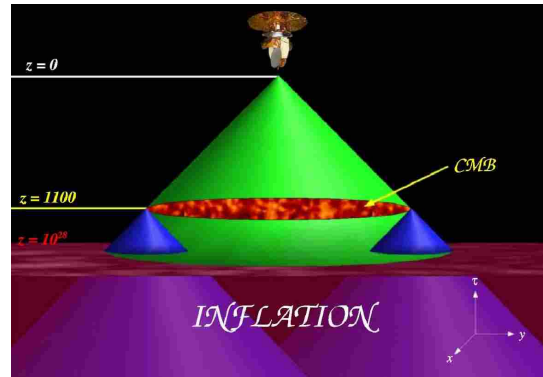
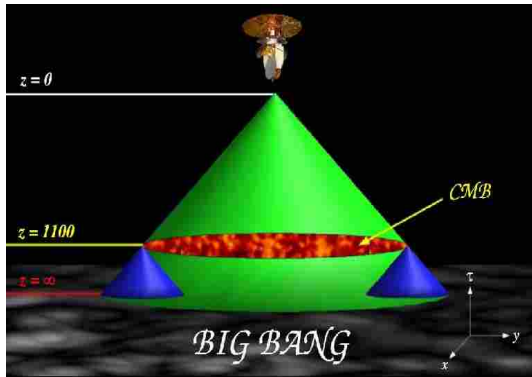


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The resolution of the horizon problem in inflation

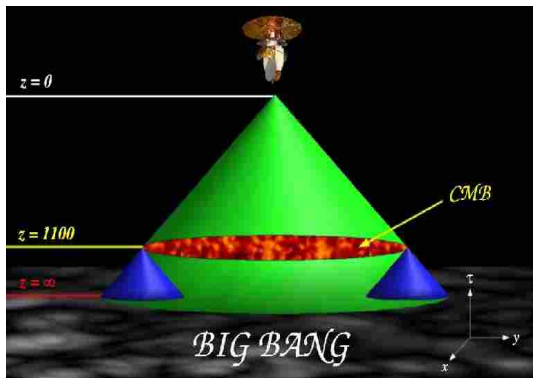


Left: The radiation from the CMB arriving at us from regions separated by more than the Hubble radius at the last scattering surface (which subtends an angle of about 1° today) could not have interacted before decoupling.

¹Images from [W. Kinney, astro-ph/0301448](#).

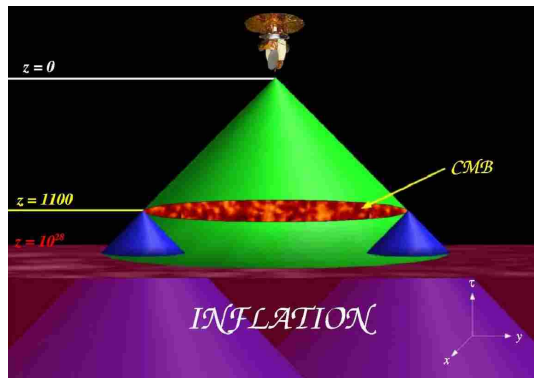


The resolution of the horizon problem in inflation



Left: The radiation from the CMB arriving at us from regions separated by more than the Hubble radius at the last scattering surface (which subtends an angle of about 1° today) could not have interacted before decoupling.

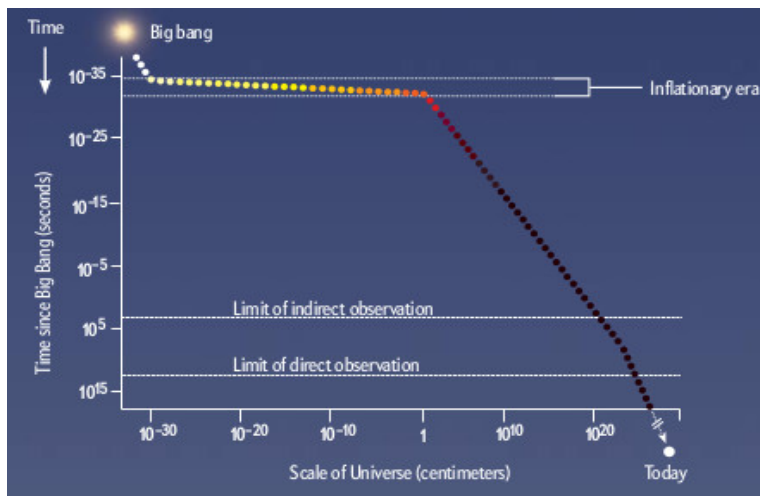
Right: An illustration of how an early and sufficiently long epoch of inflation helps in resolving the horizon problem¹.



¹Images from [W. Kinney, astro-ph/0301448](#).



The time and duration of inflation

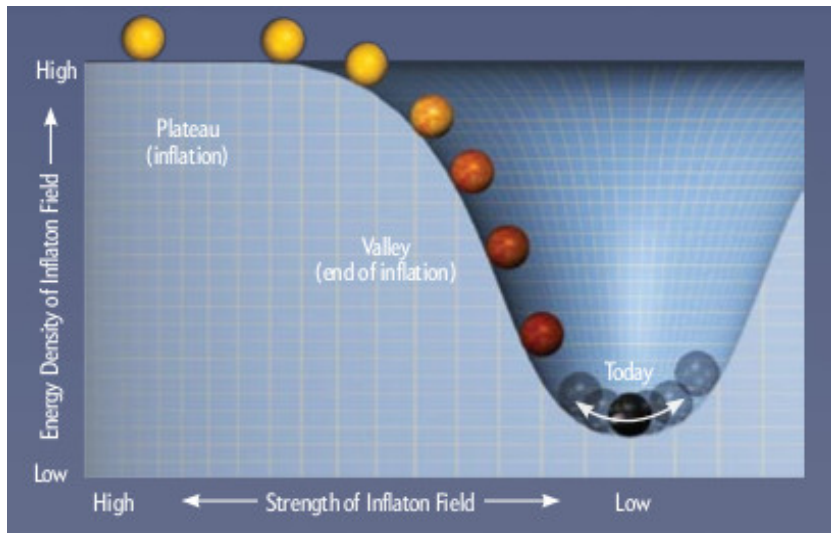


Inflation – a brief period of accelerated expansion – is expected to have taken place during the very early stages of the universe².

²Image from P. J. Steinhardt, *Sci. Am.* **304**, 18 (2011).



Driving inflation with scalar fields

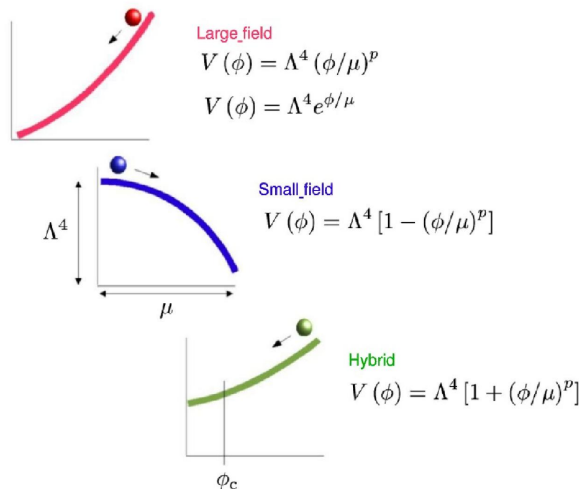


Inflation can be achieved easily with scalar fields encountered in high energy physics³.

³Image from P. J. Steinhardt, *Sci. Am.* **304**, 34 (2011).



A variety of potentials to choose from



A variety of scalar field potentials have been considered to drive inflation⁴. Often, these potentials are classified as small field, large field and hybrid models.

⁴Image from [W. Kinney, astro-ph/0301448](https://arxiv.org/abs/astro-ph/0301448).



Constraining inflationary models

5-dimensional assisted inflation	extended open inflation	late-time mild inflation	pre-Big-Bang inflation
anisotropic brane inflation	extended warm inflation	low-scale inflation	primary inflation
anomaly-induced inflation	extra dimensional inflation	low-scale supergravity inflation	primordial inflation
assisted inflation	F-term inflation	M-theory inflation	quasi-open inflation
assisted chaotic inflation	F-term hybrid inflation	mass inflation	quintessential inflation
boundary inflation	false vacuum inflation	massive chaotic inflation	R-invariant topological inflation
brane inflation	false vacuum chaotic inflation	moduli inflation	rapid asymmetric inflation
brane-assisted inflation	fast-roll inflation	multi-scalar inflation	running inflation
brane gas inflation	first order inflation	multiple inflation	scalar-tensor gravity inflation
brane-antibrane inflation	gauged inflation	multiple-field slow-roll inflation	scalar-tensor stochastic inflation
braneworld inflation	generalised inflation	multiple-stage inflation	Seiberg-Witten inflation
Brans-Dicke chaotic inflation	generalized assisted inflation	natural inflation	single-bubble open inflation
Brans-Dicke inflation	generalized slow-roll inflation	natural Chaotic inflation	spinodal inflation
bulky brane inflation	gravity driven inflation	natural double inflation	stable starobinsky-type inflation
chaotic hybrid inflation	Hagedorn inflation	natural supergravity inflation	steady-state eternal inflation
chaotic inflation	higher-curvature inflation	new inflation	steep inflation
chaotic new inflation	hybrid inflation	next-to-minimal supersymmetric hybrid inflation	stochastic inflation
D-brane inflation	hyperextended inflation	non-commutative inflation	string-forming open inflation
D-term inflation	induced gravity inflation	non-slow-roll inflation	successful D-term inflation
dilaton-driven inflation	induced gravity open inflation	nonminimal chaotic inflation	supergravity inflation
dilaton-driven brane inflation	intermediate inflation	old inflation	supernatural inflation
double inflation	inverted hybrid inflation	open hybrid inflation	superstring inflation
double D-term inflation	isocurvature inflation	open inflation	supersymmetric hybrid inflation
dual inflation	K inflation	oscillating inflation	supersymmetric inflation
dynamical inflation	kinetic inflation	polynomial chaotic inflation	supersymmetric topological inflation
dynamical SUSY inflation	lambda inflation	polynomial hybrid inflation	supersymmetric new inflation
eternal inflation	large field inflation	power-law inflation	synergistic warm inflation
extended inflation	late D-term inflation		TeV-scale hybrid inflation

A partial list of inflationary models⁵. The goal is to rule out as many of the models as possible. Until either the cosmic neutrino background or the stochastic gravitational wave background is observed, it is the anisotropies in the CMB that provides the primary window to probe physics operating at the highest energy scales.

⁵From E. P. S. Shellard, *The future of cosmology: Observational and computational prospects*, in *The Future of Theoretical Physics and Cosmology*, Eds. G. W. Gibbons, E. P. S. Shellard and S. J. Rankin (Cambridge University Press, Cambridge, England, 2003).

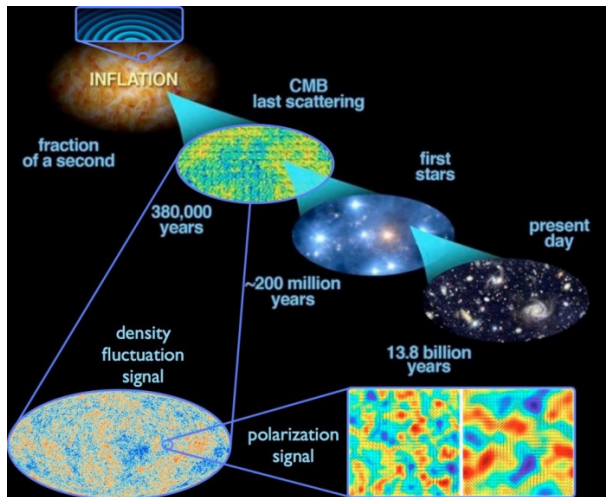


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Perturbations induced by quantum fluctuations



It is the quantum fluctuations associated with the scalar fields that generate the primordial perturbations which, in turn, induce the anisotropies in the CMB⁶.

⁶From <https://sciencesprings.wordpress.com/2016/04/29/from-ethan-siegel-the-biggest-question-about-the-beginning-of-the-universe/#jp-carousel-39872>.



The slow roll scalar amplitude, index and running⁷

At the leading order in the slow roll approximation, the spectral amplitude of the curvature perturbation can be expressed in terms of the potential $V(\phi)$ as follows:

$$\mathcal{P}_S(k) \simeq \frac{1}{12 \pi^2 M_{\text{Pl}}^6} \left(\frac{V^3}{V_\phi^2} \right)_{k=aH},$$

with the subscript on the right hand side indicating that the quantity has to be evaluated when the modes leave the Hubble radius.

At the same order of the approximation, the scalar spectral index is given by

$$n_S \equiv 1 + \left(\frac{d \ln \mathcal{P}_S}{d \ln k} \right)_{k=aH} = 1 - 2 \epsilon_1 - \epsilon_2,$$

while the running of the scalar spectral index can be evaluated to be

$$\alpha_S \equiv \left(\frac{d n_S}{d \ln k} \right)_{k=aH} = - (2 \epsilon_1 \epsilon_2 + \epsilon_2 \epsilon_3).$$

⁷See, for instance, B. A. Bassett, S. Tsujikawa and D. Wands, *Rev. Mod. Phys.* **78**, 537 (2006).



The tensor amplitude, spectral index and running

At the leading order in the slow roll approximation, the tensor amplitude is given by

$$\mathcal{P}_T(k) \simeq \frac{2}{3\pi^2} \left(\frac{V}{M_{\text{Pl}}^4} \right)_{k=aH},$$

while the spectral index and the running can be estimated to be⁸

$$n_T \equiv \left(\frac{d \ln \mathcal{P}_T}{d \ln k} \right)_{k=aH} = -2 \epsilon_1 \quad \text{and} \quad \alpha_T \equiv \left(\frac{d n_T}{d \ln k} \right)_{k=aH} = -2 \epsilon_1 \epsilon_2.$$

The tensor-to-scalar ratio is then given by

$$r \equiv \frac{\mathcal{P}_T(k)}{\mathcal{P}_S(k)} \simeq 16 \epsilon_1 = -8 n_T,$$

with the last equality often referred to as the consistency relation⁹.

⁸See, B. A. Bassett, S. Tsujikawa and D. Wands, *Rev. Mod. Phys.* **78**, 537 (2006).

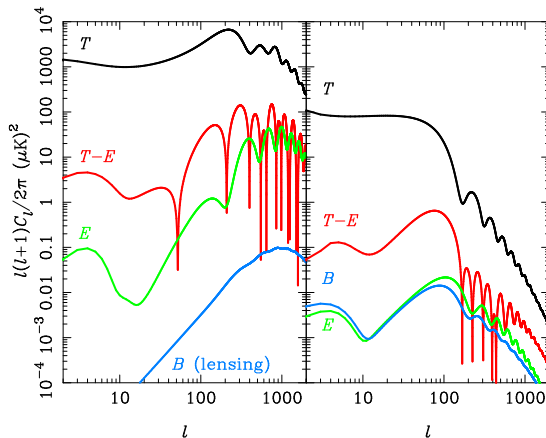
⁹J. E. Lidsey, A. R. Liddle, E. W. Kolb and E. J. Copeland, *Rev. Mod. Phys.* **69**, 373 (1997).



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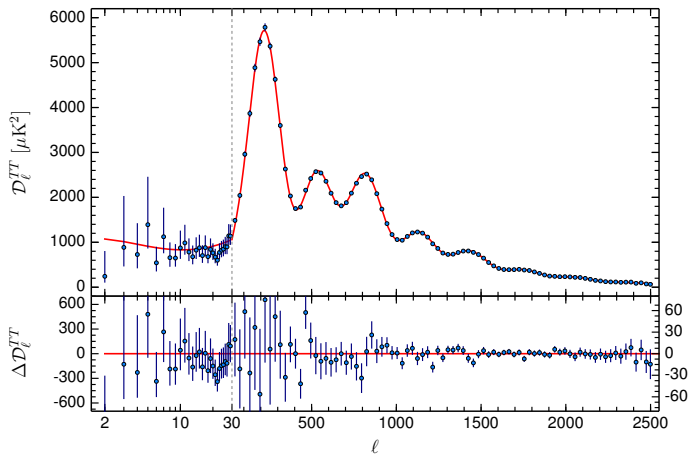
Theoretical angular power spectra¹⁰

The *theoretically* computed, CMB angular power and cross-correlation spectra – temperature (T , in black), E (in green), B (in blue), and $T-E$ (in red) – arising due to scalars (on the left) and tensors (on the right) corresponding to a tensor-to-scalar ratio of $r = 0.24$. The B -mode spectrum induced by weak gravitational lensing has also been shown (in blue) in the panel on the left.

¹⁰Figure from A. Challinor, arXiv:1210.6008 [astro-ph.CO].



CMB TT angular power spectrum from Planck

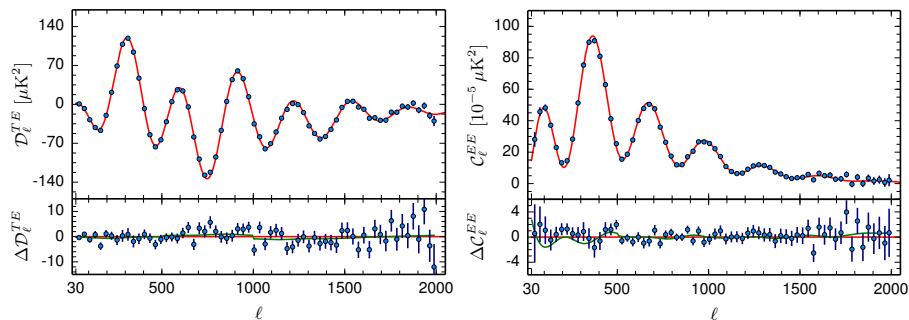


The CMB TT angular power spectrum from the Planck 2015 data (the blue dots with error bars) and the theoretical, best fit Λ CDM model with a power law primordial spectrum (the solid red curve)¹¹.

¹¹Planck Collaboration (P. A. R. Ade *et al.*), *Astron. Astrophys.* **594**, A20 (2016).



CMB TE and EE angular power spectra from Planck



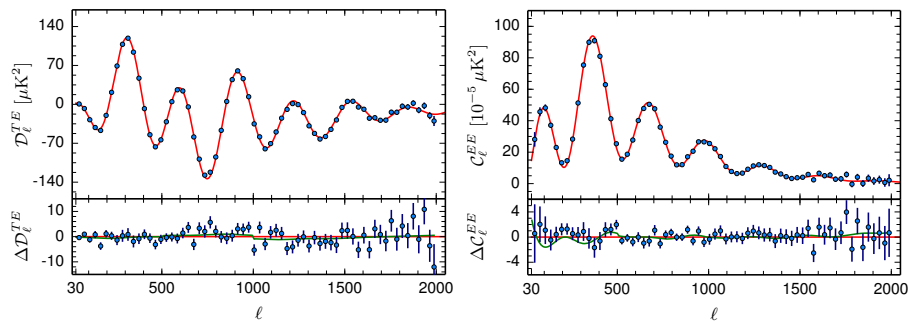
The CMB TE (on the left) and EE (on the right) angular power spectra from the Planck 2015 data (the blue dots with error bars) and the theoretical, best fit Λ CDM model with a power law primordial spectrum (the solid red curves)¹².

¹²Planck Collaboration (P. A. R. Ade *et al.*), *Astron. Astrophys.* **594**, A20 (2016).

¹³D. N. Spergel and M. Zaldarriaga, *Phys. Rev. Lett.* **79**, 2180 (1997).



CMB TE and EE angular power spectra from Planck



The CMB TE (on the left) and EE (on the right) angular power spectra from the Planck 2015 data (the blue dots with error bars) and the theoretical, best fit Λ CDM model with a power law primordial spectrum (the solid red curves)¹².

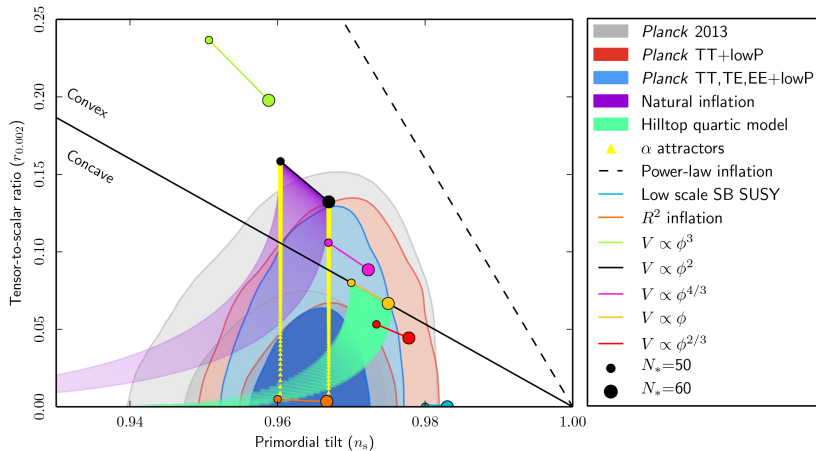
The large angle ($50 < \ell < 150$) TE anti-correlation detected by Planck (and earlier by WMAP) is a distinctive signature of primordial, super-Hubble, adiabatic perturbations¹³.

¹²Planck Collaboration (P. A. R. Ade *et al.*), *Astron. Astrophys.* **594**, A20 (2016).

¹³D. N. Spergel and M. Zaldarriaga, *Phys. Rev. Lett.* **79**, 2180 (1997).



Performance of models in the n_s - r plane



Marginalized joint **68%** and **95%** CL regions for n_s and $r_{0.002}$ from Planck in combination with other data sets, compared to the theoretical predictions of selected inflationary models¹⁴.

¹⁴Planck Collaboration (P. A. R. Ade *et al.*), *Astron. Astrophys.* **594**, A20 (2016).



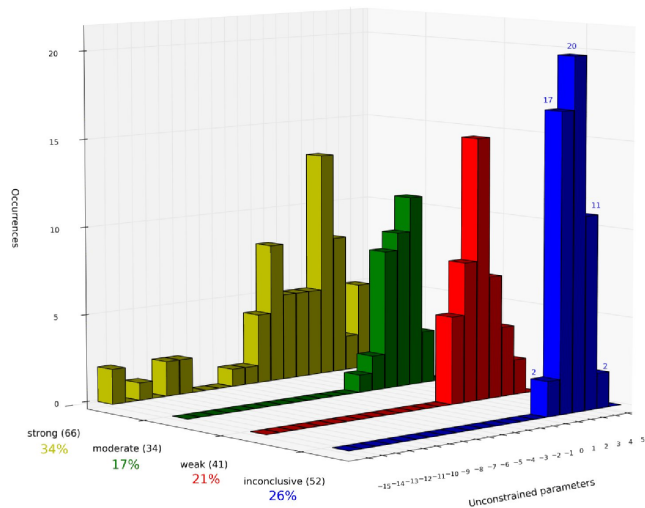
Likelihood for specific inflationary models

Inflationary model	$\Delta\chi^2$		$\ln B_{0X}$	
	$w_{\text{int}} = 0$	$w_{\text{int}} \neq 0$	$w_{\text{int}} = 0$	$w_{\text{int}} \neq 0$
$R + R^2/(6 M^2)$	+0.8	+0.3	...	+0.7
$n = 2/3$	+6.5	+3.5	-2.4	-2.3
$n = 1$	+6.2	+5.5	-2.1	-1.9
$n = 4/3$	+6.4	+5.5	-2.6	-2.4
$n = 2$	+8.6	+8.1	-4.7	-4.6
$n = 3$	+22.8	+21.7	-11.6	-11.4
$n = 4$	+43.3	+41.7	-23.3	-22.7
Natural	+7.2	+6.5	-2.4	-2.3
Hilltop ($p = 2$)	+4.4	+3.9	-2.6	-2.4
Hilltop ($p = 4$)	+3.7	+3.3	-2.8	-2.6
Double well	+5.5	+5.3	-3.1	-2.3
Brane inflation ($p = 2$)	+3.0	+2.3	-0.7	-0.9
Brane inflation ($p = 4$)	+2.8	+2.3	-0.4	-0.6
Exponential inflation	+0.8	+0.3	-0.7	-0.9
SB SUSY	+0.7	+0.4	-2.2	-1.7
Supersymmetric α -model	+0.7	+0.1	-1.8	-2.0
Superconformal ($m = 1$)	+0.9	+0.8	-2.3	-2.2
Superconformal ($m \neq 1$)	+0.7	+0.5	-2.4	-2.6

The improvement in the likelihood $\Delta\chi^2$ (with respect to the base Λ CDM model) and the Bayes factor (with respect to R^2 inflation) for a set of inflationary models.



Performance of inflationary models



The efficiency of the inflationary paradigm leads to a situation wherein, despite the strong constraints, a variety of models continue to remain consistent with the data¹⁵.

¹⁵J. Martin, C. Ringeval, R. Trotta and V. Vennin, JCAP **1403**, 039 (2014).



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Definitions of scalar bispectrum and non-Gaussianity parameter

The scalar bispectrum $\mathcal{B}_{\mathcal{R}\mathcal{R}\mathcal{R}}(\mathbf{k}_1, \mathbf{k}_2, \mathbf{k}_3)$ is related to the three point correlation function of the Fourier modes of the curvature perturbation as follows¹⁶:

$$\langle \hat{\mathcal{R}}_{\mathbf{k}_1}(\eta_e) \hat{\mathcal{R}}_{\mathbf{k}_2}(\eta_e) \hat{\mathcal{R}}_{\mathbf{k}_3}(\eta_e) \rangle = (2\pi)^3 \mathcal{B}_{\mathcal{R}\mathcal{R}\mathcal{R}}(\mathbf{k}_1, \mathbf{k}_2, \mathbf{k}_3) \delta^{(3)}(\mathbf{k}_1 + \mathbf{k}_2 + \mathbf{k}_3).$$

¹⁶D. Larson *et al.*, *Astrophys. J. Suppl.* **192**, 16 (2011);

E. Komatsu *et al.*, *Astrophys. J. Suppl.* **192**, 18 (2011).

¹⁷E. Komatsu and D. N. Spergel, *Phys. Rev. D* **63**, 063002 (2001).

¹⁸J. Martin and L. Sriramkumar, *JCAP* **1201**, 008 (2012).



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The observationally relevant non-Gaussianity parameter f_{NL} is basically introduced through the relation¹⁷

$$\mathcal{R}(\eta, \mathbf{x}) = \mathcal{R}_G(\eta, \mathbf{x}) - \frac{3f_{\text{NL}}}{5} [\mathcal{R}_G^2(\eta, \mathbf{x}) - \langle \mathcal{R}_G^2(\eta, \mathbf{x}) \rangle],$$

where \mathcal{R}_G denotes the Gaussian quantity. Utilizing the above relation and Wick's theorem, one can arrive at the following relation¹⁸:

$$f_{\text{NL}}(\mathbf{k}_1, \mathbf{k}_2, \mathbf{k}_3) = -\frac{10}{3} (2\pi)^{1/2} (k_1^3 k_2^3 k_3^3) \mathcal{B}_{\mathcal{R}\mathcal{R}\mathcal{R}}(\mathbf{k}_1, \mathbf{k}_2, \mathbf{k}_3) \\ \times [k_1^3 \mathcal{P}_S(k_2) \mathcal{P}_S(k_3) + \text{two permutations}]^{-1}.$$

¹⁶D. Larson *et al.*, *Astrophys. J. Suppl.* **192**, 16 (2011);

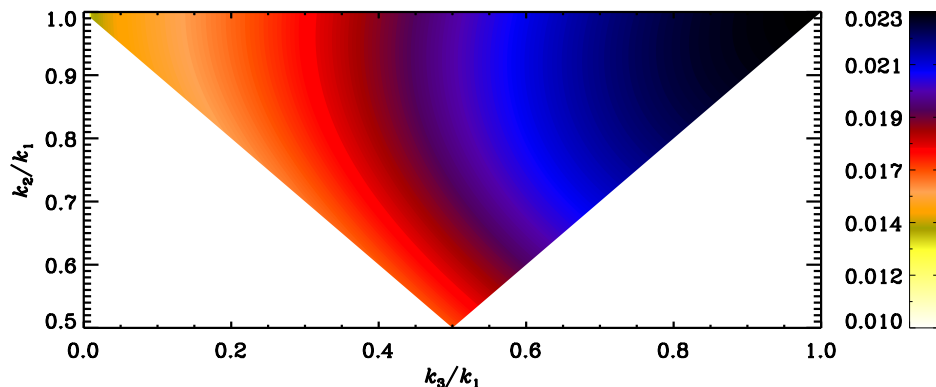
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¹⁷E. Komatsu and D. N. Spergel, *Phys. Rev. D* **63**, 063002 (2001).

¹⁸J. Martin and L. Sriramkumar, *JCAP* **1201**, 008 (2012).



The shape of the slow roll bispectrum



The non-Gaussianity parameter f_{NL} , evaluated in the slow roll approximation, has been plotted as a function of k_3/k_1 and k_2/k_1 for the case of the popular quadratic potential. Note that the non-Gaussianity parameter peaks in the equilateral limit wherein $k_1 = k_2 = k_3$. In slow roll scenarios involving the canonical scalar field, the largest value of f_{NL} is found to be of the order of the first slow roll parameter ϵ_1 ¹⁹.

¹⁹Figure from D. K. Hazra, L. Sriramkumar and J. Martin, JCAP **1305**, 026, (2013).



Template bispectra

For comparison with the observations, the scalar bispectrum is often expressed in terms of the parameters f_{NL}^{loc} , f_{NL}^{eq} and f_{NL}^{orth} as follows:

$$G_{RRR}(\mathbf{k}_1, \mathbf{k}_2, \mathbf{k}_3) = f_{NL}^{loc} G_{RRR}^{loc}(\mathbf{k}_1, \mathbf{k}_2, \mathbf{k}_3) + f_{NL}^{eq} G_{RRR}^{eq}(\mathbf{k}_1, \mathbf{k}_2, \mathbf{k}_3) + f_{NL}^{orth} G_{RRR}^{orth}(\mathbf{k}_1, \mathbf{k}_2, \mathbf{k}_3).$$

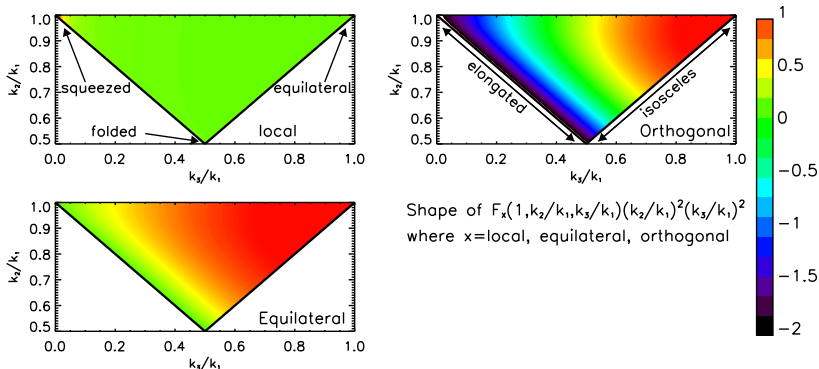


Illustration of the three template basis bispectra²⁰.

²⁰E. Komatsu, *Class. Quantum Grav.* **27**, 124010 (2010).



Constraints on the scalar non-Gaussianity parameters

The constraints on the primordial values of the non-Gaussianity parameters from the Planck data are as follows²¹:

$$\begin{aligned}f_{\text{NL}}^{\text{loc}} &= 0.8 \pm 5.0, \\f_{\text{NL}}^{\text{eq}} &= -4 \pm 43, \\f_{\text{NL}}^{\text{orth}} &= -26 \pm 21.\end{aligned}$$

²¹Planck Collaboration (P. A. R. Ade *et al.*), *Astron. Astrophys.* **594**, A17 (2016).



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It should be stressed that these are constraints on the primordial values.

Also, the constraints on each of the f_{NL} parameters have been arrived at assuming that the other two parameters are zero.

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It should be stressed that these are constraints on the primordial values.

Also, the constraints on each of the f_{NL} parameters have been arrived at assuming that the other two parameters are zero.

These constraints imply that slowly rolling single field models involving the canonical scalar field which are favored by the data at the level of power spectra are also consistent with the data at the level of non-Gaussianities.

²¹Planck Collaboration (P. A. R. Ade *et al.*), *Astron. Astrophys.* **594**, A17 (2016).

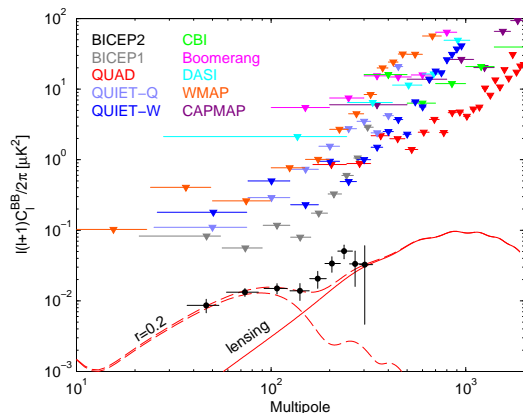


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The 'detection' of the B -mode polarization by BICEP2

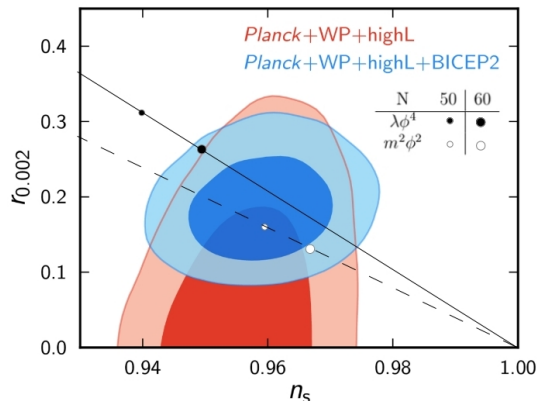


The supposed 'detection' of the angular power spectrum of the B -mode polarization of the CMB by BICEP2 as well as the limits that have been arrived at by the earlier efforts²². The BICEP2 observations, *viz.* the black dots with error bars, had seemed to be consistent with a tensor-to-scalar ratio of $r \simeq 0.2$.

²²P. A. R. Ade *et al.*, [arXiv:1403.3985 \[astro-ph.CO\]](https://arxiv.org/abs/1403.3985).



Constraints from the BICEP2 data²³



Joint constraints from the BICEP2 observations, the Planck data, the polarization data from WMAP as well as data for the high multipoles from SPT and ACT, on the inflationary parameters n_s and r .

²³P. A. R. Ade *et al.*, [arXiv:1403.3985 \[astro-ph.CO\]](https://arxiv.org/abs/1403.3985).



Amazing prescience!

VOLUME 78, NUMBER 10

PHYSICAL REVIEW LETTERS

10 MARCH 1997

What Would We Learn by Detecting a Gravitational Wave Signal in the Cosmic Microwave Background Anisotropy?

David H. Lyth

School of Physics and Chemistry, Lancaster University, Lancaster LA1 4YB, United Kingdom
(Received 20 June 1996)

Inflation generates gravitational waves, which may be observable in the low multipoles of the cosmic microwave background anisotropy but only if the inflaton field variation is at least of order the Planck scale. Such a large variation would imply that the model of inflation cannot be part of an ordinary extension of the standard model, and combined with the detection of the waves it would also suggest that the inflaton field cannot be one of the superstring moduli. Another implication of observable gravitational waves would be a potential $V^{1/4} = 2$ to 4×10^{16} GeV, which is orders of magnitude bigger than the prediction of most models. [S0031-9007(97)02506-4]

PACS numbers: 98.80.Cq, 04.30.Db, 98.70.Vc

A paper by David Lyth with a title that had seemed amazingly apt in the light of BICEP2 observations.



The scale of inflation

During slow roll, if we ignore the weak scale dependence, we can write

$$r \simeq \frac{2V}{3\pi^2 M_{\text{Pl}}^4} \frac{1}{\mathcal{A}_s},$$

where, recall that, \mathcal{A}_s denotes the amplitude of the scalar perturbations.

The amplitude of the primordial scalar perturbations is usually quoted at the pivot scales of either 0.05 or 0.02 Mpc^{-1} , which correspond to multipoles that lie in the Sachs-Wolfe plateau. This value for the scalar amplitude is often referred to as COBE normalization²⁴.

According to COBE normalization, $\mathcal{A}_s \simeq 2.14 \times 10^{-9}$, which implies that we can write

$$V^{1/4} \simeq 3.2 \times 10^{16} r^{1/4} \text{ GeV} \simeq 2.1 \times 10^{16} \text{ GeV},$$

with the final value being for the case wherein $r \simeq 0.2$.

Note that, if H_I represents the Hubble scale during the inflationary epoch, as $H_I^2 \simeq V/(3 M_{\text{Pl}}^2)$ during slow roll, the above relation also leads to

$$\frac{H_I}{M_{\text{Pl}}} \simeq 4.6 \times 10^{-5}.$$

²⁴E. F. Bunn, A. R. Liddle and M. J. White, Phys. Rev. D **54**, R5917 (1996).



The Lyth bound

The contributions of the primordial gravitational waves to the B -mode of the CMB polarization angular power spectrum drops sharply after multipoles of $\ell \simeq 100$, roughly around the same multipoles where the TT angular power spectrum exhibits its first peak.

The CMB quadrupole, *i.e.* $\ell = 2$, corresponds to the largest cosmological scale of interest, *viz.* the Hubble radius H_0^{-1} today. Hence, we can relate the wavenumbers to the multipoles as $k \simeq H_0 \ell/2$. Therefore, a $\Delta \ell$ corresponds to the width $\Delta k \simeq H_0 \Delta \ell/2$ in terms of wavenumbers.

As $a \propto e^N$, the modes over a domain Δk corresponding to $\Delta \ell \simeq 100$ will leave the Hubble radius during inflation over the time period $\Delta N \simeq \log 10 \simeq 3.9$. During slow roll, we have $H^2 = V/(3 M_{\text{Pl}}^2)$ and $3 H \dot{\phi} \simeq V_\phi$, so that²⁵

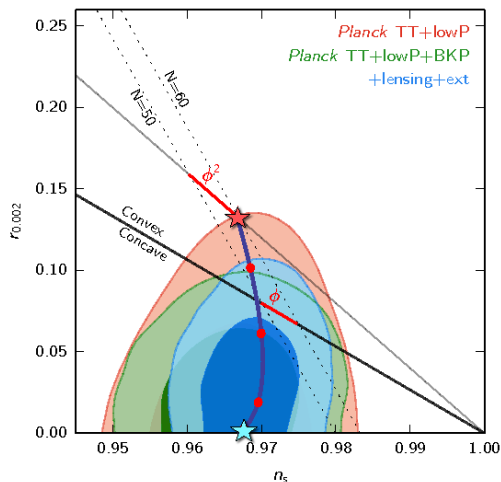
$$\Delta \phi \simeq (r/8)^{1/2} \Delta N M_{\text{Pl}} \simeq 0.6 M_{\text{Pl}},$$

with the final value corresponding to $r \simeq 0.2$.

²⁵D. H. Lyth, *Phys. Rev. Letts.* **78**, 1861 (1997).



Models with small tensor-to-scalar ratio

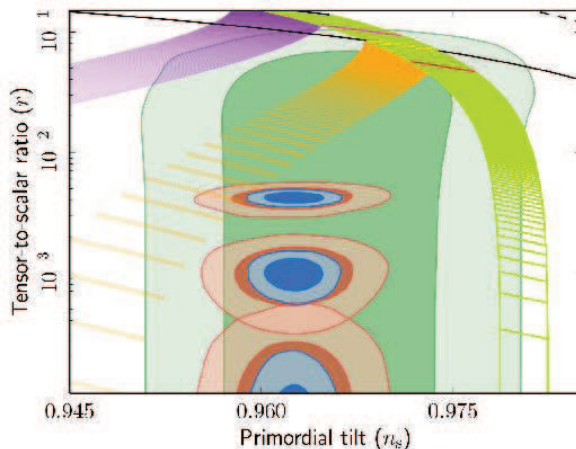


The theorists are ahead! The so-called alpha-attractor models which can lead to rather small values of the tensor-to-scalar ratio²⁶.

²⁶R. Kallosh and A. Linde, *Phys. Rev. D* **91**, 083528 (2015).



The n_s - r -plane with CORE

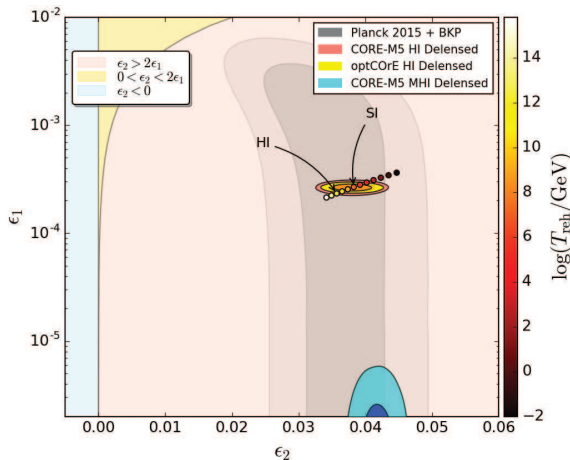


Marginalized forecasts for CORE²⁷. The small blue contours illustrate what a CORE detection would look like if $r \simeq 0.0042$ (as in the Starobinsky model), $r \simeq 0.001$ or when the tensors are undetectably small. The red contours correspond to forecasts for LITEBIRD.

²⁷F. Finelli *et al.*, arXiv:1612.08270 [astro-ph.CO].



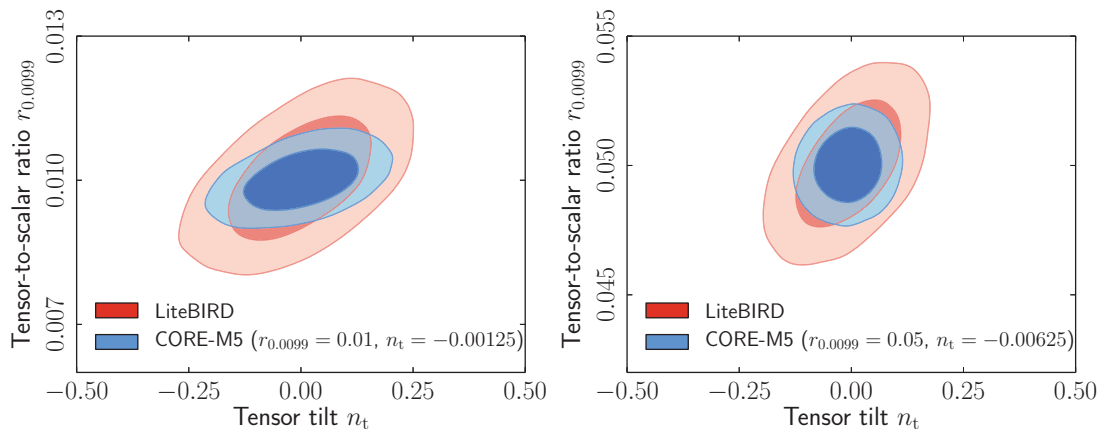
Discriminating between different post-inflationary dynamics



Marginalized forecasts for CORE²⁸. CORE can, in principle, distinguish between Higgs inflation (HI) and Starobinsky inflation (SI), which share the same inflationary potential, but have different reheating temperatures (around 10^{12} GeV for HI and 10^8 GeV for SI).

²⁸F. Finelli *et al.*, arXiv:1612.08270 [astro-ph.CO].

CORE forecasts for the slow roll consistency relation



Marginalized forecasts for the slow roll consistency relation corresponding to two different values of the tensor-to-scalar ratio²⁹. Deviations from the consistency relation would imply inflation driven by multiple fields.

²⁹F. Finelli *et al.*, arXiv:1612.08270 [astro-ph.CO].

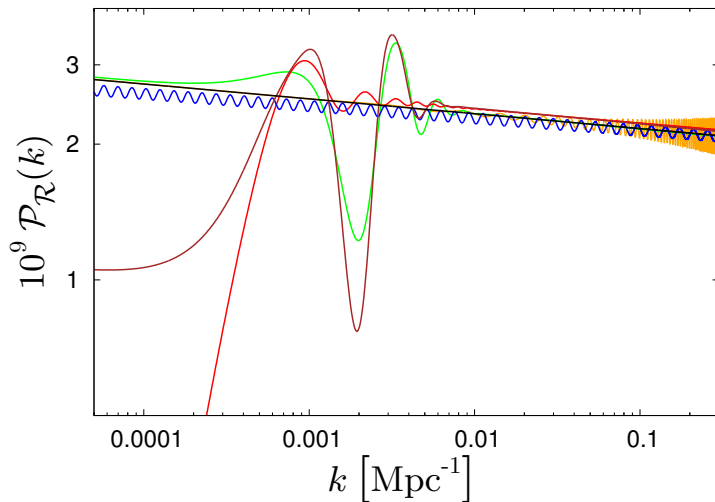


Plan of the talk

- 1 The inflationary paradigm
- 2 The power spectra generated during inflation
- 3 Constraints on the primordial power spectra from Planck
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- 6 'Anomalies'**
- 7 Expertise in India
- 8 Summary



Power spectra with features



Primordial power spectra with features that lead to an improved fit to the data than the conventional, nearly scale, invariant spectra³⁰.

³⁰Planck Collaboration (P. A. R. Ade *et al.*), *Astron. Astrophys.* **594**, A20 (2016).



Inflationary models permitting deviations from slow roll

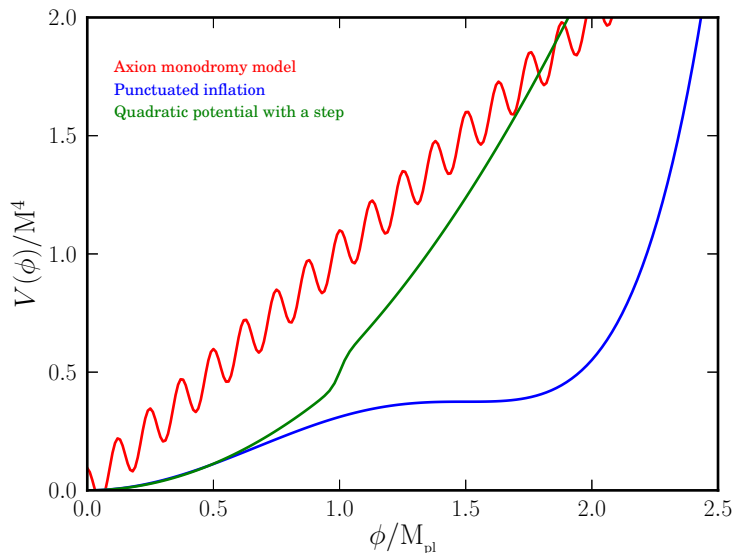
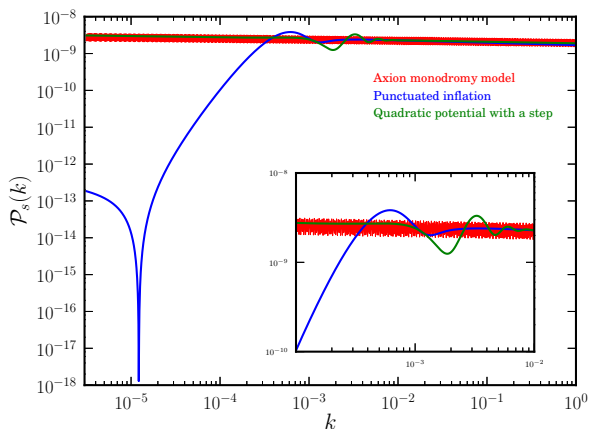


Illustration of potentials that admit departures from slow roll.



Spectra leading to an improved fit to the CMB data

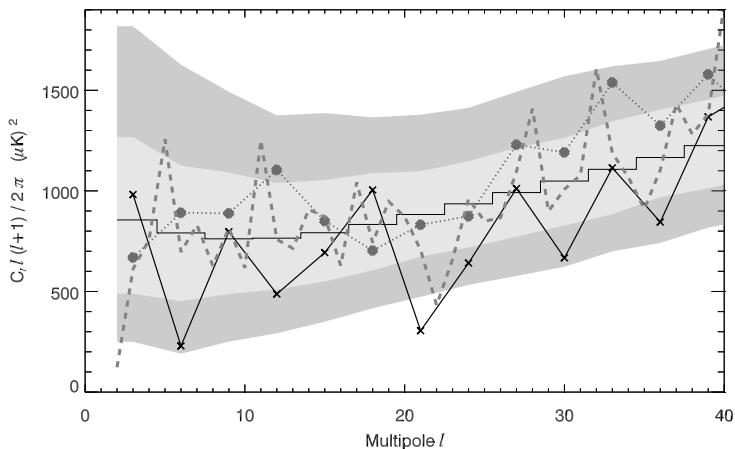


The scalar power spectra in different inflationary models that lead to a better fit to the CMB data than the conventional power law spectrum³¹.

³¹R. K. Jain, P. Chingangbam, J.-O. Gong, L. Sriramkumar and T. Souradeep, JCAP **0901**, 009 (2009);
 D. K. Hazra, M. Aich, R. K. Jain, L. Sriramkumar and T. Souradeep, JCAP **1010**, 008 (2010);
 M. Aich, D. K. Hazra, L. Sriramkumar and T. Souradeep, Phys. Rev. D **87**, 083526 (2013).



Hemispherical power asymmetry

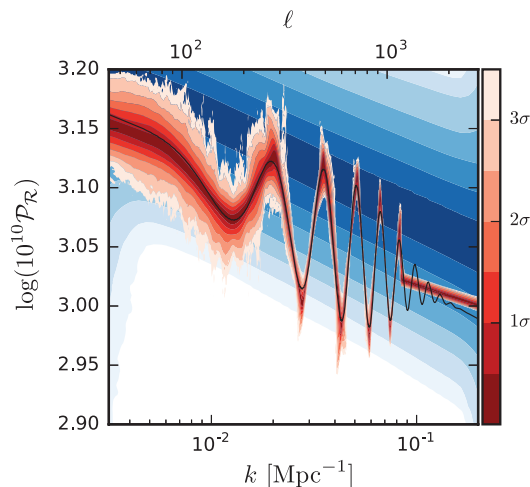
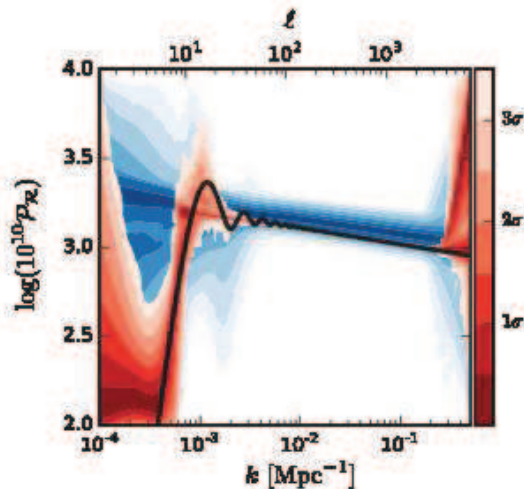


The three jagged lines show the binned angular power spectrum calculated over the whole unmasked sky (dashed), northern hemisphere (solid line, with crosses), and southern hemisphere (dotted line, with circles)³².

³²H. K. Eriksen, F. K. Hansen, A. J. Banday, K. M. Gorski and P. B. Lilje, *Astrophys. J.* **605**, 14 (2004).



Reconstruction of primordial spectra with features



Reconstructing a simulated power spectrum with features (black lines) for a CORE experiment (in red), compared to existing constraints provided by Planck (in blue)³³.

³³F. Finelli *et al.*, arXiv:1612.08270 [astro-ph.CO].



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Expertise in India I

- ◆ **IIT Madras** – Features in the primordial spectrum and comparison of models with the data, computation of primordial non-Gaussianities
- ◆ **IIA, IISc** – Effects due to gauge fields during inflation, measures of non-Gaussianities, non-trivial post-inflationary dynamics
- ◆ **IoP** – Models of inflation motivated by string theory, initial conditions during inflation
- ◆ **IUCAA** – Constructing viable models of inflation, features in the primordial spectrum and comparison of models with the data, deviations from statistical isotropy, Generation of primordial magnetic fields
- ◆ **IIT Mumbai, TIFR** – Models of inflation motivated by string theory and modified gravity, characterizing non-Gaussianities, quantum-to-classical transition of primordial perturbations
- ◆ **ISI Kolkata, SINP** – Models of inflationary motivated by string theory, effective field theories of inflation



Expertise in India II

- ◆ **PRL** – Models of inflation involving modified gravity and non-minimal coupling, imprints of pre-inflationary dynamics, comparison of models with the data
- ◆ **HRI** – Models of inflationary models motivated by string theory
- ◆ **IIT Kanpur** – Models of inflation, Deviations from statistical isotropy, quantum-to-classical transition of primordial perturbations
- ◆ **Jamia Milia Islamia, University of Delhi** – Non-canonical models of inflation, generation of primordial magnetic fields



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Summary

- ◆ A nearly scale invariant primordial spectrum as is generated in slow roll inflation is remarkably consistent with the cosmological data.

³⁴ J. Martin, C. Ringeval and V. Vennin, *Phys. Dark Univ.* **5–6**, 75 (2014).

³⁵ J. R. Fergusson, H. F. Gruetjen, E. P. S. Shellard and M. Liguori, *Phys. Rev. D* **91**, 023502 (2015).



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- ◆ It is important that a systematic search involving the scalar and the tensor power spectra³⁴, the scalar and the tensor bispectra and the cross correlations is carried to arrive at a smallest possible subset of viable inflationary models³⁵. Further, precise observations of the CMB anisotropies can play a significant role towards this effort.

³⁴ J. Martin, C. Ringeval and V. Vennin, *Phys. Dark Univ.* **5–6**, 75 (2014).

³⁵ J. R. Fergusson, H. F. Gruetjen, E. P. S. Shellard and M. Liguori, *Phys. Rev. D* **91**, 023502 (2015).



Thank you for your attention